



Answer Key

(Step-By-Step Mathematics 6)



Unit 1 Algebra

Drills

Exercise 1

- | | |
|-----------------------------|-------------------|
| 1. The sum of 4 and q | L. $25 + j$ |
| 2. t divided by 45 | E. $4 + q$ |
| 3. The product of 9 and f | I. $n - 6$ |
| 4. Subtract 6 from n | V. $g - 18$ |
| 5. Add 12 to n | R. $n + 12$ |
| 6. 18 less than g | B. $9f$ |
| 7. 25 more than j | A. $\frac{t}{45}$ |

$\frac{V}{6}$ A $\frac{R}{5}$ I $\frac{A}{2}$ B $\frac{L}{7}$ $\frac{E}{1}$

Exercise 2

- | | |
|---|--------------------|
| 1. $5r + 3r = 8r$ | 7j |
| 2. $45n - 21n + 8n$
$= 24n + 8n$
$= 32n$ | 8r |
| 3. $7 \times j = 7j$ | 33u |
| 4. $(24 - z) \div 6$
$= \frac{24 - z}{6}$ | 9t |
| 5. $29u - 7u + 11u$
$= 22u + 11u$
$= 33u$ | 24k |
| 6. $8t + 4t - 3t$
$= 12t - 3t$
$= 9t$ | 32n |
| 7. $36k - 12k = 24k$ | $\frac{24 - z}{6}$ |

Exercise 3

1.	$4n + 6n$	R	6
2.	$n + \frac{n}{4}$	A	20
3.	$\frac{24}{n} + 6n$	G	896
4.	$\frac{3n}{2} + 2n - n$	L	80
5.	$8n - 3n$	B	40
6.	$\frac{3n + 24}{8}$	A	10
7.	$\frac{3n + 5n}{2}$	E	32
8.	$56 \times 2n$	I	51

A L G E B R A !
 10 20 51 32 40 80 6 896

1. $4n + 6n$
 $= 10n$
 $= 10(8)$
 $= 80$

2. $n + \frac{n}{4}$
 $= 8 + \frac{8}{4}$
 $= 8 + 2$
 $= 10$

3. $\frac{24}{n} + 6n$
 $= \frac{24}{8} + 6(8)$
 $= 3 + 48$
 $= 51$

4. $\frac{3n}{2} + 2n - n$
 $= \frac{3n}{2} + n$
 $= \frac{3(8)}{2} + 8$
 $= \frac{24}{2} + 8$
 $= 12 + 8$
 $= 20$

5. $8n - 3n$
 $= 5n$
 $= 5(8)$
 $= 40$

6. $\frac{3n + 24}{8}$
 $= \frac{3(8) + 24}{8}$
 $= \frac{24 + 24}{8}$
 $= \frac{48}{8}$
 $= 6$

7. $\frac{3n + 5n}{2}$
 $= \frac{8n}{2}$
 $= 4n$
 $= 4(8)$
 $= 32$

8. $56 \times 2n$
 $= 56 \times 2(8)$
 $= 56 \times 16$
 $= 896$

Exercise 4

- Length of Rope B
 $= (a + 8)$ cm
- Number of necklaces Emily made
 $= w - 34$
- Number of marbles in each bag
 $= \frac{y}{7}$
- Total number of bars of chocolates
 $= 25f$
- Wife's monthly income
 $= \$\left(\frac{u}{2}\right)$
- Cost of scanner
 $= \$(t - 200)$
- Number of stickers Sean collected
 $= (k + 15)$ stickers
- Average number of cupcakes
 $= \left(\frac{q}{4}\right)$ cupcakes
- Area of triangle
 $= \frac{1}{2} \times p \times s^4$
 $= 4p$ cm²

Perform

Exercise 1

- (2)
 $4x + 2x - x + 5$
 $= 6x - x + 5$
 $= \underline{5x + 5}$
- (1)
Number of stamps Bryan collected
 $= \underline{q + 5}$

- (3)
When $p = 9$,
 $9p + 12 - p$
 $= 9(9) + 12 - 9$
 $= 81 + 12 - 9$
 $= 93 - 9$
 $= \underline{84}$
- (1)
 $7w + 15 - w + 7$
 $= 7w - w + 15 + 7$
 $= \underline{6w + 22}$
- (2)
Perimeter of square
 $= 4 \times b$
 $= \underline{4b}$ cm
- (2)
 $9t + 4 - 3t - 2$
 $= 9t - 3t + 4 - 2$
 $= \underline{6t + 2}$
- (1)
When $r = 5$,
 $\frac{8r + 20}{5} = \frac{8(5) + 20}{5}$
 $= \frac{40 + 20}{5}$
 $= \frac{60}{5}$
 $= \underline{12}$
- (1)
Area of square base
 $= 2 \times 2$
 $= 4$ cm²

Height
 $= 12a \div 4$
 $= \frac{12a}{4}$
 $= \underline{3a}$ cm

9. (3)
 $7g - g + 6 - 3g$
 $= 6g + 6 - 3g$
 $= \underline{3g + 6}$

10. (3)
 When $d = 12$,
 $20d + 25 - 5d$
 $= 20(12) + 25 - 5(12)$
 $= 240 + 25 - 60$
 $= 265 - 60$
 $= \underline{205}$

Exercise 2

1. Amount she had at first
 $= t \times \$29 + \123
 $= \$29t + \123
 $= \underline{\$(29t + 123)}$

2. Amount of change
 $= \$50 - (12 \times \$f)$
 $= \underline{\$(50 - 12f)}$

3. Mass of 1 packet of sugar
 $= 6h \text{ kg} \div 10$
 $= \frac{6h}{10} \text{ kg}$
 $= \frac{3h}{5} \text{ kg}$
 Total mass of 45 such packets of sugar
 $= 45 \times \frac{3h}{5} \text{ kg}$
 $= \underline{27h \text{ kg}}$

4. Brother's age
 $= (p - 5) \text{ years}$

Total age
 $= p + p - 5$
 $= \underline{(2p - 5) \text{ years}}$

5. Number of badges Alex had
 $= 2 \times 3k$
 $= 6k \text{ badges}$

Number of badges Brenda had
 $= \underline{(6k + 4) \text{ badges}}$

6. Length + Breadth = $(\frac{4h + 12}{2}) \text{ cm}$
 $= (2h + 6) \text{ cm}$
 Length + 2 = $2h + 6$
 Length = $2h + 6 - 2$
 $= \underline{(2h + 4) \text{ cm}}$

Achieve

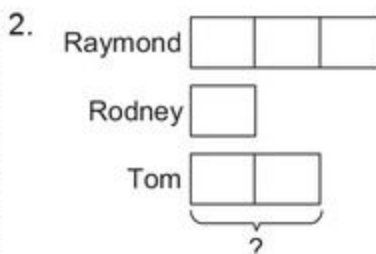
Exercise 1

1. Capacity of container
 $= 75k$
 $= 75(8)$
 $= 600 \text{ l}$

Half the container
 $= 600 \text{ l} \div 2$
 $= 300 \text{ l}$

$5 \text{ l} \rightarrow 1 \text{ min}$
 $1 \text{ l} \rightarrow \frac{1}{5} \text{ min}$
 $300 \text{ l} \rightarrow 300 \times \frac{1}{5} \text{ min} = 60 \text{ min}$
 $= 1 \text{ h}$

It will take 1 hour to fill half the container.



1 unit = $62a \text{ kg}$
 2 units = $2 \times 62a \text{ kg}$
 $= 124a \text{ kg}$

Tom's mass is $124a \text{ kg}$.

$$\begin{aligned}
 3. \quad & \text{Total number of stamps} \\
 & = (7 \times p) + 6 \\
 & = 7p + 6
 \end{aligned}$$

When $p = 105$,

$$\begin{aligned}
 7p + 6 & = 7(105) + 6 \\
 & = 735 + 6 \\
 & = 741
 \end{aligned}$$

The total number of stamps is **741**.

$$\begin{aligned}
 4. \quad & \text{Perimeter of rectangle} = 24n \\
 & \text{Length} + \text{Breadth} = 24n \div 2 \\
 & \quad \quad \quad = 12n
 \end{aligned}$$

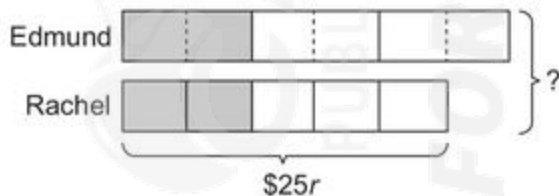
$$\begin{aligned}
 18 + \text{Breadth} & = 12n \\
 \text{Breadth} & = (12n - 18) \text{ cm}
 \end{aligned}$$

Its breadth is **$(12n - 18)$ cm**.

$$\begin{aligned}
 5. \quad & 6 \times \$3 = \$18 \\
 & \$122 + \$18 = \$140 \\
 & \$140 \div 14 = \$10 \\
 & \$10 - \$3 = \$7
 \end{aligned}$$

The admission fee to the Science Centre is **\$7**.

6.



$$5 \text{ units} = \$25r$$

$$1 \text{ unit} = \$\left(\frac{25r}{5}\right) = \$5r$$

$$\begin{aligned}
 11 \text{ units} & = 11 \times \$5r \\
 & = \$55r
 \end{aligned}$$

They save **\$55r** in all.

$$\begin{aligned}
 7. \quad & \text{Total number of T-shirts sold} \\
 & = 3y + (5y + 7) \\
 & = 8y + 7
 \end{aligned}$$

$$\begin{aligned}
 8y + 7 & = 135 \\
 8y & = 135 - 7 \\
 & = 128 \\
 y & = 128 \div 8 \\
 & = 16
 \end{aligned}$$

The value of y is **16**.

$$\begin{aligned}
 8. \quad & \text{Number of postcards George had} \\
 & = (5 + 2x) + 4x \\
 & = 6x + 5
 \end{aligned}$$

Number of postcards Tim had

$$= \frac{6x + 5}{2}$$

Tim had $\left(\frac{6x + 5}{2}\right)$ postcards.

$$\begin{aligned}
 9. \quad & \text{Number of stickers Ben has} \\
 & = (p + 5) + p \\
 & = 2p + 5
 \end{aligned}$$

Total number of stickers both children have

$$\begin{aligned}
 & = p + 5 + (2p + 5) \\
 & = 3p + 10
 \end{aligned}$$

$$\begin{aligned}
 3p + 10 & = 64 \\
 3p & = 64 - 10 \\
 3p & = 54 \\
 p & = 54 \div 3 \\
 & = 18
 \end{aligned}$$

The value of p is **18**.

10. (a) Number of beads left
 $= n - 9$

Number of beads in each bottle
 $= \frac{n - 9}{5}$

The number of beads in each bottle is $\left(\frac{n - 9}{5}\right)$.

(b) When $n = 144$,

$$\begin{aligned} \frac{n - 9}{5} &= \frac{144 - 9}{5} \\ &= \frac{135}{5} \\ &= 27 \end{aligned}$$

There were 27 beads in each bottle.

Unit 2 Fractions

Drills

Exercise 1

1. $3 \div \frac{1}{2}$
 $= 3 \times 2$
 $= 6$

2. $1 \div \frac{1}{4}$
 $= 1 \times 4$
 $= 4$

3. $2 \div \frac{1}{6}$
 $= 2 \times 6$
 $= 12$

4. $9 \div \frac{6}{7}$
 $= 9 \times \frac{7}{6}$
 $= \frac{21}{2}$
 $= 10\frac{1}{2}$

5. $5 \div \frac{2}{3}$
 $= 5 \times \frac{3}{2}$
 $= \frac{15}{2}$
 $= 7\frac{1}{2}$

6. $8 \div \frac{4}{5}$
 $= 8 \times \frac{5}{4}$
 $= 10$

$$\begin{aligned} 7. \quad & \frac{2}{3} \div 9 \\ & = \frac{2}{3} \times \frac{1}{9} \\ & = \frac{2}{27} \end{aligned}$$

$$\begin{aligned} 8. \quad & \frac{1}{4} \div 3 \\ & = \frac{1}{4} \times \frac{1}{3} \\ & = \frac{1}{12} \end{aligned}$$

$$\begin{aligned} 9. \quad & \frac{5}{7} \div 10 \\ & = \frac{5}{7} \times \frac{1}{10} \\ & = \frac{1}{14} \end{aligned}$$

$$\begin{aligned} 10. \quad & \frac{3}{4} \div 6 \\ & = \frac{3}{4} \times \frac{1}{6} \\ & = \frac{1}{8} \end{aligned}$$

$$\begin{aligned} 11. \quad & \frac{2}{5} \div 12 \\ & = \frac{2}{5} \times \frac{1}{12} \\ & = \frac{1}{30} \end{aligned}$$

$$\begin{aligned} 12. \quad & \frac{5}{8} \div 15 \\ & = \frac{5}{8} \times \frac{1}{15} \\ & = \frac{1}{24} \end{aligned}$$

$$\begin{aligned} 13. \quad & \frac{1}{2} \div \frac{1}{8} \\ & = \frac{1}{2} \times 8 \\ & = 4 \end{aligned}$$

$$\begin{aligned} 14. \quad & \frac{3}{5} \div \frac{3}{10} \\ & = \frac{3}{5} \times \frac{10}{3} \\ & = 2 \end{aligned}$$

$$\begin{aligned} 15. \quad & \frac{2}{3} \div \frac{5}{6} \\ & = \frac{2}{3} \times \frac{6}{5} \\ & = \frac{4}{5} \end{aligned}$$

$$\begin{aligned} 16. \quad & \frac{1}{4} \div \frac{1}{10} \\ & = \frac{1}{4} \times 10 \\ & = 2\frac{1}{2} \end{aligned}$$

$$\begin{aligned} 17. \quad & \frac{4}{9} \div \frac{2}{3} \\ & = \frac{4}{9} \times \frac{3}{2} \\ & = \frac{2}{3} \end{aligned}$$

$$\begin{aligned} 18. \quad & \frac{9}{10} \div \frac{2}{5} \\ & = \frac{9}{10} \times \frac{5}{2} \\ & = \frac{9}{4} \\ & = 2\frac{1}{4} \end{aligned}$$

$$\begin{aligned}
 19. \quad & \frac{5}{8} \div \frac{5}{11} \\
 &= \frac{5^1}{8} \times \frac{11}{5^1} \\
 &= \frac{11}{8} \\
 &= 1 \frac{3}{8}
 \end{aligned}$$

$$\begin{aligned}
 20. \quad & \frac{8}{15} \div \frac{4}{9} \\
 &= \frac{8^2}{15^5} \times \frac{9^3}{4^1} \\
 &= \frac{6}{5} \\
 &= 1 \frac{1}{5}
 \end{aligned}$$

Exercise 2

$$\begin{aligned}
 1. \quad & \frac{3}{4} \div \frac{1}{4} \\
 &= \frac{3}{1^4} \times 4^1 \\
 &= 3
 \end{aligned}$$

There are 3 quarters in $\frac{3}{4}$.

$$\begin{aligned}
 2. \quad & \frac{2}{3} \div \frac{1}{6} \\
 &= \frac{2}{1^3} \times 6^2 \\
 &= 4
 \end{aligned}$$

There are 4 sixths in $\frac{2}{3}$.

$$\begin{aligned}
 3. \quad & \frac{4}{5} \div \frac{1}{10} \\
 &= \frac{4}{1^5} \times 10^2 \\
 &= 8
 \end{aligned}$$

There are 8 tenths in $\frac{4}{5}$.

$$\begin{aligned}
 4. \quad & \frac{2}{3} \div \frac{1}{9} \\
 &= \frac{2}{1^3} \div 9^3 \\
 &= 6
 \end{aligned}$$

There are 6 ninths in $\frac{2}{3}$.

Perform

Exercise 1

$$\begin{aligned}
 1. \quad (1) \quad & 6 \div \frac{2}{3} \\
 &= \frac{3^6}{9} \times \frac{3}{2^1}
 \end{aligned}$$

$$\begin{aligned}
 2. \quad (3) \quad & \frac{2}{3} \div \frac{1}{3} \\
 &= \frac{2}{1^3} \times 3^1 \\
 &= 2
 \end{aligned}$$

$$\begin{aligned}
 3. \quad (4) \quad & 24 \div \frac{1}{2} \\
 &= 24 \times 2
 \end{aligned}$$

$$\begin{aligned}
 4. \quad (4) \quad & \frac{3}{4} \div 12 \\
 &= \frac{3}{4} \times \frac{1}{12}
 \end{aligned}$$

5. (2)
 Option (1): $\frac{1}{2} + \frac{1}{4}$
 $= \frac{2}{4} + \frac{1}{4}$
 $= \frac{3}{4}$

Option (2): $\frac{1}{2} \div \frac{1}{4}$
 $= \frac{1}{\cancel{2}} \times \cancel{4}_2$
 $= 2$ (✓)

Option (3): $\frac{1}{2} \times \frac{1}{4}$
 $= \frac{1}{8}$

Option (4): $\frac{1}{2} - \frac{1}{4}$
 $= \frac{2}{4} - \frac{1}{4}$
 $= \frac{1}{4}$

6. (4)
 Amount of orange juice in each bottle
 $= \frac{3}{5} \text{ l} \div 9$
 $= \frac{\cancel{3}}{5} \text{ l} \times \frac{1}{\cancel{9}_3}$
 $= \frac{1}{15} \text{ l}$

Exercise 2

1. $\frac{5}{\square} \div \frac{5}{6} = \frac{1}{2}$
 $\frac{5}{\square} = \frac{1}{2} \times \frac{5}{6}$
 $= \frac{5}{12}$

The missing number in the box is 12.

2. Other fraction
 $= \frac{1}{4} \div \frac{5}{8}$
 $= \frac{1}{\cancel{4}} \times \frac{\cancel{8}_2}{5}$
 $= \frac{2}{5}$

3. $\frac{3}{10}$ of fraction $\rightarrow \frac{3}{14}$
 $\frac{1}{10}$ of fraction $\rightarrow \frac{3}{14} \div 3$
 $= \frac{\cancel{3}}{14} \times \frac{1}{\cancel{3}_1}$
 $= \frac{1}{14}$
 $\frac{10}{10}$ of fraction $\rightarrow 10 \times \frac{1}{14}$
 $= \frac{10}{14}$
 $= \frac{5}{7}$

4. Number of pieces
 $= 12 \div \frac{3}{10}$
 $= 12 \times \frac{10}{\cancel{3}_1}$
 $= 40$

5. Length of square
 $= \frac{3}{5} \text{ m} \div 4$
 $= \frac{3}{5} \text{ m} \times \frac{1}{4}$
 $= \frac{3}{20} \text{ m}$

6. Length of each piece
 $= \frac{8}{9} \text{ m} \div 16$
 $= \frac{\cancel{8}}{9} \text{ m} \times \frac{1}{\cancel{16}_2}$
 $= \frac{1}{18} \text{ m}$

7. Number of bottles

$$\begin{aligned} &= \frac{3}{4} \div \frac{1}{8} \\ &= \frac{3}{4} \times 8^2 \\ &= 6 \end{aligned}$$

8. Number of children

$$\begin{aligned} &= \frac{2}{3} \div \frac{1}{6} \\ &= \frac{2}{3} \times 6^2 \\ &= 4 \end{aligned}$$

9. $1 - \frac{2}{5} = \frac{3}{5}$

Fraction of each slice

$$\begin{aligned} &= \frac{3}{5} \div 6 \\ &= \frac{3}{5} \times \frac{1}{6^2} \\ &= \frac{1}{10} \end{aligned}$$

Achieve

Exercise 1

1. $1 - \frac{1}{6} = \frac{5}{6}$

Fraction of jug left with orange juice

$$\begin{aligned} &= \frac{5}{6} \times \frac{3^1}{5^1} \\ &= \frac{1}{2} \end{aligned}$$

$\frac{1}{2}$ of the jug is still left with orange juice.

2. $1 - \frac{1}{3} = \frac{2}{3}$
 $\frac{2}{3} \div 3 = \frac{2}{3} \times \frac{1}{3}$
 $= \frac{2}{9}$

Dan paid $\frac{2}{9}$ of the cost.

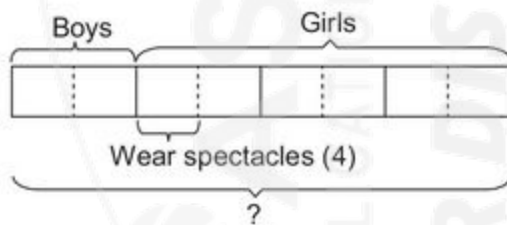
3. Number of packets

$$\begin{aligned} &= 45 \div \frac{2}{3} \\ &= 45 \times \frac{3}{2} \\ &= \frac{135}{2} \\ &= 67 \frac{1}{2} \end{aligned}$$

$$\frac{1}{2} \times \frac{2^1}{3} \text{ kg} = \frac{1}{3} \text{ kg}$$

67 packets can be packed and $\frac{1}{3}$ kg of salt remains.

4.



1 unit = 4 pupils
8 units = 8×4
= 32 pupils

There are 32 pupils in the class.

5. $1 - \frac{2}{5} = \frac{3}{5}$

Fraction of beads used to make 3 bracelets

$$\begin{aligned} &= \frac{3}{5} \times \frac{3^1}{5^1} \\ &= \frac{1}{2} \end{aligned}$$

Fraction of beads used to make 1 bracelet

$$= \frac{1}{2} \div 3$$

$$= \frac{1}{2} \times \frac{1}{3}$$

$$= \frac{1}{6}$$

She used $\frac{1}{6}$ of her beads to make 1 bracelet.

6. $11\frac{3}{5} \text{ m} - 2\frac{3}{5} \text{ m} = 9 \text{ m}$

$$75 \text{ cm} = \frac{75}{100} \text{ m}$$

$$= \frac{3}{4} \text{ m}$$

Number of cushions

$$= 9 \div \frac{3}{4}$$

$$= 9 \times \frac{4}{3}$$

$$= 12$$

He made 12 cushions.

7. Number of bags of rice
 $= \$120 \div \8
 $= 15$

Total mass of rice
 $= 15 \times 5 \text{ kg}$
 $= 75 \text{ kg}$

Number of packets

$$= 75 \div \frac{3}{4}$$

$$= 75 \times \frac{4}{3}$$

$$= 100$$

He would get 100 packets.

8. $5\frac{1}{2} \text{ l} - 4\frac{3}{4} \text{ l}$
 $= 5\frac{2}{4} \text{ l} - 4\frac{3}{4} \text{ l}$
 $= 4\frac{6}{4} \text{ l} - 4\frac{3}{4} \text{ l}$
 $= \frac{3}{4} \text{ l}$

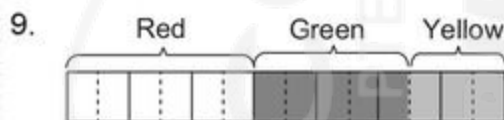
Amount of milk in each cup

$$= \frac{3}{4} \text{ l} \div 6$$

$$= \frac{3}{4} \text{ l} \times \frac{1}{6}$$

$$= \frac{1}{8} \text{ l}$$

She poured $\frac{1}{8}$ l milk into each cup.



$$6 \text{ units} - 3 \text{ units} = 3 \text{ units}$$

$$3 \text{ units} = 36 \text{ marbles}$$

$$1 \text{ unit} = 36 \div 3$$

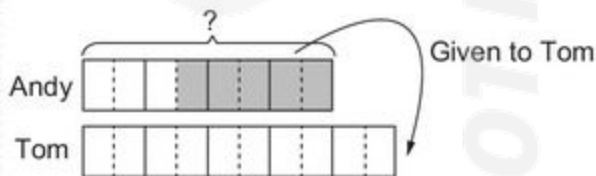
$$= 12 \text{ marbles}$$

$$5 \text{ units} = 5 \times 12$$

$$= 60 \text{ marbles}$$

He had 60 green marbles.

10. Before:



After:



$$\begin{aligned}
 12 \text{ units} &= 204 \text{ marbles} \\
 1 \text{ unit} &= 204 \div 12 \\
 &= 17 \text{ marbles} \\
 8 \text{ units} &= 8 \times 17 \\
 &= 136 \text{ marbles}
 \end{aligned}$$

Andy had 136 marbles at first.

$$\begin{aligned}
 11. \quad \frac{3}{1\frac{1}{4}} \times 160 \text{ kg} &= 120 \text{ kg} \\
 160 \text{ kg} - 120 \text{ kg} &= 40 \text{ kg}
 \end{aligned}$$

$$\begin{aligned}
 \text{Number of packets} \\
 &= 40 \div \frac{4}{5} \\
 &= \frac{10}{4} \times \frac{5}{1} \\
 &= 50
 \end{aligned}$$

$$\begin{aligned}
 \text{Amount received} \\
 &= (120 \times \$1.05) + (50 \times \$0.80) \\
 &= \$126 + \$40 \\
 &= \$166
 \end{aligned}$$

He received \$166 from selling all the sugar.

Unit 3 Ratio

Drills

Exercise 1

- $\$100 - \$70 = \$30$
Charles : Jordan
 $\frac{70}{70} : \frac{30}{30}$
 $= 7 : 3$
- $42 + 36 = 78$
Sean : Total
 $\frac{36}{36} : \frac{78}{78}$
 $= 6 : 13$
- $\text{Number of red beads} = 22 + 8 = 30$
Red : Green : Blue
 $\frac{30}{30} : \frac{22}{22} : \frac{18}{18}$
 $= 15 : 11 : 9$
- $9 - 2 - 3 = 4$
Mother : Sister : Matthew
 $\frac{4}{4} : \frac{2}{2} : \frac{3}{3}$
- $33 + 24 = 57$
Mason : Total
 $\frac{33}{33} : \frac{57}{57}$
 $= 11 : 19$
- $\$480 - \$80 - \$240 = \160
Transport : Food : Games
 $\frac{160}{160} : \frac{80}{80} : \frac{240}{240}$
 $= 16 : 8 : 24$
 $= 2 : 1 : 3$
- $4 + 7 = 11$
String A : String B : Total
 $\frac{4}{4} : \frac{7}{7} : \frac{11}{11}$

Exercise 2

- Black : Coloured
7 : 5
7 units + 5 units = 12 units
Fraction of black buttons
= $\frac{7}{12}$
- (a) Adults : Children
11 : 6
Required fraction = $\frac{6}{11}$
(b) 11 units + 6 units = 17 units
Required fraction = $\frac{11}{17}$
- Julie : Matthias : Joe
3 : 7 : 8
3 units + 7 units + 8 units = 18 units
Fraction of money Matthias received
= $\frac{7}{18}$
- Bracelets : Necklaces
4 : 5
4 units + 5 units = 9 units
Required fraction = $\frac{4}{9}$

Perform

Exercise 1

- (2)
Alice : John : Tom
7 : 3 : 2
7 units + 3 units + 2 units
= 12 units
12 units = \$3600
1 unit = \$3600 ÷ 12
= \$300
2 units = 2 × \$300
= \$600
Tom received \$600.

2. (2)

$$+5 \left(\begin{array}{l} 125 : 70 \\ \hline = 25 : 14 \end{array} \right) -5$$

The missing number is 25.

3. (4)

Charles : Megan : Anthony
2 : 5 : 6

$$2 \text{ units} + 5 \text{ units} + 6 \text{ units} \\ = 13 \text{ units}$$

Fraction of candies Anthony received

$$= \frac{6}{13}$$

4. (3)

$$54 + 30 = 84$$

There are 84 red apples.

$$54 + 84 = 138$$

There 138 green and red apples altogether.

Red : Total
84 : 138
= 14 : 23

5. (1)

Number of girls left
= 90 - 12
= 78

Total number of children left
= 63 + 78
= 141

Boys : Total
63 : 141
= 21 : 47

6. (2)

$$\frac{\text{Orange syrup}}{4} : \frac{\text{Water}}{9}$$

$$\begin{aligned} 9 \text{ units} &= 324 \text{ l} \\ 1 \text{ unit} &= 324 \text{ l} \div 9 \\ &= 36 \text{ l} \\ 4 \text{ units} &= 4 \times 36 \text{ l} \\ &= 144 \text{ l} \end{aligned}$$

144 l of orange syrup are required.

7. (3)

$$\frac{\text{Leslie}}{1} : \frac{\text{Lena}}{3}$$

$$\begin{aligned} 3 \text{ units} - 1 \text{ unit} &= 2 \text{ units} \\ 2 \text{ units} &= \$428 \\ 1 \text{ unit} &= \$428 \div 2 \\ &= \$214 \\ 3 \text{ units} &= 3 \times \$214 \\ &= \$642 \end{aligned}$$

Lena has \$642.

Exercise 2

1.
$$\frac{\text{Bag A}}{7} : \frac{\text{Bag B}}{6}$$

$$\begin{aligned} \frac{2}{7} \times 7 \text{ units} &= 2 \text{ units} \\ 2 \text{ units} &= 40 \text{ pens} \\ 1 \text{ unit} &= 40 \div 2 \\ &= 20 \text{ pens} \end{aligned}$$

$$\begin{aligned} 7 \text{ units} + 6 \text{ units} &= 13 \text{ units} \\ 13 \text{ units} &= 13 \times 20 \\ &= 260 \text{ pens} \end{aligned}$$

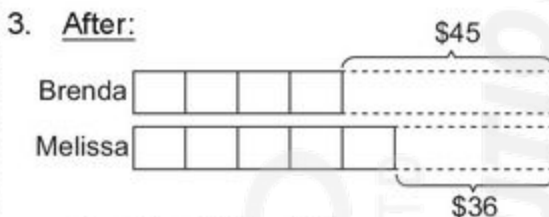
There are **260** pens in all.

2.
$$\frac{\text{White}}{3} : \frac{\text{Red}}{7}$$

$$3 \text{ units} + 7 \text{ units} = 10 \text{ units}$$

$$\begin{aligned} 7 \text{ units} &= 91 \text{ roses} \\ 1 \text{ unit} &= 91 \div 7 \\ &= 13 \text{ roses} \\ 10 \text{ units} &= 10 \times 13 \\ &= 130 \text{ roses} \end{aligned}$$

There are **130** roses altogether.

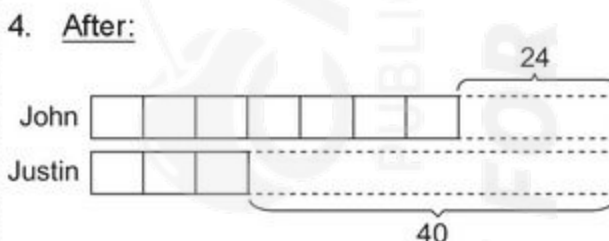


$$\begin{aligned} 1 \text{ unit} &= \$45 - \$36 \\ &= \$9 \\ 4 \text{ units} &= 4 \times \$9 \\ &= \$36 \end{aligned}$$

$$\begin{aligned} \$36 + \$45 &= \$81 \\ \text{Brenda had } &\$81 \text{ at first.} \end{aligned}$$

$$2 \times \$81 = \$162$$

They had **\$162** at first.



$$\begin{aligned} 4 \text{ units} &= 40 - 24 \\ &= 16 \text{ stickers} \\ 1 \text{ unit} &= 16 \div 4 \\ &= 4 \text{ stickers} \\ 7 \text{ units} &= 7 \times 4 \\ &= 28 \text{ stickers} \end{aligned}$$

$$28 + 24 = 52$$

John had **52** stickers at first.

Exercise 3

1. (a) $\frac{\text{Flour}}{5} : \frac{\text{Sugar}}{2}$

$$\begin{aligned}1 \text{ kg} &= 1000 \text{ g} \\5 \text{ units} &= 1000 \text{ g} \\1 \text{ unit} &= 1000 \text{ g} \div 5 \\&= 200 \text{ g} \\2 \text{ units} &= 2 \times 200 \text{ g} \\&= 400 \text{ g}\end{aligned}$$

She used **400 g** of sugar.

(b) $2 \text{ parts} = 240 \text{ g}$
 $1 \text{ part} = 240 \text{ g} \div 2$
 $= 120 \text{ g}$
 $5 \text{ parts} = 5 \times 120 \text{ g}$
 $= 600 \text{ g}$

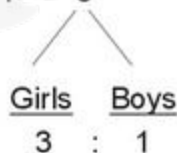
600 g of flour was needed.

2. $\frac{\text{Boys}}{5} : \frac{\text{Girls}}{6}$

$$\begin{aligned}6 \text{ units} &= 156 \text{ children} \\1 \text{ unit} &= 156 \div 6 \\&= 26 \text{ children} \\5 \text{ units} &= 5 \times 26 \\&= 130 \text{ children}\end{aligned}$$

There were **130** boys.

3. $\frac{\text{Teachers}}{3} : \frac{\text{Children}}{5}$



$$\begin{aligned}3 \text{ units} &= 1500 \text{ children} \\1 \text{ unit} &= 1500 \div 3 \\&= 500 \text{ children} \\4 \text{ units} &= 4 \times 500 \text{ children} \\&= 2000 \text{ children}\end{aligned}$$

There are **2000** children.

$$\begin{aligned}5 \text{ parts} &= 2000 \text{ people} \\1 \text{ part} &= 2000 \div 5 \\&= 400 \text{ people} \\8 \text{ parts} &= 8 \times 400 \\&= 3200 \text{ people}\end{aligned}$$

There are **3200** people altogether.

4. $\frac{\text{Tulips}}{3} : \frac{\text{Roses}}{5}$

```
graph TD
    Tulips[Tulips  
3] --- Pink[Pink  
2]
    Tulips --- Yellow[Yellow  
1]
```

$$\frac{\text{Pink tulips}}{2} : \frac{\text{Yellow tulips}}{1} : \frac{\text{Roses}}{5}$$

$$\begin{aligned}2 \text{ units} &= 10 \text{ flowers} \\1 \text{ unit} &= 10 \div 2 \\&= 5 \text{ flowers} \\6 \text{ units} &= 6 \times 5 \\&= 30 \text{ flowers}\end{aligned}$$

The total numbers of yellow tulips and roses is **30**.

Exercise 4

1. $\frac{\text{Men}}{3} : \frac{\text{Women}}{7}$

$$7 \text{ units} - 3 \text{ units} = 4 \text{ units}$$

$$\begin{aligned}4 \text{ units} &= 36 \text{ people} \\1 \text{ unit} &= 36 \div 4 \\&= 9 \text{ people} \\10 \text{ units} &= 10 \times 9 \\&= 90 \text{ people}\end{aligned}$$

There are **90** people altogether.

2. $\frac{\text{Matthew}}{4} : \frac{\text{Ray}}{9}$

$$9 \text{ units} - 4 \text{ units} = 5 \text{ units}$$

$$5 \text{ units} = 25 \text{ sweets}$$

$$1 \text{ unit} = 25 \div 5$$

$$= 5 \text{ sweets}$$

$$13 \text{ units} = 13 \times 5$$

$$= 65 \text{ sweets}$$

The total number of sweets shared was **65**.

3. $\text{Length} + \text{Breadth} = 360 \text{ cm} \div 2$
 $= 180 \text{ cm}$

$$\frac{\text{Length}}{7} : \frac{\text{Breadth}}{3}$$

$$7 \text{ units} + 3 \text{ units} = 10 \text{ units}$$

$$10 \text{ units} = 180 \text{ cm}$$

$$1 \text{ unit} = 180 \div 10$$

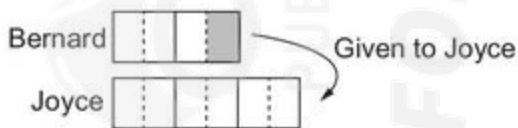
$$= 18 \text{ cm}$$

$$3 \text{ units} = 3 \times 18 \text{ cm}$$

$$= 54 \text{ cm}$$

Its breadth is **54 cm**.

4. Before:



New ratio:

$$\frac{\text{Bernard}}{3} : \frac{\text{Joyce}}{7}$$

5. $\frac{\text{Boys}}{5} : \frac{\text{Girls}}{3}$

$$8 \text{ units} = 280 \text{ children}$$

$$1 \text{ unit} = 280 \div 8$$

$$= 35 \text{ children}$$

$$5 \text{ units} - 3 \text{ units} = 2 \text{ units}$$

$$2 \text{ units} = 2 \times 35$$

$$= 70 \text{ children}$$

There were **70** more boys than girls.

6. $\frac{\text{Red}}{1} : \frac{\text{Yellow}}{3}$

$$1 \text{ unit} + 3 \text{ units} = 4 \text{ units}$$

$$4 \text{ units} = 24 \text{ l}$$

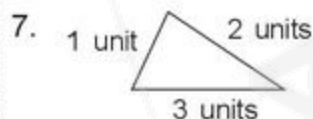
$$1 \text{ unit} = 24 \text{ l} \div 4$$

$$= 6 \text{ l}$$

$$3 \text{ units} = 3 \times 6 \text{ l}$$

$$= 18 \text{ l}$$

He used **18 l** of yellow paint.



$$1 \text{ unit} + 2 \text{ units} + 3 \text{ units} = 6 \text{ units}$$

$$6 \text{ units} = 126 \text{ cm}$$

$$1 \text{ unit} = 126 \text{ cm} \div 6$$

$$= 21 \text{ cm}$$

$$3 \text{ units} - 1 \text{ unit} = 2 \text{ units}$$

$$2 \text{ units} = 2 \times 21 \text{ cm}$$

$$= 42 \text{ cm}$$

The difference between the longest and shortest sides is **42 cm**.

Achieve

Exercise 1

1. $\frac{\text{Blue}}{1 \times 5} : \frac{\text{Green and Red}}{2 \times 5}$

$$= 5 : 10$$

$$\begin{array}{cc} \text{Green} & : & \text{Red} \\ \frac{2 \times 2}{4} & : & \frac{3 \times 2}{6} \end{array}$$

$$\frac{\text{Blue}}{5} : \frac{\text{Green}}{4} : \frac{\text{Red}}{6}$$

$$5 \text{ units} + 4 \text{ units} + 6 \text{ units} = 15 \text{ units}$$

Fraction of blue marbles

$$= \frac{5}{15}$$

$$= \frac{1}{3}$$

2. $\frac{\text{Cindy}}{3} : \frac{\text{Natalie}}{7}$ (Beginning)
 $9 : 9$ (End)

$$9 \text{ units} - 3 \text{ units} = 6 \text{ units}$$

$$6 \text{ units} = 72 \text{ buttons}$$

$$1 \text{ unit} = 72 \div 6$$

$$= 12 \text{ buttons}$$

$$18 \text{ units} = 18 \times 12$$

$$= 216 \text{ buttons}$$

The total number of buttons they had in the end was **216**.

3. $\frac{\text{Ducks}}{4 \times 2} : \frac{\text{Chickens}}{5 \times 2}$

$$= 8 : 10$$

$$\begin{array}{cc} \text{Roosters} & : & \text{Hens} \\ \frac{3}{3} & : & \frac{7}{7} \end{array}$$

$$\frac{\text{Ducks}}{8} : \frac{\text{Roosters}}{3} : \frac{\text{Hens}}{7}$$

$$7 \text{ units} = 42 \text{ animals}$$

$$1 \text{ unit} = 42 \div 7$$

$$= 6 \text{ animals}$$

$$8 \text{ units} = 8 \times 6$$

$$= 48 \text{ animals}$$

There are **48** ducks.

4. $\frac{\text{Adults}}{5} : \frac{\text{Children}}{4}$

$$\begin{array}{cc} \text{Boys} & : & \text{Girls} \\ \frac{3}{3} & : & \frac{1}{1} \end{array}$$

$$\frac{\text{Adults}}{5} : \frac{\text{Boys}}{3} : \frac{\text{Girls}}{1}$$

$$5 \text{ units} - 1 \text{ unit} = 4 \text{ units}$$

$$4 \text{ units} = 72 \text{ people}$$

$$1 \text{ unit} = 72 \div 4$$

$$= 18 \text{ people}$$

$$5 \text{ units} + 3 \text{ units} + 1 \text{ unit} = 9 \text{ units}$$

$$9 \text{ units} = 9 \times 18$$

$$= 162 \text{ people}$$

There were **162** people at the book fair.

5. $\frac{\text{Red}}{4 \times 2} : \frac{\text{Pink}}{3 \times 2} : \frac{\text{White}}{2 \times 3} : \frac{\text{White}}{5 \times 3}$

$$8 : 6 : 15$$

$$8 \text{ units} + 15 \text{ units} = 23 \text{ units}$$

$$23 \text{ units} = 92 \text{ beads}$$

$$1 \text{ unit} = 92 \div 23$$

$$= 4 \text{ beads}$$

$$6 \text{ units} = 6 \times 4$$

$$= 24 \text{ beads}$$

She has **24** pink beads.

6. After:

$$\frac{\text{Box B}}{4} : \frac{\text{Box A}}{3}$$

4 units + 3 units = 7 units

7 units = 238 postcards

1 unit = $238 \div 7$

= 34 postcards

3 units = 3×34

= 102 postcards

There were 102 postcards in Box A in the end.

$102 + 42 = 144$

There were **144** postcards in Box A at first.

7. Before:

$$\frac{\text{Pens}}{3} : \frac{\text{Pencils}}{5}$$

$\times 5 \left(\begin{array}{l} 3 : 5 \\ \hline = 15 : 25 \end{array} \right) \times 5$

After:

$$\frac{\text{Pens}}{5} : \frac{\text{Pencils}}{3}$$

$\times 3 \left(\begin{array}{l} 5 : 3 \\ \hline = 15 : 9 \end{array} \right) \times 3$

25 units - 9 units = 16 units

16 units = 48 items

1 unit = $48 \div 16$

= 3 items

15 units = 15×3

= 45 items

The shopkeeper had **45** pens.

8.
$$\frac{\text{Tin A}}{1} : \frac{\text{Tin B}}{3}$$

 $\times 3 \left(\begin{array}{l} 1 : 3 \\ \hline 3 : 9 \\ \hline + 2 \text{ units} \\ \hline 5 : 7 \end{array} \right) \times 3$
 $- 2 \text{ units}$

2 units = 14 biscuits

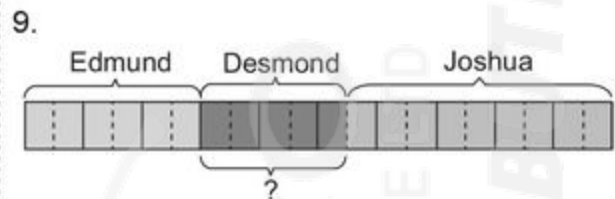
1 unit = $14 \div 2$

= 7 biscuits

3 units = 3×7

= 21 biscuits

There were **21** biscuits in Tin A at first.



9 units - 6 units = 3 units

3 units = \$900

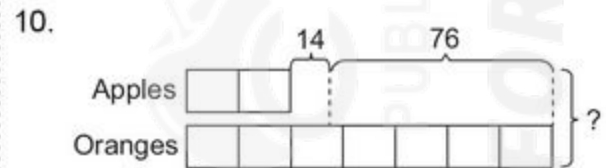
1 unit = $900 \div 3$

= \$300

5 units = $5 \times \$300$

= \$1500

Desmond donated **\$1500**.



5 units = $14 + 76$

= 90 fruits

1 unit = $90 \div 5$

= 18 fruits

9 units = 9×18

= 162 fruits

There were **162** fruits in the basket at first.

11. Total value of 1 set of 4 \$2 notes,
2 \$5 notes and 3 \$10 notes
 $= (4 \times \$2) + (2 \times \$5) + (3 \times \$10)$
 $= \$8 + \$10 + \$30$
 $= \$48$

Number of sets
 $= \$336 \div \48
 $= 7$

Number of \$5 notes
 $= 7 \times 2$
 $= 14$

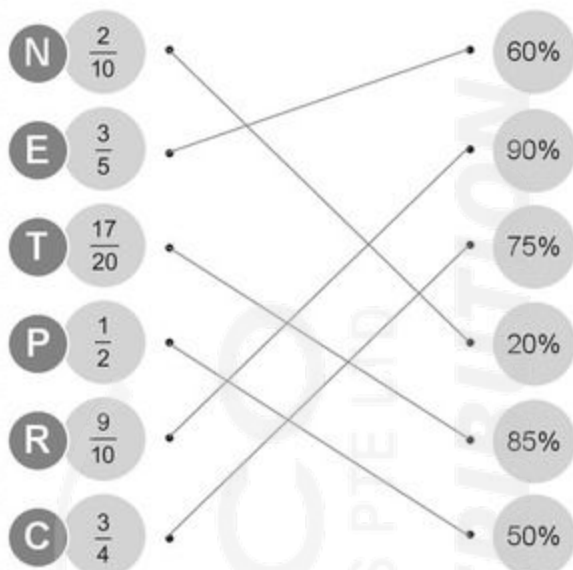
$14 \times \$5 = \70

The total value of the \$5 notes is **\$70**.

Unit 4 Percentage

Drills

Exercise 1



P 50% **E** 60% **R** 90% **C** 75% **E** 60% **N** 20% **T** 85%

Exercise 2

No.	Fraction	Decimal	Percentage
1.	$\frac{58}{100} = \frac{29}{50}$	0.58	58%
2.	$\frac{3}{5}$	0.6	60%
3.	$2\frac{35}{100} = 2\frac{7}{20}$	2.35	235%
4.	$\frac{76}{100} = \frac{19}{25}$	0.76	76%
5.	$\frac{7}{10}$	0.7	70%
6.	$8\frac{18}{100} = 8\frac{9}{50}$	8.18	818%

Exercise 3

- Percentage increase
 $= \frac{50}{2500} \times 100\%$
 $= 2\%$
- $\$25 - \$20 = \$5$
Percentage decrease
 $= \frac{5}{25} \times 100\%$
 $= 20\%$
- $\frac{60}{100} \times 15 = 9$
 $15 - 9 = 6$
6 fire disasters occurred in August.
- $1400 - 1200 = 200$
Percentage increase
 $= \frac{200}{1200} \times 100\%$
 $= 16\frac{2}{3}\%$
- $180 - 160 = 20$
Percentage decrease
 $= \frac{20}{180} \times 100\%$
 $= 11\frac{1}{9}\%$
- $120\% \rightarrow \$1980$
 $1\% \rightarrow \$\left(\frac{1980}{120}\right)$
 $20\% \rightarrow 20 \times \$\left(\frac{1980}{120}\right) = \330
His increase in salary was **\$330**.

Perform

Exercise 1

- (2)
 $40\% \rightarrow 248$
 $1\% \rightarrow \frac{248}{40}$
 $100\% \rightarrow 100 \times \frac{248}{40} = 620$
 $\frac{1}{4} \times 620 = \underline{155}$
- (1)
 $\frac{1}{2} \rightarrow 166$
 $\frac{2}{2} \rightarrow 2 \times 166 = 332$
 $\frac{30}{100} \times 332 = \underline{99.6}$
- (3)
 $100\% + 3\% = 103\%$
 $\frac{103}{100} \times \$500 = \underline{\$515}$
- (1)
Percentage of boys
 $= 100\% - 55\%$
 $= 45\%$
 $55\% - 45\% = 10\%$
 $\frac{10}{100} \times 40 = \underline{4}$
- (2)
 $100\% - 20\% = 80\%$
 $\frac{80}{100} \times \$1500 = \underline{\$1200}$
- (4)
 $\frac{625}{500} \times 100\% = \underline{125\%}$

7. (2)
 $100\% - 18\% = 82\%$

$$\frac{82}{100} \times 150 = \underline{123}$$

8. (3)
 $40 - 18 - 10 = 12$

$$\frac{12}{40} \times 100\% = \underline{30\%}$$

Exercise 2

1. $\$100 - \$89 = \$11$
 Percent discount

$$= \frac{11}{100} \times 100\%$$

$$= \underline{11\%}$$

2. $\$70 - \$42 = \$28$

$$\frac{28}{42} \times 100\% = 66\frac{2}{3}\%$$

Mary saved $66\frac{2}{3}\%$ more than Monica.

3. $120 - 84 = 36$
 Percentage decrease

$$= \frac{36}{120} \times 100\%$$

$$= \underline{30\%}$$

4. $54 \text{ kg} - 48 \text{ kg} = 6 \text{ kg}$
 Percentage decrease

$$= \frac{6}{54} \times 100\%$$

$$= \underline{11.11\% \text{ (correct of 2 d.p.)}}$$

5. $100\% - 20\% = 80\%$
 $80\% \rightarrow \$600$

$$1\% \rightarrow \$\left(\frac{600}{80}\right)$$

$$100\% \rightarrow 100 \times \$\left(\frac{600}{80}\right) = \$750$$

The original price of the dress was \$750.

$$\$750 - \$630 = \$120$$

Percentage discount Mrs Tan received

$$= \frac{120}{750} \times 100\%$$

$$= \underline{16\%}$$

6. Percentage painted dark blue
 $= 100\% - 80\% - 15\%$
 $= 5\%$

$$15\% \rightarrow 300 \text{ cm}^2$$

$$1\% \rightarrow 300 \text{ cm}^2 \div 15 = 20 \text{ cm}^2$$

$$5\% \rightarrow 5 \times 20 \text{ cm}^2 = 100 \text{ cm}^2$$

100 cm² of the wall is painted dark blue.

Achieve

Exercise 1

1. $100\% - 36\% = 64\%$
 $64\% - 36\% = 28\%$

$$28\% \rightarrow 15\,736 \text{ books}$$

$$1\% \rightarrow 15\,736 \div 28 = 562 \text{ books}$$

$$100\% \rightarrow 100 \times 562 = 56\,200 \text{ books}$$

The total number of books in the library is 56 200.

2. $100\% - 12\% = 88\%$
 $88\% - 12\% = 76\%$

$$76\% \rightarrow 38 \text{ beads}$$

$$1\% \rightarrow \left(\frac{38}{76}\right) \text{ beads}$$

$$100\% \rightarrow 100 \times \frac{38}{76} = 50 \text{ beads}$$

There are 50 beads in the bag.

3. Number of red apples left
 $= 250 - 40$
 $= 210$
- Number of green apples left
 $= 308 - 210$
 $= 98$
- Percentage of green apples left
 $= 100\% - 30\%$
 $= 70\%$
- 70% \rightarrow 98 apples
 1% \rightarrow $(\frac{98}{70})$ apples
 100% \rightarrow $100 \times \frac{98}{70} = 140$ apples
- He had **140** green apples at first.

4. $100\% - 55\% = 45\%$
- 45% \rightarrow 360 marbles
 1% \rightarrow $360 \div 45 = 8$ marbles
 100% \rightarrow $100 \times 8 = 800$ marbles
- He had **800** marbles in the end.

Percentage of yellow marbles
 $= \frac{240}{800} \times 100\%$
 $= 30\%$

30% of his marbles were yellow in the end.

5. Percentage of monthly salary that she saves
 $= (100\% - 20\%)$ of $(100\% - 40\%)$
 $= 80\%$ of 60%
- $= \frac{80}{100} \times 60\%$
 $= 48\%$
- 48% \rightarrow \$1200
 1% \rightarrow $\$1200 \div 48 = \25
 100% \rightarrow $100 \times \$25 = \2500

Her monthly salary is **\$2500**.

6. At first:

$$\begin{array}{l} \text{White} : \text{Black} \\ 40\% : 60\% \\ = 2 : 3 \end{array}$$

After:

$$\begin{array}{l} \text{White} : \text{Black} \\ 75\% : 25\% \\ = 3 : 1 \\ \times 3 \left(\begin{array}{l} 3 : 1 \\ \downarrow \quad \downarrow \\ 9 : 3 \end{array} \right) \times 3 \\ = 9 : 3 \end{array}$$

$$3 \text{ units} + 2 \text{ units} = 5 \text{ units}$$

$$\begin{array}{l} 5 \text{ units} = 240 \text{ buttons} \\ 1 \text{ unit} = 240 \div 5 \\ = 48 \text{ buttons} \end{array}$$

$$\begin{array}{l} 9 \text{ units} - 2 \text{ units} = 7 \text{ units} \\ 7 \text{ units} = 7 \times 48 \\ = 336 \text{ buttons} \end{array}$$

He put **336** white buttons into the box.

7. $100\% + 25\% = 125\%$
 $125\% \rightarrow$ 280 T-shirts
- 1% \rightarrow $(\frac{280}{125})$ T-shirts
 $100\% \rightarrow$ $100 \times \frac{280}{125} = 224$ T-shirts

There were **224** T-shirts in Box B at first.

$$280 - 224 = 56$$

$$35\% \rightarrow 56 \text{ T-shirts}$$

$$1\% \rightarrow (\frac{56}{35}) \text{ T-shirts}$$

$$100\% \rightarrow 100 \times \frac{56}{35} = 160 \text{ T-shirts}$$

There are **160** T-shirts in Box A at first.

8. Percentage of purple beads
 $= 100\% - 45\%$
 $= 55\%$
- $55\% - 45\% = 10\%$
- $10\% \rightarrow 60 - 40 = 20$ beads
 $1\% \rightarrow 20 \div 10 = 2$ beads
 $55\% \rightarrow 55 \times 2 = 110$ beads

She had **110** purple beads.

9. Mass of red apples at first

$$= \frac{20}{100} \times 70 \text{ kg}$$

$$= 14 \text{ kg}$$

Mass of green apples at first
 $= 70 \text{ kg} - 14 \text{ kg}$
 $= 56 \text{ kg}$

$$100\% - 30\% = 70\%$$

$$70\% \rightarrow 56 \text{ kg}$$

$$1\% \rightarrow \left(\frac{56}{70}\right) \text{ kg}$$

$$30\% \rightarrow 30 \times \frac{56}{70} = 24 \text{ kg}$$

He had **24 kg** of red apples in the end.

$$24 \text{ kg} - 14 \text{ kg} = 10 \text{ kg}$$

He bought **10 kg** of red apples.

10. $100\% - 20\% = 80\%$
 Discounted price of scarf

$$= \frac{80}{100} \times \$25$$

$$= \$20$$

Normal price : Discounted price

$$= \frac{40\%}{2} : \frac{60\%}{3}$$

Total cost of 1 set of 2 scarves (normal price) and 3 scarves (discounted price)
 $= 2 \times \$25 + 3 \times \20
 $= \$110$

Number of sets
 $= \$1980 \div \110
 $= 18$

Total number of scarves sold
 $= 5 \times 18$
 $= 90$

She sold **90** scarves altogether.

11. $100\% - 20\% = 80\%$
 $80\% - 20\% = 60\%$

$$60\% \rightarrow 180 \text{ kg}$$

$$1\% \rightarrow 180 \text{ kg} \div 60 = 3 \text{ kg}$$

$$100\% \rightarrow 100 \times 3 \text{ kg} = 300 \text{ kg}$$

Mass of beans in red-bean bag in the end

$$= \frac{30}{100} \times 300 \text{ kg}$$

$$= 90 \text{ kg}$$

There were **90 kg** of beans in the red-bean bag in the end.

12. Pens : Pencils : Rulers
 25% : $\frac{2}{75}$: $\frac{5}{75}$

$$5 \text{ units} - 2 \text{ units} = 3 \text{ units}$$

$$3 \text{ units} = 45 \text{ items}$$

$$1 \text{ unit} = 45 \div 3$$

$$= 15 \text{ items}$$

$$7 \text{ units} = 7 \times 15$$

$$= 105 \text{ items}$$

There were **105** pencils and rulers altogether.

$$75\% \rightarrow 105 \text{ items}$$

$$1\% \rightarrow \left(\frac{105}{75}\right) \text{ items}$$

$$100\% \rightarrow 100 \times \frac{105}{75} = 140 \text{ items}$$

There were **140** stationery items in all in the box.

Drills

Exercise 1

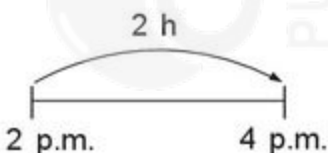
- Distance
 $= 50 \text{ m/min} \times 15 \text{ min}$
 $= 750 \text{ m}$
- Time taken
 $= 137.5 \text{ km} \div 55 \text{ km/h}$
 $= 2.5 \text{ h}$
- $1 \text{ h } 20 \text{ min} = 1 \frac{20}{60} \text{ h}$
 $= 1 \frac{1}{3} \text{ h}$

Average speed

$$= 120 \text{ km} \div 1 \frac{1}{3} \text{ h}$$

$$= 90 \text{ km/h}$$

- Average speed
 $= 1350 \text{ m} \div 9 \text{ min}$
 $= 150 \text{ m/min}$
- Time taken
 $= 900 \text{ m} \div 45 \text{ m/min}$
 $= 20 \text{ min}$

- 

Average speed

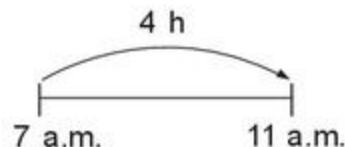
$$= 4 \text{ km} \div 2 \text{ h}$$

$$= 2 \text{ km/h}$$

Perform

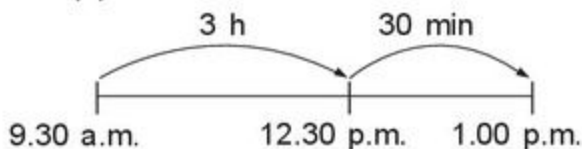
Exercise 1

- (3)
 Average speed
 $= 240 \text{ cm} \div 12 \text{ s}$
 $= 20 \text{ cm/s}$
- (1)
 Distance
 $= 650 \text{ km/h} \times 6 \text{ h}$
 $= 3900 \text{ km}$
- (2)
 Time taken
 $= 605 \text{ km} \div 110 \text{ km/h}$
 $= 5.5 \text{ h}$
- (4)
 $3 \times 450 \text{ m} = 1350 \text{ m}$
 Average speed
 $= 1350 \text{ m} \div 12 \text{ min}$
 $= 112.5 \text{ m/min}$
- (3)
 $45 \text{ min} = \frac{45}{60} \text{ h} = \frac{3}{4} \text{ h}$
 Distance
 $= 72 \text{ km/h} \times \frac{3}{4} \text{ h}$
 $= 54 \text{ km}$
- (2)
 Time taken
 $= 300 \text{ km} \div 75 \text{ km/h}$
 $= 4 \text{ h}$



It reached Station B at 11 a.m.

7. (4)



$$3 \text{ h } 30 \text{ min} = 3\frac{1}{2} \text{ h}$$

$$\begin{aligned} \text{Distance} &= 80 \text{ km/h} \times 3\frac{1}{2} \text{ h} \\ &= \underline{280 \text{ km}} \end{aligned}$$

Exercise 2

1. Speed

$$\begin{aligned} &= 42 \text{ km} \div 1\frac{1}{2} \text{ h} \\ &= 28 \text{ km/h} \end{aligned}$$

$$28 \text{ km/h} - 4 \text{ km/h} = 24 \text{ km/h}$$

$$\begin{aligned} \text{Distance} &= 24 \text{ km/h} \times 2\frac{3}{4} \text{ h} \\ &= 66 \text{ km} \end{aligned}$$

She can travel **66 km** in $2\frac{3}{4}$ h.

2. Distance

$$\begin{aligned} &= 45 \text{ km/h} \times 4 \text{ h} \\ &= 180 \text{ km} \end{aligned}$$

$$4 \text{ h} + \frac{1}{2} \text{ h} = 4\frac{1}{2} \text{ h}$$

Jerry's average speed

$$\begin{aligned} &= 180 \text{ km} \div 4\frac{1}{2} \text{ h} \\ &= 40 \text{ km/h} \end{aligned}$$

3. Distance

$$\begin{aligned} &= 60 \text{ km/h} \times 5 \text{ h} \\ &= 300 \text{ km} \end{aligned}$$

Jimmy's average speed

$$\begin{aligned} &= 300 \text{ km} \div 7\frac{1}{2} \text{ h} \\ &= 40 \text{ km/h} \end{aligned}$$

4. Distance (1st part)

$$\begin{aligned} &= 10 \text{ km/h} \times \frac{3}{4} \text{ h} \\ &= 7.5 \text{ km} \end{aligned}$$

Distance (2nd part)

$$\begin{aligned} &= 6 \text{ km/h} \times \frac{1}{2} \text{ h} \\ &= 3 \text{ km} \end{aligned}$$

Total distance covered

$$\begin{aligned} &= 7.5 \text{ km} + 3 \text{ km} \\ &= \underline{10.5 \text{ km}} \end{aligned}$$

5. Distance travelled by Thomas in $1\frac{1}{2}$ h

$$\begin{aligned} &= 50 \text{ km/h} \times 1\frac{1}{2} \text{ h} \\ &= 75 \text{ km} \end{aligned}$$

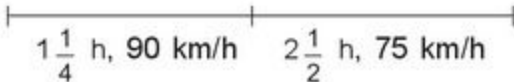
Distance travelled by Brian in $1\frac{1}{2}$ h

$$\begin{aligned} &= 65 \text{ km/h} \times 1\frac{1}{2} \text{ h} \\ &= 97.5 \text{ km} \end{aligned}$$

$$97.5 \text{ km} - 75 \text{ km} = 22.5 \text{ km}$$

Their distance apart after $1\frac{1}{2}$ h was **22.5 km**.

Exercise 3

1. 

Distance travelled (1st part)

$$= 90 \text{ km/h} \times 1\frac{1}{4} \text{ h}$$

$$= 112.5 \text{ km}$$

Distance travelled (2nd part)

$$= 75 \text{ km/h} \times 2\frac{1}{2} \text{ h}$$

$$= 187.5 \text{ km}$$

Total distance travelled

$$= 112.5 \text{ km} + 187.5 \text{ km}$$

$$= 300 \text{ km}$$

Total time taken

$$= 1\frac{1}{4} \text{ h} + 2\frac{1}{2} \text{ h}$$

$$= 1\frac{1}{4} \text{ h} + 2\frac{2}{4} \text{ h}$$

$$= 3\frac{3}{4} \text{ h}$$

Average speed for whole journey

$$= 300 \text{ km} \div 3\frac{3}{4} \text{ h}$$

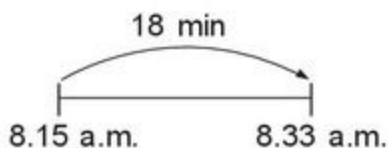
$$= 80 \text{ km/h}$$

2. Time taken

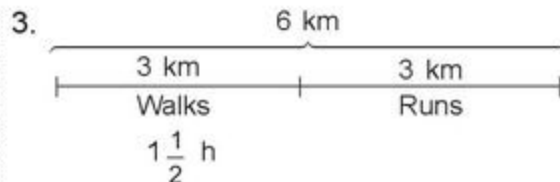
$$= 13.5 \text{ km} \div 45 \text{ km/h}$$

$$= 0.3 \text{ h}$$

$$= 18 \text{ min}$$



She reached her office at 8.33 a.m.



$$6 \text{ km} \div 2 = 3 \text{ km}$$

Walking speed

$$= 3 \text{ km} \div 1\frac{1}{2} \text{ h}$$

$$= 2 \text{ km/h}$$

Running speed

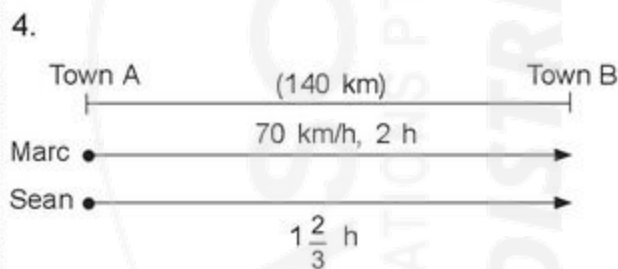
$$= 2 \text{ km/h} + 4 \text{ km/h}$$

$$= 6 \text{ km/h}$$

Time he spends running

$$= 3 \text{ km} \div 6 \text{ km/h}$$

$$= \frac{1}{2} \text{ h}$$



Distance between Town A and Town B

$$= 70 \text{ km/h} \times 2 \text{ h}$$

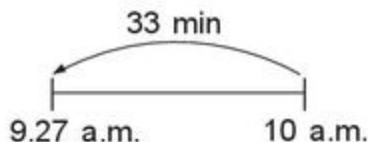
$$= 140 \text{ km}$$

Sean's average speed

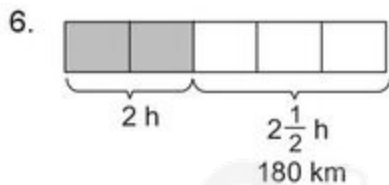
$$= 140 \text{ km} \div 1\frac{2}{3} \text{ h}$$

$$= 84 \text{ km/h}$$

5. Time taken
 $= 2.2 \text{ km} \div 4 \text{ km/h}$
 $= 0.55 \text{ h}$
 $= 33 \text{ min}$



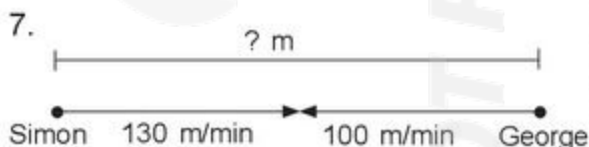
He left the library at 9.27 a.m.



$$\begin{aligned} 3 \text{ units} &= 180 \text{ km} \\ 1 \text{ unit} &= 180 \text{ km} \div 3 \\ &= 60 \text{ km} \\ 5 \text{ units} &= 5 \times 60 \text{ km} \\ &= 300 \text{ km} \end{aligned}$$

$$\begin{aligned} \text{Total time taken} \\ &= 2 \text{ h} + 2\frac{1}{2} \text{ h} \\ &= 4\frac{1}{2} \text{ h} \end{aligned}$$

$$\begin{aligned} \text{Average speed for whole journey} \\ &= 300 \text{ km} \div 4\frac{1}{2} \text{ h} \\ &= 66\frac{2}{3} \text{ km/h} \end{aligned}$$



$$130 \text{ m} + 100 \text{ m} = 230 \text{ m}$$

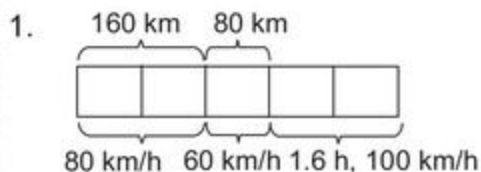
In 1 min, both of them covered a distance of 230 m.

$$\begin{aligned} 1 \text{ min} &\longrightarrow 230 \text{ m} \\ 4 \text{ min} &\longrightarrow 4 \times 230 \text{ m} = 920 \text{ m} \end{aligned}$$

The distance of the track was 920 m.

Achieve

Exercise 1



$$\begin{aligned} \text{Distance (last part)} \\ &= 100 \text{ km/h} \times 1.6 \text{ h} \\ &= 160 \text{ km} \end{aligned}$$

$$\begin{aligned} 2 \text{ units} &= 160 \text{ km} \\ 1 \text{ unit} &= 160 \div 2 \\ &= 80 \text{ km} \end{aligned}$$

$$\begin{aligned} \text{Time taken (1st part)} \\ &= 160 \text{ km} \div 80 \text{ km/h} \\ &= 2 \text{ h} \end{aligned}$$

$$\begin{aligned} \text{Time taken (2nd part)} \\ &= 80 \text{ km} \div 60 \text{ km/h} \\ &= 1\frac{1}{3} \text{ h} \end{aligned}$$

$$\begin{aligned} \text{Total time taken} \\ &= 2 \text{ h} + 1\frac{1}{3} \text{ h} + 1.6 \text{ h} \\ &= 2 \text{ h} + 1 \text{ h } 20 \text{ min} + 1 \text{ h } 36 \text{ min} \\ &= 4 \text{ h } 56 \text{ min} \end{aligned}$$

The total time Janet took for the whole journey was 4 h 56 min.

2. 60 km/h,
1 h 20 min 160 km



Distance (1st part)

$$= 60 \text{ km/h} \times 1\frac{1}{3} \text{ h}$$

$$= 80 \text{ km}$$

1 unit = 80 km

$$2 \text{ units} = 2 \times 80 \text{ km}$$

$$= 160 \text{ km}$$

$$3 \text{ h} - 1\frac{1}{3} \text{ h} = 1\frac{2}{3} \text{ h}$$

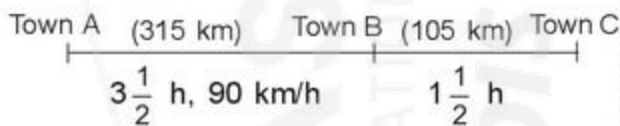
Average speed (2nd part)

$$= 160 \text{ km} \div 1\frac{2}{3} \text{ h}$$

$$= 96 \text{ km/h}$$

He must travel at an average speed of **96 km/h** for the rest of the journey.

3.



Distance between Town A and Town B

$$= 90 \text{ km/h} \times 3\frac{1}{2} \text{ h}$$

$$= 315 \text{ km}$$

Total time taken

$$= 3\frac{1}{2} \text{ h} + 1\frac{1}{2} \text{ h}$$

$$= 5 \text{ h}$$

Total distance between Town A and Town C

$$= 84 \text{ km/h} \times 5 \text{ h}$$

$$= 420 \text{ km}$$

Distance between Town B and Town C

$$= 420 \text{ km} - 315 \text{ km}$$

$$= 105 \text{ km}$$

Speed (Town B to Town C)

$$= 105 \text{ km/h} \div 1\frac{1}{2} \text{ h}$$

$$= 70 \text{ km/h}$$

His speed was **70 km/h** when he was travelling from Town B to Town C.

4. 1 min \longrightarrow 20 m
45 min \longrightarrow $45 \times 20 \text{ m} = 900 \text{ m}$

Marc had jogged 900 m more than Ben when Marc completed the journey.

$$1 - \frac{7}{8} = \frac{1}{8}$$

$$\frac{1}{8} \longrightarrow 900 \text{ m}$$

$$\frac{8}{8} \longrightarrow 8 \times 900 \text{ m} = 7200 \text{ m}$$

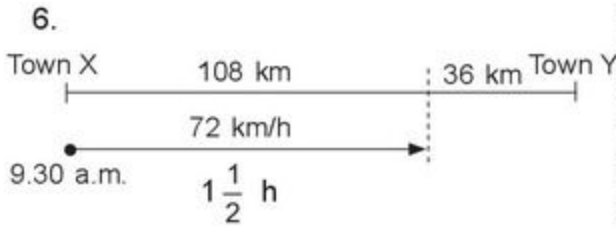
The park is **7200 m** from their home.

5. Difference between their speed
 $= 6 \text{ m/s} - 4 \text{ m/s}$
 $= 2 \text{ m/s}$

Time taken for Tim to catch up with Jane
 $= 80 \text{ m} \div 2 \text{ m/s}$
 $= 40 \text{ s}$

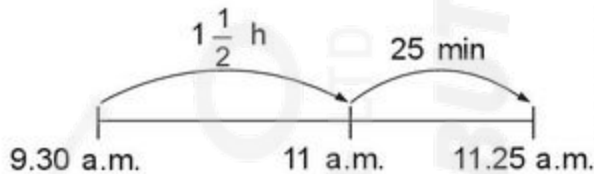
Distance Tim cycled when he caught up with Jane
 $= 6 \text{ m/s} \times 40 \text{ s}$
 $= 240 \text{ m}$

Tim should have cycled **240 m** when he caught up with Jane.



Distance travelled (1st part)
 $= 72 \text{ km/h} \times 1\frac{1}{2} \text{ h}$
 $= 108 \text{ km}$

$\frac{3}{4} \rightarrow 108 \text{ km}$
 $\frac{1}{4} \rightarrow 108 \text{ km} \div 3 = 36 \text{ km}$



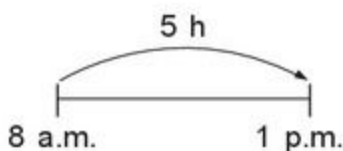
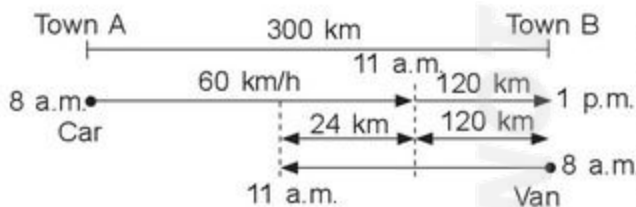
$25 \text{ min} = \frac{25}{60} \text{ h}$
 $= \frac{5}{12} \text{ h}$

Average speed for remaining journey

$= 36 \text{ km} \div \frac{5}{12} \text{ h}$
 $= 86\frac{2}{5} \text{ km/h}$

She must drive at a speed of $86\frac{2}{5} \text{ km/h}$ to reach Town Y at 11.25 a.m.

7.



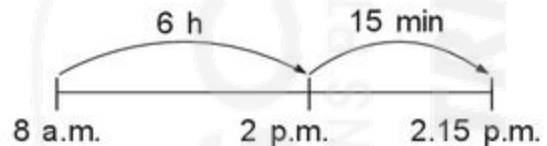
Distance between Town A and Town B
 $= 60 \text{ km/h} \times 5 \text{ h}$
 $= 300 \text{ km}$

Distance travelled by car from 11 a.m. to 1 p.m.
 $= 60 \text{ km/h} \times 2 \text{ h}$
 $= 120 \text{ km}$

$120 \text{ km} + 24 \text{ km} = 144 \text{ km}$

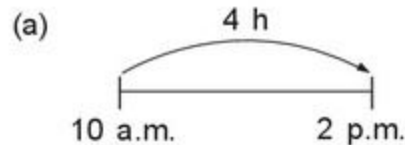
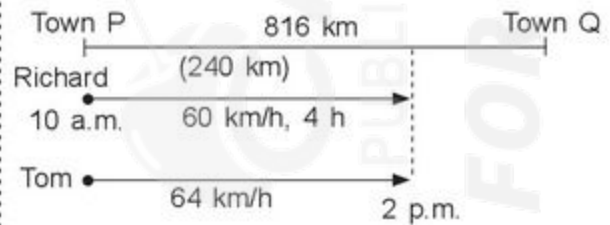
Average speed of van
 $= 144 \text{ km} \div 3 \text{ h}$
 $= 48 \text{ km/h}$

Time taken by van for whole journey
 $= 300 \text{ km} \div 48 \text{ km/h}$
 $= 6\frac{1}{4} \text{ h}$
 $= 6 \text{ h } 15 \text{ min}$



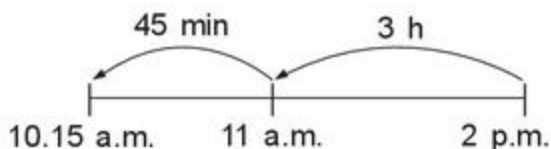
The van arrived at Town A at 2.15 p.m.

8.



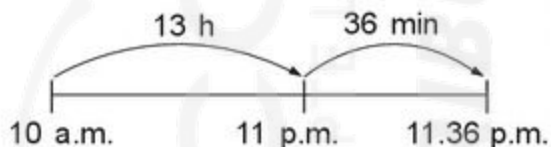
Distance travelled when they passed each other
 $= 60 \text{ km/h} \times 4 \text{ h}$
 $= 240 \text{ km}$

$$\begin{aligned}
 &\text{Time taken by Tom} \\
 &= 240 \text{ km} \div 64 \text{ km/h} \\
 &= 3.75 \text{ h} \\
 &= 3 \text{ h } 45 \text{ min}
 \end{aligned}$$

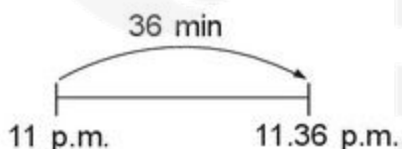
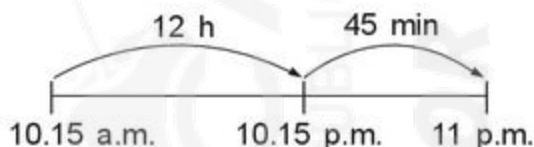


Tom left Town P at 10.15 a.m.

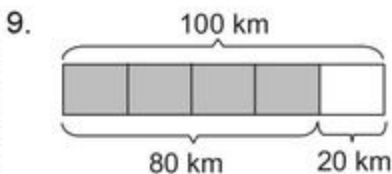
- (b) Time taken by Richard for the whole journey
 $= 816 \text{ km} \div 60 \text{ km/h}$
 $= 13.6 \text{ h}$
 $= 13 \text{ h } 36 \text{ min}$



$$\begin{aligned}
 &\text{Time taken by Tom for the whole} \\
 &\text{journey} \\
 &= 816 \text{ km} \div 64 \text{ km/h} \\
 &= 12.75 \text{ h} \\
 &= 12 \text{ h } 45 \text{ min}
 \end{aligned}$$



Tom had arrived for 36 min when Richard reached Town Q.



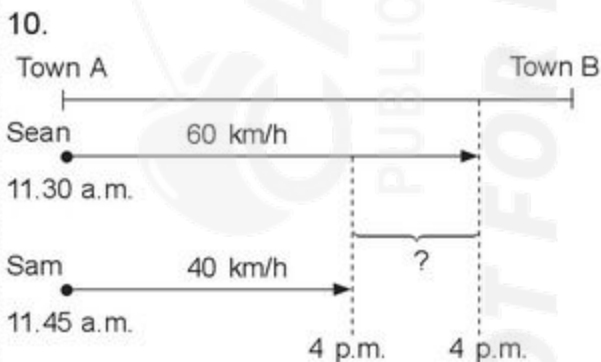
$$\begin{aligned}
 4 \text{ units} &= 80 \text{ km} \\
 1 \text{ unit} &= 80 \text{ km} \div 4 \\
 &= 20 \text{ km} \\
 5 \text{ units} &= 5 \times 20 \text{ km} \\
 &= 100 \text{ km}
 \end{aligned}$$

$$\begin{aligned}
 &\text{Time taken (Travelling at } 75 \text{ km/h)} \\
 &= 100 \text{ km} \div 75 \text{ km/h} \\
 &= 1 \frac{1}{3} \text{ h}
 \end{aligned}$$

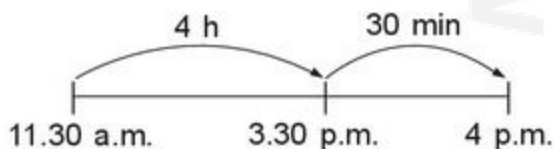
$$\begin{aligned}
 &\text{Time taken (Travelling at } 80 \text{ km/h)} \\
 &= 100 \text{ km} \div 80 \text{ km/h} \\
 &= 1 \frac{1}{4} \text{ h}
 \end{aligned}$$

$$\begin{aligned}
 1 \frac{1}{3} \text{ h} - 1 \frac{1}{4} \text{ h} &= \frac{1}{12} \text{ h} \\
 &= 5 \text{ min}
 \end{aligned}$$

He would have saved 5 min.



Sean:

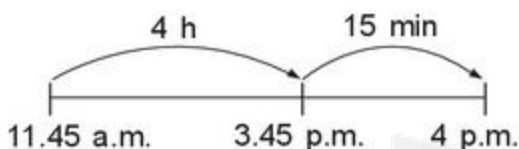


$$4 \text{ h} + 30 \text{ min} = 4 \frac{1}{2} \text{ h}$$

Distance travelled by Sean

$$= 60 \text{ km/h} \times 4\frac{1}{2} \text{ h}$$
$$= 270 \text{ km}$$

Sam:



$$4 \text{ h} + 15 \text{ min} = 4\frac{1}{4} \text{ h}$$

Distance travelled by Sam

$$= 40 \text{ km/h} \times 4\frac{1}{4} \text{ h}$$
$$= 170 \text{ km}$$

$$270 \text{ km} - 170 \text{ km} = 100 \text{ km}$$

The distance between Sean and Sam at 4 p.m. was 100 km.

Unit 6 Circles

Drills

Exercise 1

Circle	Radius	Diameter	Circumference	Area
A	6 cm	12 cm	37.68 cm	113.04 cm ²
B	12 cm	24 cm	75.36 cm	452.16 cm ²
C	10 cm	20 cm	62.8 cm	314 cm ²
D	7 cm	14 cm	43.96 cm	153.86 cm ²

1. Circle A
2. Circle B
3. Circle A
4. Circle B

Exercise 2

1. Circumference = $\pi \times 60$
 $= 3.14 \times 60$
 $= 188.4 \text{ cm}$
2. Circumference = $\frac{22}{7} \times 56$
 $= 176 \text{ cm}$
3. Circumference = 3.14×36
 $= 113.04 \text{ cm}$
4. Circumference = $\frac{22}{7} \times 75$
 $= 235\frac{5}{7} \text{ cm}$
5. Diameter = 18 cm
Circumference = 3.14×18
 $= 56.52 \text{ cm}$

6. Diameter = 24 cm
 Circumference = $\frac{22}{7} \times 24$
 $= 75\frac{3}{7}$ cm

7. Diameter = 30 cm
 Circumference = 3.14×30
 $= 94.2$ cm

8. Diameter = 19 cm
 Circumference = $\frac{22}{7} \times 19$
 $= 59\frac{5}{7}$ cm

Exercise 3

1. Area of circle = $\pi \times 8 \times 8$
 $= 3.14 \times 64$
 $= 200.96$ cm²

2. Area of circle = $\frac{22}{7} \times 5 \times 5$
 $= \frac{22}{7} \times 25$
 $= 78\frac{4}{7}$ cm²

3. Area of circle = $3.14 \times 6 \times 6$
 $= 3.14 \times 36$
 $= 113.04$ cm²

4. Area of circle
 $= \frac{22}{7} \times 12\frac{1}{2} \times 12\frac{1}{2}$
 $= \frac{22}{7} \times 156\frac{1}{4}$
 $= 491\frac{1}{14}$ cm²

Exercise 4

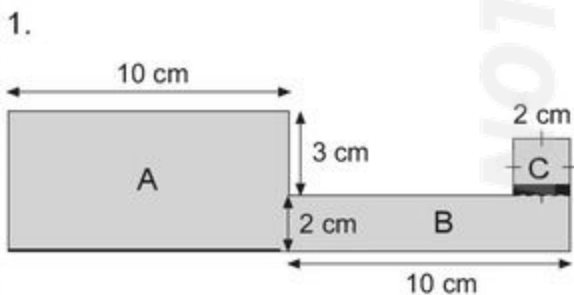
1. Area of semicircle
 $= \frac{1}{2} \times 3.14 \times 8 \times 8$
 $= \frac{1}{2} \times 200.96$
 $= 100.48$ cm²

2. Area of semicircle
 $= \frac{1}{2} \times \frac{22}{7} \times 3 \times 3$
 $= \frac{1}{2} \times 28\frac{2}{7}$
 $= \frac{1}{2} \times \frac{198}{7}$
 $= 14\frac{1}{7}$ cm²

3. Area of quarter circle
 $= \frac{1}{4} \times 3.14 \times 10 \times 10$
 $= \frac{1}{4} \times 314$
 $= 78.5$ cm²

4. Area of quarter circle
 $= \frac{1}{4} \times \frac{22}{7} \times 7 \times 7$
 $= \frac{1}{4} \times 154$
 $= 38.5$ cm²

Exercise 5



$$\begin{aligned} \text{Area of Rectangle A} \\ &= 10 \times 5 \\ &= 50 \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} \text{Area of Rectangle B} \\ &= 10 \times 2 \\ &= 20 \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} \text{Area of Square C} \\ &= 2 \times 2 \\ &= 4 \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} \text{Area of figure} \\ &= 50 + 20 + 4 \\ &= 74 \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} 2. \text{ Area of triangle} \\ &= \frac{1}{2} \times 42 \times 42 \\ &= \frac{1}{2} \times 1764 \\ &= 882 \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} \text{Area of circle} \\ &= \frac{22}{7} \times 7 \times 7 \\ &= 154 \text{ cm}^2 \end{aligned}$$

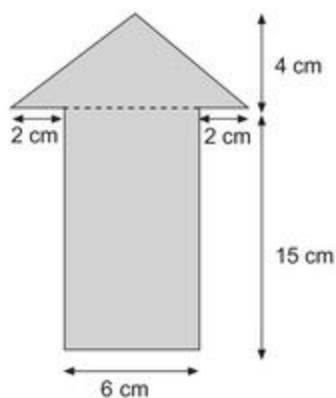
$$\begin{aligned} \text{Shaded area of figure} \\ &= 882 - 154 \\ &= 728 \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} 3. \text{ Area of semicircle} \\ &= \frac{1}{2} \times 3.14 \times 5 \times 5 \\ &= \frac{1}{2} \times 78.5 \\ &= 39.25 \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} \text{Area of triangle} \\ &= \frac{1}{2} \times 10 \times 8 \\ &= 40 \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} \text{Area of figure} \\ &= 39.25 + 40 \\ &= 79.25 \text{ cm}^2 \end{aligned}$$

4.



$$\begin{aligned} \text{Area of triangle} \\ &= \frac{1}{2} \times (2 + 6 + 2) \times 4 \\ &= \frac{1}{2} \times 10 \times 4 \\ &= \frac{1}{2} \times 40 \\ &= 20 \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} \text{Area of rectangle} \\ &= 15 \times 6 \\ &= 90 \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} \text{Area of arrow} \\ &= 20 + 90 \\ &= 110 \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} 5. \text{ Area of rectangle} \\ &= 18 \times 9 \\ &= 162 \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} \text{Area of triangle} \\ &= \frac{1}{2} \times 9 \times 9 \\ &= \frac{1}{2} \times 81 \\ &= 40.5 \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} \text{Area of shaded part} \\ &= 162 - 40.5 \\ &= 121.5 \text{ cm}^2 \end{aligned}$$

6. Curved part of small semicircle

$$= \frac{1}{2} \times 3.14 \times 14$$

$$= \frac{1}{2} \times 43.96$$

$$= 21.98 \text{ cm}$$

Curved part of big semicircle

$$= \frac{1}{2} \times 3.14 \times 20$$

$$= \frac{1}{2} \times 62.8$$

$$= 31.4 \text{ cm}$$

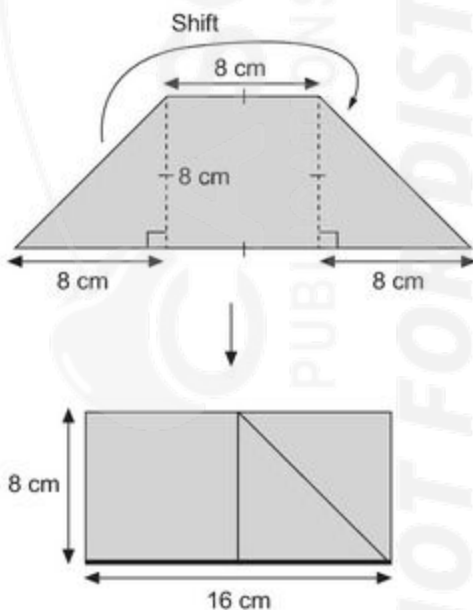
Perimeter of figure

$$= 21.98 + 31.4 + 6$$

$$= 59.38 \text{ cm}$$

7. Perimeter of figure
- $$= 2 + 6 + 6 + 6 + 2 + 16 + 6 + 6$$
- $$+ 4 + 10$$
- $$= 64 \text{ cm}$$

8.



Area of figure

$$= 16 \times 8$$

$$= 128 \text{ cm}^2$$

Perform

Exercise 1

1. (3)

$$\text{Diameter} = 2 \times 120 \text{ cm}$$

$$= 240 \text{ cm}$$

$$\text{Circumference} = 3.14 \times 240$$

$$= \underline{753.6 \text{ cm}}$$

2. (4)

Area of semicircle

$$= \frac{1}{2} \times 3.14 \times 8 \times 8$$

$$= \frac{1}{2} \times 200.96$$

$$= 100.48 \text{ cm}^2$$

Area of triangle

$$= \frac{1}{2} \times 16 \times 4$$

$$= 32 \text{ cm}^2$$

Area of figure

$$= 100.48 + 32$$

$$= \underline{132.48 \text{ cm}^2}$$

3. (2)

Curved part of small semicircle

$$= \frac{1}{2} \times \pi \times 10$$

$$= 5\pi \text{ cm}$$

Curved part of big semicircle

$$= \frac{1}{2} \times \pi \times 14$$

$$= 7\pi \text{ cm}$$

Perimeter of shaded figure

$$= 5\pi + 7\pi + 2 + 2$$

$$= \underline{(12\pi + 4) \text{ cm}}$$

$$\begin{aligned}
 3. \text{ Circumference of each circle} \\
 &= 36\pi \div 2 \\
 &= 18\pi \text{ cm}
 \end{aligned}$$

$$\begin{aligned}
 \text{Diameter of each circle} &= 18 \text{ cm} \\
 \text{Radius of each circle} &= 9 \text{ cm}
 \end{aligned}$$

$$\begin{aligned}
 \text{Area of one circle} \\
 &= \pi \times 9 \times 9 \\
 &= 81\pi \text{ cm}^2
 \end{aligned}$$

$$\begin{aligned}
 4. \text{ Area of triangle} \\
 &= \frac{1}{2} \times 6 \times 8 \\
 &= 24 \text{ cm}^2
 \end{aligned}$$

$$\begin{aligned}
 \text{Area of semicircle} \\
 &= \frac{1}{2} \times 3.14 \times 5 \times 5 \\
 &= 39.25 \text{ cm}^2
 \end{aligned}$$

$$\begin{aligned}
 \text{Shaded area of figure} \\
 &= 39.25 - 24 \\
 &= 15.25 \text{ cm}^2
 \end{aligned}$$

Exercise 3

$$\begin{aligned}
 1. \text{ Curved part of semicircle} \\
 &= \frac{1}{2} \times 3.14 \times 7 \\
 &= 10.99 \text{ m}
 \end{aligned}$$

$$\begin{aligned}
 \text{Perimeter of figure} \\
 &= 10.99 \text{ m} + 7 \text{ m} \\
 &= 17.99 \text{ m}
 \end{aligned}$$

$$\begin{aligned}
 2. \text{ Area of big semicircle} \\
 &= \frac{1}{2} \times \frac{22}{7} \times 7 \times 7 \\
 &= 77 \text{ cm}^2
 \end{aligned}$$

$$\begin{aligned}
 \text{Area of small semicircle} \\
 &= \frac{1}{2} \times \frac{22}{7} \times 3.5 \times 3.5 \\
 &= 19.25 \text{ cm}^2
 \end{aligned}$$

$$\begin{aligned}
 \text{Area of shaded part} \\
 &= 77 - 19.25 \\
 &= 57.75 \text{ cm}^2
 \end{aligned}$$

$$\begin{aligned}
 3. \text{ Curved part of each semicircle} \\
 &= \frac{1}{2} \times \pi \times 8 \\
 &= 4\pi \text{ cm}
 \end{aligned}$$

$$\begin{aligned}
 \text{Length of wire} \\
 &= 3 \times 4\pi \\
 &= 12\pi \text{ cm}
 \end{aligned}$$

$$\begin{aligned}
 4. \text{ Area of big semicircle} \\
 &= \frac{1}{2} \times \pi \times 6 \times 6 \\
 &= 18\pi \text{ cm}^2
 \end{aligned}$$

$$\begin{aligned}
 \text{Area of small semicircle} \\
 &= \frac{1}{2} \times \pi \times 3 \times 3 \\
 &= 4\frac{1}{2}\pi \text{ cm}^2
 \end{aligned}$$

$$\begin{aligned}
 \text{Area of shaded part} \\
 &= 18\pi - 4\frac{1}{2}\pi \\
 &= 13\frac{1}{2}\pi \text{ cm}^2
 \end{aligned}$$

$$\begin{aligned}
 5. \text{ Area of triangle} \\
 &= \frac{1}{2} \times 12 \times 18 \\
 &= 108 \text{ cm}^2
 \end{aligned}$$

$$\begin{aligned}
 \text{Area of rectangle} \\
 &= 45 \times 18 \\
 &= 810 \text{ cm}^2
 \end{aligned}$$

$$\begin{aligned}
 \text{Area of semicircle} \\
 &= \frac{1}{2} \times 3.14 \times 9 \times 9 \\
 &= 127.17 \text{ cm}^2
 \end{aligned}$$

$$\begin{aligned}
 \text{Area of figure} \\
 &= 108 + 810 + 127.17 \\
 &= 1045.17 \text{ cm}^2
 \end{aligned}$$

6. Length of square
 $= 2 \times 40 \text{ cm}$
 $= 80 \text{ cm}$

Area of square
 $= 80 \times 80$
 $= 6400 \text{ cm}^2$

Area of circle
 $= 3.14 \times 40 \times 40$
 $= 5024 \text{ cm}^2$

Area of shaded region
 $= 6400 - 5024$
 $= 1376 \text{ cm}^2$

7. Circumference of circle
 $= 3.14 \times 15$
 $= 47.1 \text{ cm}$

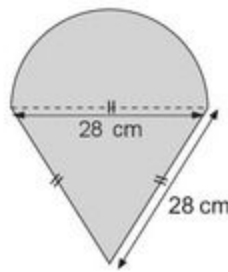
Perimeter of figure
 $= 47.1 + 25 + 25$
 $= 97.1 \text{ cm}$

8. Curved part of quarter circle
 $= \frac{1}{4} \times \pi \times 24$
 $= 6\pi \text{ cm}$

Curved part of semicircle
 $= \frac{1}{2} \times \pi \times 12$
 $= 6\pi \text{ cm}$

Perimeter of figure
 $= 6\pi + 6\pi + 12$
 $= (12\pi + 12) \text{ cm}$

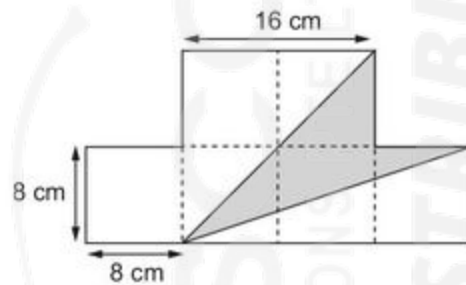
9.



Perimeter of figure
 $= \text{Curved part of semicircle} + 28 + 28$
 $= \left(\frac{1}{2} \times \pi \times 28\right) + 56$
 $= (14\pi + 56) \text{ cm}$

Exercise 4

1.



Area of each small square
 $= 8 \times 8$
 $= 64 \text{ cm}^2$

Total area of unshaded parts
 $= 4 \times \frac{1}{2} \times 64 \text{ cm}^2$
 $= 288 \text{ cm}^2$

2.

Area of big square
 $= 11 \times 11$
 $= 121 \text{ cm}^2$

Area of 1 small square
 $= 3 \times 3$
 $= 9 \text{ cm}^2$

Area of figure
 $= 121 - (4 \times 9)$
 $= 121 - 36$
 $= 85 \text{ cm}^2$

$$\begin{aligned}
 3. \text{ Radius of circle} \\
 &= 20 \text{ cm} \div 2 \\
 &= 10 \text{ cm}
 \end{aligned}$$

$$\begin{aligned}
 \text{Area of circle} \\
 &= 3.14 \times 10 \times 10 \\
 &= 314 \text{ cm}^2
 \end{aligned}$$

$$\begin{aligned}
 \text{Area of square} \\
 &= 5 \times 5 \\
 &= 25 \text{ cm}^2
 \end{aligned}$$

$$\begin{aligned}
 \text{Shaded area} \\
 &= 314 - 25 \\
 &= 289 \text{ cm}^2
 \end{aligned}$$

$$\begin{aligned}
 4. \text{ Area of rectangle} \\
 &= 17 \times 11 \\
 &= 187 \text{ cm}^2
 \end{aligned}$$

$$\begin{aligned}
 \text{Total area of 2 triangles} \\
 &= \left(\frac{1}{2} \times 7 \times 3\right) + \left(\frac{1}{2} \times 10 \times 3\right) \\
 &= 10.5 + 15 \\
 &= 25.5 \text{ cm}
 \end{aligned}$$

$$\begin{aligned}
 \text{Area of shaded part} \\
 &= 187 - 25.5 \\
 &= 161.5 \text{ cm}^2
 \end{aligned}$$

$$\begin{aligned}
 5. \text{ Perimeter} \\
 &= 24 \times 2 \text{ cm} \\
 &= 48 \text{ cm}
 \end{aligned}$$

$$\begin{aligned}
 6. \text{ Area of triangle} \\
 &= \frac{1}{2} \times 15 \times 15 \\
 &= 112.5 \text{ cm}^2
 \end{aligned}$$

$$\begin{aligned}
 \text{Unshaded area} \\
 &= \frac{2}{3} \times 112.5 \text{ cm}^2 \\
 &= 75 \text{ cm}^2
 \end{aligned}$$

$$\begin{aligned}
 7. \text{ Area of figure} \\
 &= (8 \times 3) + (5 \times 4) + (8 \times 3) \\
 &= 24 + 20 + 24 \\
 &= 68 \text{ cm}^2
 \end{aligned}$$

$$\begin{aligned}
 \text{Perimeter of figure} \\
 &= 3 + 4 + 5 + 2 + 3 + 8 + 3 + 2 \\
 &\quad + 8 + 8 \\
 &= 46 \text{ cm}
 \end{aligned}$$

$$\begin{aligned}
 8. \text{ Area of square} \\
 &= 7 \times 7 \\
 &= 49 \text{ cm}^2
 \end{aligned}$$

$$\begin{aligned}
 \text{Area of circle} \\
 &= \frac{22}{7} \times 3.5 \times 3.5 \\
 &= 38.5 \text{ cm}^2
 \end{aligned}$$

$$\begin{aligned}
 \text{Area of triangle} \\
 &= \frac{1}{2} \times 7 \times 3.5 \\
 &= 12.25 \text{ cm}^2
 \end{aligned}$$

$$\begin{aligned}
 \text{Total area of shaded parts} \\
 &= (49 - 38.5) + 12.25 \\
 &= 10.5 + 12.25 \\
 &= 22.75 \text{ cm}^2
 \end{aligned}$$

Achieve

Exercise 1

$$\begin{aligned}
 1. \text{ Diameter} &= 2 \times 105 \text{ m} \\
 &= 210 \text{ m}
 \end{aligned}$$

$$\begin{aligned}
 \text{Curved part of semicircle} \\
 &= \frac{1}{2} \times \frac{22}{7} \times 210 \\
 &= 330 \text{ m}
 \end{aligned}$$

$$330 \text{ m} - 210 \text{ m} = 120 \text{ m}$$

The man has to travel **120 m** further.

2. Diameter = $2 \times 12 \text{ cm} = 24 \text{ cm}$

Circumference of circle
 $= 3.14 \times 24$
 $= 75.36 \text{ cm}$

60 min \rightarrow 75.36 cm

1 min \rightarrow $\left(\frac{75.36}{60}\right) \text{ cm}$

38 min \rightarrow $38 \times \frac{75.36}{60} = 47.728 \text{ cm}$

The tip of the minute hand moves **47.728 cm**.

3. (a) Area of rectangle
 $= 16 \times 14$
 $= 224 \text{ cm}^2$

Area of big semicircle
 $= \frac{1}{2} \times 3.14 \times 3.5 \times 3.5$
 $= 19.2325 \text{ cm}^2$

Area of small semicircle
 $= \frac{1}{2} \times 3.14 \times 2 \times 2$
 $= 6.28 \text{ cm}^2$

Area of figure
 $= 224 + 19.2325 + 6.28$
 $= 249.5125$
 $= 249.51 \text{ cm}^2$ (correct to 2 d.p.)

The area of the figure is **249.51 cm²**.

(b) Curved part of big semicircle
 $= \frac{1}{2} \times 3.14 \times 7$
 $= 10.99 \text{ cm}$

Curved part of small semicircle
 $= \frac{1}{2} \times 3.14 \times 4$
 $= 6.28 \text{ cm}$

Perimeter of figure
 $= 16 + 10.99 + 7 + 12 + 6.28 + 14$
 $= 66.27 \text{ cm}$

The perimeter of the figure is **66.27 cm**.

4. Breadth of rectangle
 $= 40 \text{ cm}^2 \div 8 \text{ cm}$
 $= 5 \text{ cm}$

Area of semicircle
 $= \frac{1}{2} \times 3.14 \times 2.5 \times 2.5$
 $= 9.8125 \text{ cm}^2$

Area of triangle
 $= \frac{1}{2} \times 4 \times 5$
 $= 10 \text{ cm}^2$

Area of figure
 $= 9.8125 + 40 + 10$
 $= 59.8125$
 $= 59.81 \text{ cm}^2$ (correct to 2 d.p.)

The area of the figure is **59.81 cm²**.

5. Circumference of circle = $50\pi \text{ cm}$
 $\pi \times \text{Diameter} = 50\pi$
 Diameter = 50 cm
 Radius = $50 \text{ cm} \div 2$
 $= 25 \text{ cm}$

The radius of the circle is **25 cm**.

Area of circle
 $= \pi \times 25 \times 25$
 $= 625\pi \text{ cm}^2$

The area of the circle is **625 π cm²**.

6. Area of square
 $= 14 \times 14$
 $= 196 \text{ cm}^2$

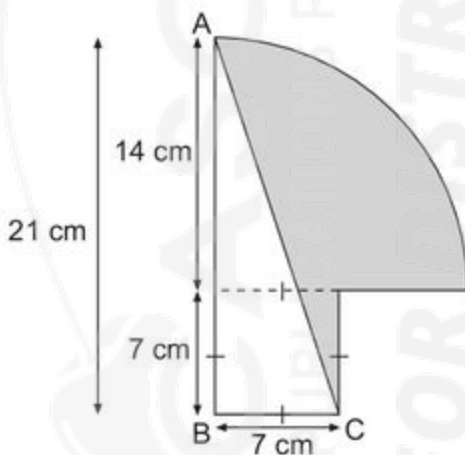
Area of quarter circle
 $= \frac{1}{4} \times \frac{22}{7} \times 14 \times 14$
 $= 154 \text{ cm}^2$

Area of triangle
 $= \frac{1}{2} \times 14 \times 14$
 $= 98 \text{ cm}^2$

Total area of shaded parts
 $= (196 - 154) + 98$
 $= 42 + 98$
 $= 140 \text{ cm}^2$

The total area of the shaded parts of the square is 140 cm^2 .

7.



Length of square
 $= 21 \text{ cm} \div 3$
 $= 7 \text{ cm}$

Radius of quarter circle
 $= 2 \times 7 \text{ cm}$
 $= 14 \text{ cm}$

Area of square
 $= 7 \times 7$
 $= 49 \text{ cm}^2$

Area of quarter circle
 $= \frac{1}{4} \times \frac{22}{7} \times 14 \times 14$
 $= 154 \text{ cm}^2$

Area of $\triangle ABC$
 $= \frac{1}{2} \times 7 \times 21$
 $= 73.5 \text{ cm}^2$

Area of shaded part
 $= (49 + 154) - 73.5$
 $= 203 - 73.5$
 $= 129.5 \text{ cm}^2$

The area of the shaded part of the figure is 129.5 cm^2 .

8. Area of big square
 $= 26 \times 26$
 $= 676 \text{ cm}^2$

Area of 1 isosceles triangle
 $= \frac{1}{2} \times 13 \times 13$
 $= 84.5 \text{ cm}^2$

Area of 4 isosceles triangles
 $= 4 \times 84.5 \text{ cm}^2$
 $= 338 \text{ cm}^2$

Area of circle
 $= \frac{22}{7} \times 7 \times 7$
 $= 154 \text{ cm}^2$

Area of shaded part
 $= 676 - 338 - 154$
 $= 184 \text{ cm}^2$

The area of the shaded part of the figure is 184 cm^2 .

9. (a) Length of painting
 $= 24.5 - 3 - 3$
 $= 18.5 \text{ cm}$

Breadth of painting
 $= 12 - 3 - 3$
 $= 6 \text{ cm}$

Area of painting
 $= 18.5 \times 6$
 $= 111 \text{ cm}^2$

The area of the painting is **111 cm²**.

(b) Area of big rectangle
 $= 24.5 \times 12$
 $= 294 \text{ cm}^2$

Area of border
 $= 294 - 111$
 $= 183 \text{ cm}^2$

The area of the border is **183 cm²**.

10. Radius of 1 circle
 $= 21 \text{ cm} \div 6$
 $= 3.5 \text{ cm}$

Area of 1 circle
 $= \frac{22}{7} \times 3.5 \times 3.5$
 $= 38.5 \text{ cm}^2$

Area of 6 circles
 $= 6 \times 38.5 \text{ cm}^2$
 $= 231 \text{ cm}^2$

Area of rectangle
 $= 21 \times 14$
 $= 294 \text{ cm}^2$

Total shaded area
 $= 294 - 231$
 $= 63 \text{ cm}^2$

The total shaded area is **63 cm²**.

11. Base : Height
 $4 : 3$

3 units = 6 cm
 1 unit = $6 \text{ cm} \div 3$
 $= 2 \text{ cm}$
 4 units = $4 \times 2 \text{ cm}$
 $= 8 \text{ cm}$

The height of the triangle is 8 cm.
 Length of square = 8 cm

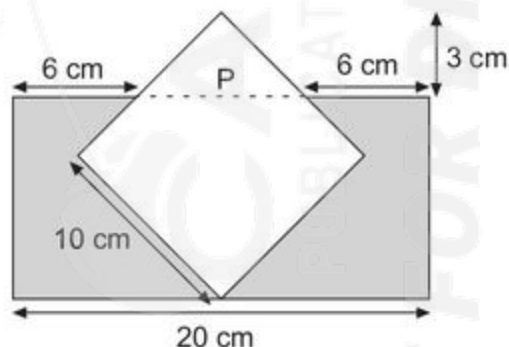
Area of triangle
 $= \frac{1}{2} \times 8 \times 6$
 $= 24 \text{ cm}^2$

Area of square
 $= 8 \times 8$
 $= 64 \text{ cm}^2$

Area of figure
 $= 24 + 64$
 $= 88 \text{ cm}^2$

The area of the figure is **88 cm²**.

12.



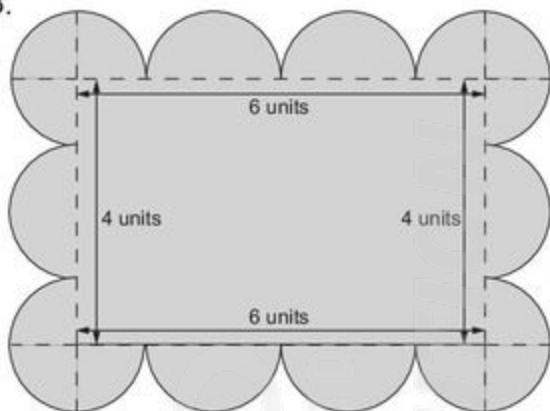
Area of 1 square
 $= 10 \times 10$
 $= 100 \text{ cm}^2$

Area of $\triangle P$
 $= \frac{1}{2} \times (20 - 6 - 6) \times 3$
 $= \frac{1}{2} \times 8 \times 3$
 $= 12 \text{ cm}^2$

$$\begin{aligned} \text{Area of overlap part} \\ &= 100 - 12 \\ &= 88 \text{ cm}^2 \end{aligned}$$

The area of the overlap is 88 cm^2 .

13.



Let the radius of each circle be 1 unit.
Perimeter of rectangle = 70 cm

$$6 \text{ units} + 4 \text{ units} + 6 \text{ units} + 4 \text{ units} = 70 \text{ cm}$$

$$20 \text{ units} = 70 \text{ cm}$$

$$\begin{aligned} 1 \text{ unit} &= 70 \text{ cm} \div 20 \\ &= 3.5 \text{ cm} \end{aligned}$$

$$\begin{aligned} \text{Length of rectangle} \\ &= 6 \times 3.5 \text{ cm} \\ &= 21 \text{ cm} \end{aligned}$$

$$\begin{aligned} \text{Breadth of rectangle} \\ &= 4 \times 3.5 \text{ cm} \\ &= 14 \text{ cm} \end{aligned}$$

$$\begin{aligned} \text{Area of rectangle} \\ &= 21 \times 14 \\ &= 294 \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} \text{Area of a quarter circle} \\ &= \frac{1}{4} \times \frac{22}{7} \times 3.5 \times 3.5 \\ &= 9.625 \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} \text{Area of 24 quarter circles} \\ &= 24 \times 9.625 \text{ cm}^2 \\ &= 231 \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} \text{Area of figure} \\ &= 294 + 231 \\ &= 525 \text{ cm}^2 \end{aligned}$$

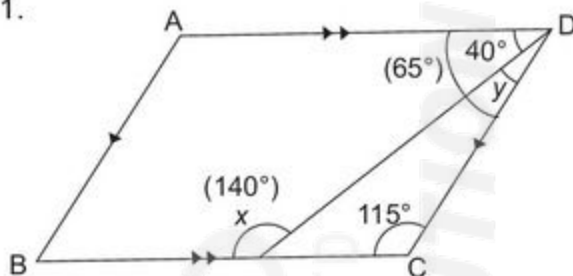
The area of the figure is 525 cm^2 .

Unit 7 Angles in Geometric Figures

Drills

Exercise 1

1.

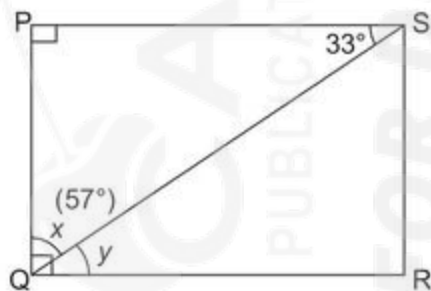


$$\angle x = 180^\circ - 40^\circ \text{ (\angle s between // lines)} \\ = 140^\circ$$

$$\angle ADC = 180^\circ - 115^\circ \text{ (\angle s between // lines)} \\ = 65^\circ$$

$$\angle y = 65^\circ - 40^\circ \\ = 25^\circ$$

2.



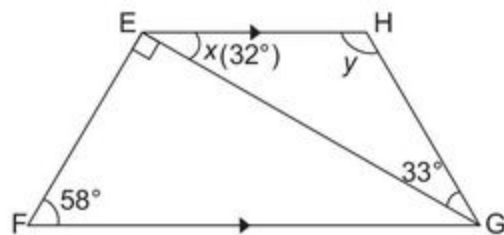
$$\angle QPS = 90^\circ \text{ (\angle s of a rectangle)}$$

$$\angle x = 180^\circ - 90^\circ - 33^\circ \text{ (\angle sum of } \triangle) \\ = 57^\circ$$

$$\angle PQR = 90^\circ \text{ (\angle s of a rectangle)}$$

$$\angle y = 90^\circ - 57^\circ \\ = 33^\circ$$

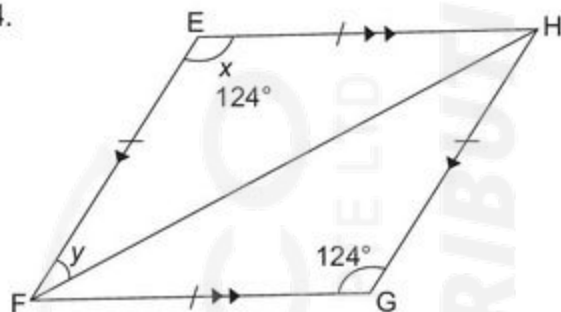
3.



$$\angle x = 180^\circ - 90^\circ - 58^\circ \text{ (\angle s between // lines)} \\ = 32^\circ$$

$$\angle y = 180^\circ - 33^\circ - 32^\circ \text{ (\angle sum of } \triangle) \\ = 115^\circ$$

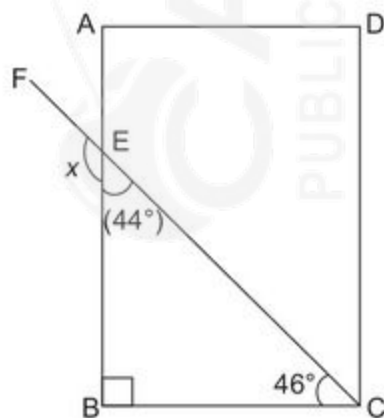
4.



$$\angle x = 124^\circ \text{ (opp. } \angle \text{ s of a rhombus)}$$

$$\angle y = (180^\circ - 124^\circ) \div 2 \text{ (isos. } \triangle) \\ = 56^\circ \div 2 \\ = 28^\circ$$

5.

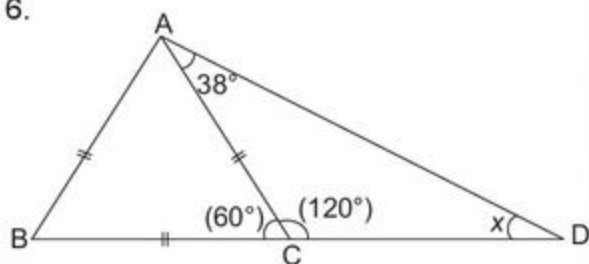


$$\angle ABC = 90^\circ \text{ (\angle s of a rectangle)}$$

$$\angle BEC = 180^\circ - 90^\circ - 46^\circ \text{ (\angle sum of } \triangle) \\ = 44^\circ$$

$$\angle x = 180^\circ - 44^\circ \text{ (\angle s on a straight line)} \\ = 136^\circ$$

6.



$$\begin{aligned}\angle ACB &= 180^\circ \div 3 \text{ (equi. } \triangle) \\ &= 60^\circ\end{aligned}$$

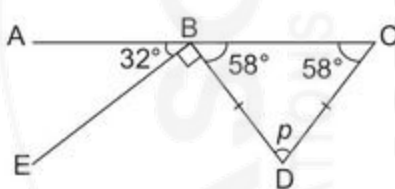
$$\begin{aligned}\angle ACD &= 180^\circ - 60^\circ \text{ (}\angle\text{s on a straight line)} \\ &= 120^\circ\end{aligned}$$

$$\begin{aligned}\angle x &= 180^\circ - 120^\circ - 38^\circ \text{ (}\angle\text{ sum of } \triangle) \\ &= 22^\circ\end{aligned}$$

Perform

Exercise 1

1.

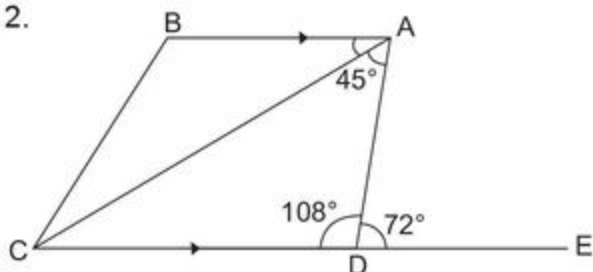


$$\begin{aligned}\angle DBC &= 180^\circ - 90^\circ - 32^\circ \text{ (}\angle\text{s on a straight line)} \\ &= 58^\circ\end{aligned}$$

$$\angle DCB = 58^\circ \text{ (isos. } \triangle)$$

$$\begin{aligned}\angle p &= 180^\circ - 58^\circ - 58^\circ \text{ (}\angle\text{ sum of } \triangle) \\ &= 64^\circ\end{aligned}$$

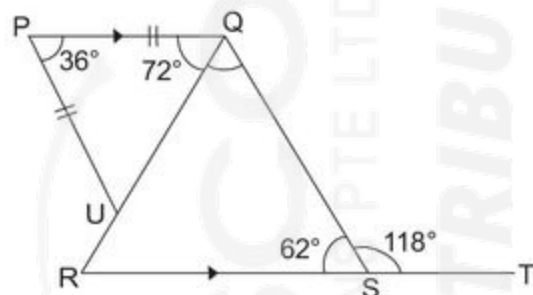
2.



$$\begin{aligned}\angle ADC &= 180^\circ - 72^\circ \text{ (}\angle\text{s on a straight line)} \\ &= 108^\circ\end{aligned}$$

$$\begin{aligned}\angle BAC &= 180^\circ - 45^\circ - 108^\circ \\ &\text{ (}\angle\text{s between } // \text{ lines)} \\ &= 27^\circ\end{aligned}$$

3.

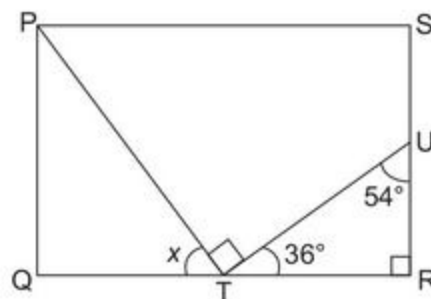


$$\begin{aligned}\angle PQU &= (180^\circ - 36^\circ) \div 2 \text{ (isos. } \triangle) \\ &= 144^\circ \div 2 \\ &= 72^\circ\end{aligned}$$

$$\begin{aligned}\angle QSR &= 180^\circ - 118^\circ \text{ (}\angle\text{s on a straight line)} \\ &= 62^\circ\end{aligned}$$

$$\begin{aligned}\angle RQS &= 180^\circ - 72^\circ - 62^\circ \text{ (}\angle\text{s between } // \text{ lines)} \\ &= 46^\circ\end{aligned}$$

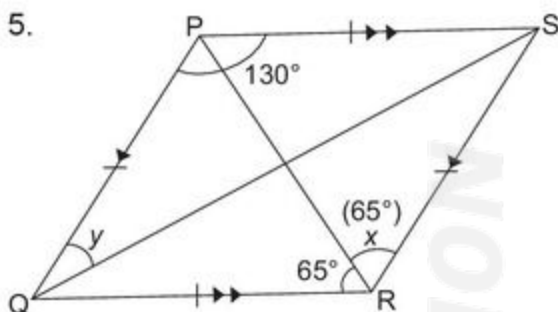
4.



$$\angle QRS = 90^\circ \text{ (}\angle\text{s of a rectangle)}$$

$$\begin{aligned}\angle RTU &= 180^\circ - 90^\circ - 54^\circ \text{ (\angle sum of } \triangle) \\ &= 36^\circ\end{aligned}$$

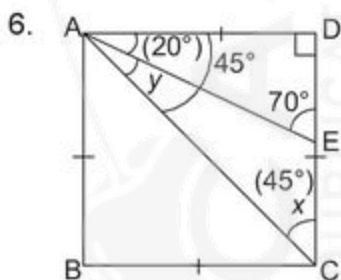
$$\begin{aligned}\angle x &= 180^\circ - 90^\circ - 36^\circ \text{ (\angle s on a straight line)} \\ &= 54^\circ\end{aligned}$$



$$\begin{aligned}\angle x &= \angle QRP \text{ (PR divides the rhombus into half)} \\ &= 65^\circ\end{aligned}$$

$$\begin{aligned}\angle QPS &= \angle QRS \text{ (opp. } \angle \text{ s of rhombus)} \\ &= 65^\circ + 65^\circ \\ &= 130^\circ\end{aligned}$$

$$\begin{aligned}\angle y &= (180^\circ - 130^\circ) \div 2 \text{ (isos. } \triangle) \\ &= 50^\circ \div 2 \\ &= 25^\circ\end{aligned}$$



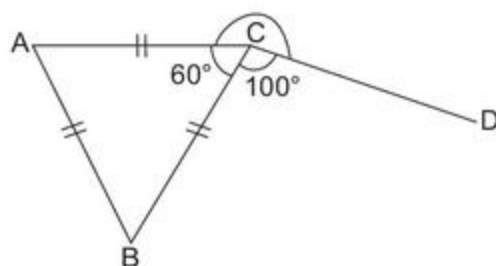
$$\angle ADC = 90^\circ \text{ (\angle s of a square)}$$

$$\begin{aligned}\angle x &= (180^\circ - 90^\circ) \div 2 \text{ (isos. } \triangle) \\ &= 90^\circ \div 2 \\ &= 45^\circ\end{aligned}$$

$$\begin{aligned}\angle DAE &= 180^\circ - 90^\circ - 70^\circ \text{ (\angle sum of } \triangle) \\ &= 20^\circ\end{aligned}$$

$$\angle DAC = 45^\circ$$

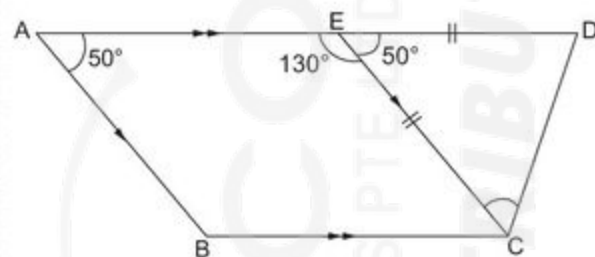
$$\begin{aligned}\angle y &= 45^\circ - 20^\circ \\ &= 25^\circ\end{aligned}$$



$$\begin{aligned}\angle ACB &= 180^\circ \div 3 \text{ (equi. } \triangle) \\ &= 60^\circ\end{aligned}$$

$$\begin{aligned}\angle ACD &= 360^\circ - 60^\circ - 100^\circ \text{ (\angle s at a point)} \\ &= 200^\circ\end{aligned}$$

8.

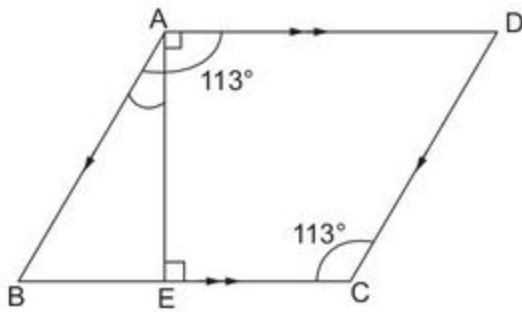


$$\begin{aligned}\angle AEC &= 180^\circ - 50^\circ \text{ (\angle s between } // \text{ lines)} \\ &= 130^\circ\end{aligned}$$

$$\begin{aligned}\angle CED &= 180^\circ - 130^\circ \text{ (\angle s on a straight line)} \\ &= 50^\circ\end{aligned}$$

$$\begin{aligned}\angle ECD &= (180^\circ - 50^\circ) \div 2 \text{ (isos. } \triangle) \\ &= 130^\circ \div 2 \\ &= 65^\circ\end{aligned}$$

9.

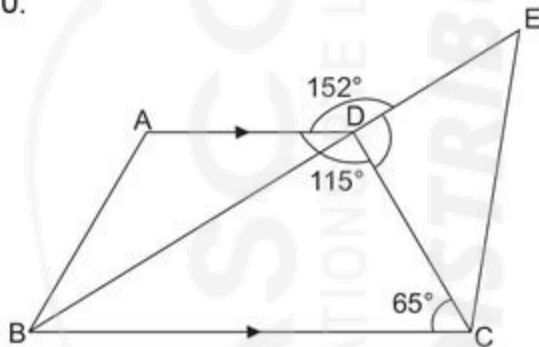


$$\begin{aligned}\angle DAE &= 180^\circ - 90^\circ \text{ (\angle s between // lines)} \\ &= 90^\circ\end{aligned}$$

$$\angle BAD = 113^\circ \text{ (opp. } \angle \text{ s of a parallelogram)}$$

$$\begin{aligned}\angle BAE &= 113^\circ - 90^\circ \\ &= 23^\circ\end{aligned}$$

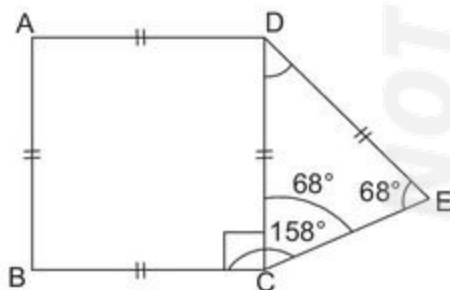
10.



$$\begin{aligned}\angle ADC &= 180^\circ - 65^\circ \text{ (\angle s between parallel lines)} \\ &= 115^\circ\end{aligned}$$

$$\begin{aligned}\angle CDE &= 360^\circ - 152^\circ - 115^\circ \text{ (\angle s at a point)} \\ &= 93^\circ\end{aligned}$$

11.



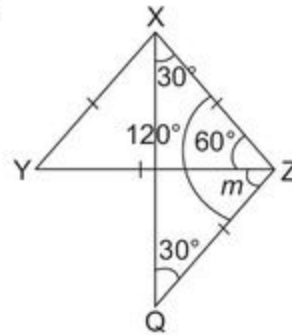
$$\angle BCD = 90^\circ \text{ (\angle s of a square)}$$

$$\begin{aligned}\angle DCE &= 158^\circ - 90^\circ \\ &= 68^\circ\end{aligned}$$

$$\angle DEC = 68^\circ \text{ (isos. } \Delta)$$

$$\begin{aligned}\angle CDE &= 180^\circ - 68^\circ - 68^\circ \text{ (\angle sum of } \Delta) \\ &= 44^\circ\end{aligned}$$

12.



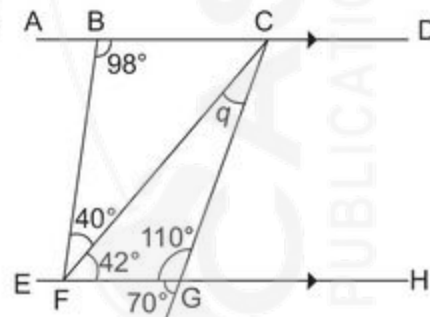
$$\angle ZXQ = 30^\circ \text{ (isos. } \Delta)$$

$$\begin{aligned}\angle QZX &= 180^\circ - 30^\circ - 30^\circ \text{ (\angle sum of } \Delta) \\ &= 120^\circ\end{aligned}$$

$$\begin{aligned}\angle XZY &= 180^\circ \div 3 \text{ (equi. } \Delta) \\ &= 60^\circ\end{aligned}$$

$$\begin{aligned}\angle m &= 120^\circ - 60^\circ \\ &= 60^\circ\end{aligned}$$

13.

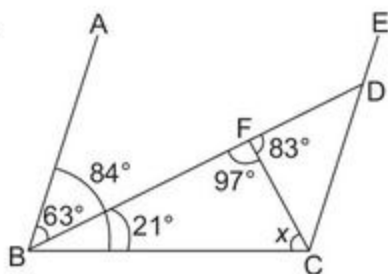


$$\begin{aligned}\angle CFG &= 180^\circ - 98^\circ - 40^\circ \text{ (\angle s between // lines)} \\ &= 42^\circ\end{aligned}$$

$$\begin{aligned}\angle FGC &= 180^\circ - 70^\circ \text{ (\angle s on a straight line)} \\ &= 110^\circ\end{aligned}$$

$$\begin{aligned}\angle q &= 180^\circ - 42^\circ - 110^\circ \text{ (\angle sum of } \Delta) \\ &= 28^\circ\end{aligned}$$

14.

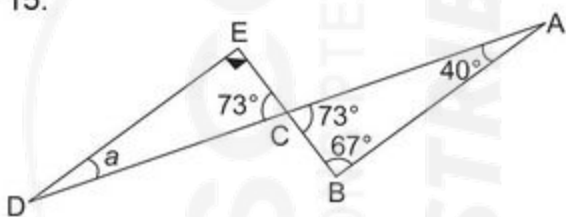


$$\begin{aligned}\angle CBF &= 84^\circ - 63^\circ \\ &= 21^\circ\end{aligned}$$

$$\begin{aligned}\angle BFC &= 180^\circ - 83^\circ \text{ (\angle s on a straight line)} \\ &= 97^\circ\end{aligned}$$

$$\begin{aligned}\angle x &= 180^\circ - 21^\circ - 97^\circ \text{ (\angle sum of } \triangle) \\ &= 62^\circ\end{aligned}$$

15.



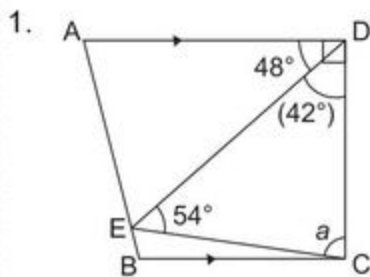
$$\begin{aligned}\angle ACB &= 180^\circ - 67^\circ - 40^\circ \text{ (\angle sum of } \triangle) \\ &= 73^\circ\end{aligned}$$

$$\angle DCE = 73^\circ \text{ (vert. opp. } \angle \text{s)}$$

$$\begin{aligned}\angle CDE &= 180^\circ - 90^\circ - 73^\circ \text{ (\angle sum of } \triangle) \\ &= 17^\circ\end{aligned}$$

Achieve

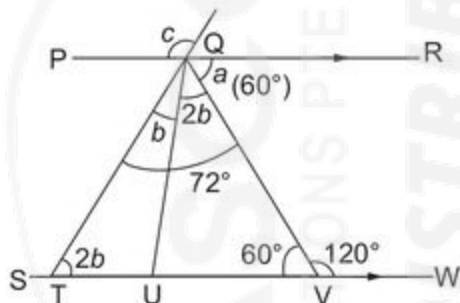
Exercise 1



$$\begin{aligned}\angle CDE &= 90^\circ - 48^\circ \\ &= 42^\circ\end{aligned}$$

$$\begin{aligned}\angle a &= 180^\circ - 42^\circ - 54^\circ \text{ (\angle sum of } \triangle) \\ &= 84^\circ\end{aligned}$$

2.

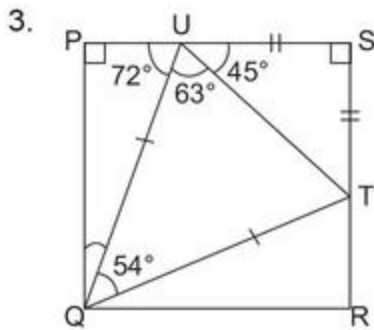


$$\begin{aligned}\angle a &= 180^\circ - 120^\circ \text{ (\angle s between } // \text{ lines)} \\ &= 60^\circ\end{aligned}$$

$$\begin{aligned}\angle QVT &= 180^\circ - 120^\circ \text{ (\angle s on a straight line)} \\ &= 60^\circ\end{aligned}$$

$$\begin{aligned}\angle b &= (180^\circ - 60^\circ) \div 5 \text{ (\angle sum of } \triangle) \\ &= 120^\circ \div 5 \\ &= 24^\circ\end{aligned}$$

$$\begin{aligned}\angle c &= 60^\circ + (3 \times 24^\circ) \text{ (vert. opp. } \angle \text{s)} \\ &= 60^\circ + 72^\circ \\ &= 132^\circ\end{aligned}$$



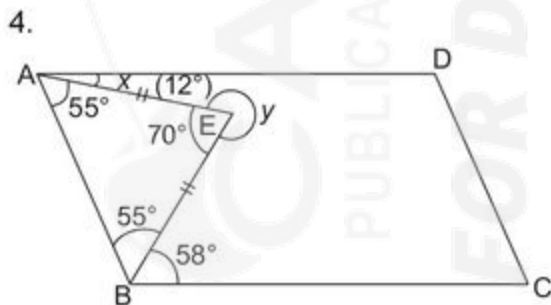
$$\begin{aligned}\angle QUT &= (180^\circ - 54^\circ) \div 2 \text{ (isos. } \triangle) \\ &= 126^\circ \div 2 \\ &= 63^\circ\end{aligned}$$

$$\angle PSR = 90^\circ \text{ (}\angle\text{s of a square)}$$

$$\begin{aligned}\angle SUT &= (180^\circ - 90^\circ) \div 2 \text{ (isos. } \triangle) \\ &= 90^\circ \div 2 \\ &= 45^\circ\end{aligned}$$

$$\begin{aligned}\angle QUP &= 180^\circ - 45^\circ - 63^\circ \text{ (}\angle\text{s on a straight line)} \\ &= 72^\circ\end{aligned}$$

$$\begin{aligned}\angle QPS &= 90^\circ \text{ (}\angle\text{s of a square)} \\ \angle PQU &= 180^\circ - 90^\circ - 72^\circ \text{ (}\angle\text{ sum of } \triangle) \\ &= 18^\circ\end{aligned}$$

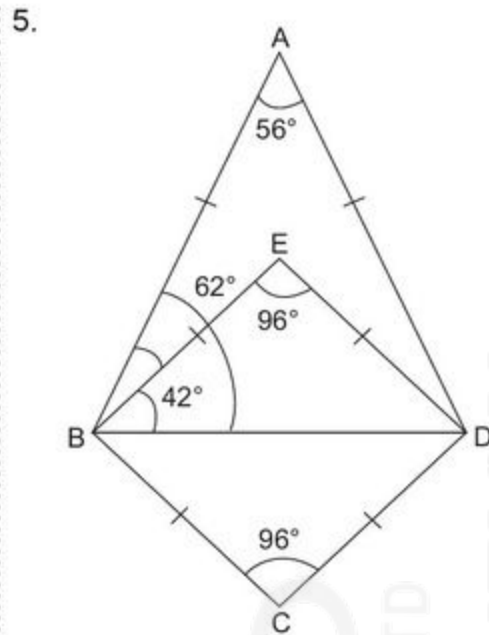


$$\angle EBA = 55^\circ \text{ (isos. } \triangle)$$

$$\begin{aligned}\angle x &= 180^\circ - 58^\circ - 55^\circ - 55^\circ \text{ (}\angle\text{s between } \parallel \text{ lines)} \\ &= 12^\circ\end{aligned}$$

$$\begin{aligned}\angle AEB &= 180^\circ - 55^\circ - 55^\circ \text{ (}\angle\text{ sum of } \triangle) \\ &= 70^\circ\end{aligned}$$

$$\begin{aligned}\angle y &= 360^\circ - 70^\circ \text{ (}\angle\text{s at a point)} \\ &= 290^\circ\end{aligned}$$

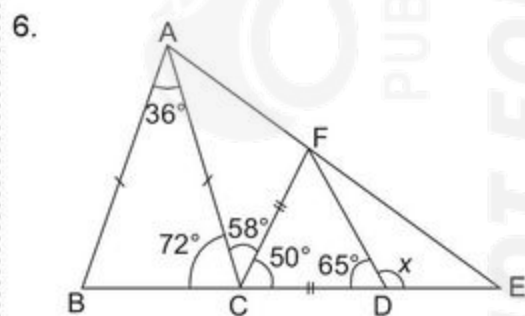


$$\angle BED = 96^\circ \text{ (opp. } \angle\text{s of a rhombus)}$$

$$\begin{aligned}\angle EBD &= (180^\circ - 96^\circ) \div 2 \text{ (isos. } \triangle) \\ &= 84^\circ \div 2 \\ &= 42^\circ\end{aligned}$$

$$\begin{aligned}\angle ABD &= (180^\circ - 56^\circ) \div 2 \text{ (isos. } \triangle) \\ &= 124^\circ \div 2 \\ &= 62^\circ\end{aligned}$$

$$\begin{aligned}\angle ABE &= 62^\circ - 42^\circ \\ &= 20^\circ\end{aligned}$$



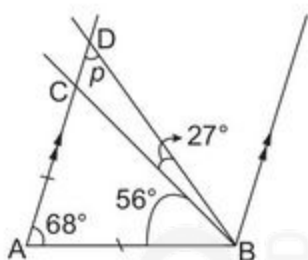
$$\begin{aligned}\angle ACB &= (180^\circ - 36^\circ) \div 2 \text{ (isos. } \triangle) \\ &= 144^\circ \div 2 \\ &= 72^\circ\end{aligned}$$

$$\begin{aligned}\angle FCD &= 180^\circ - 72^\circ - 58^\circ \text{ (\(\angle\text{s on a straight line})} \\ &= 50^\circ\end{aligned}$$

$$\begin{aligned}\angle CDF &= (180^\circ - 50^\circ) \div 2 \text{ (isos. } \triangle) \\ &= 130^\circ \div 2 \text{ (isos. } \triangle) \\ &= 65^\circ\end{aligned}$$

$$\begin{aligned}\angle x &= 180^\circ - 65^\circ \text{ (\(\angle\text{s on a straight line})} \\ &= 115^\circ\end{aligned}$$

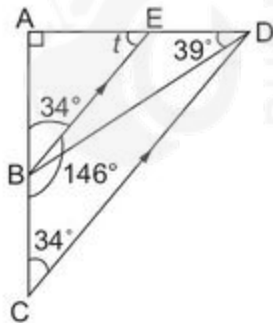
7.



$$\begin{aligned}\angle ABC &= (180^\circ - 68^\circ) \div 2 \text{ (isos. } \triangle) \\ &= 112^\circ \div 2 \\ &= 56^\circ\end{aligned}$$

$$\begin{aligned}\angle p &= 180^\circ - 68^\circ - 56^\circ - 27^\circ \text{ (\(\angle\text{ sum of } \triangle))} \\ &= 29^\circ\end{aligned}$$

8.

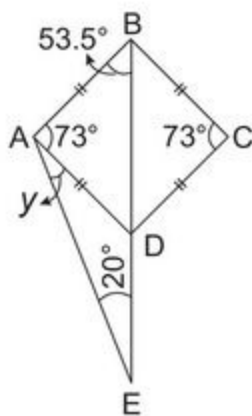


$$\begin{aligned}\angle CBE &= 180^\circ - 34^\circ \text{ (\(\angle\text{s between } // \text{ lines})} \\ &= 146^\circ\end{aligned}$$

$$\begin{aligned}\angle ABE &= 180^\circ - 146^\circ \text{ (\(\angle\text{s on a straight line})} \\ &= 34^\circ\end{aligned}$$

$$\begin{aligned}\angle t &= 180^\circ - 90^\circ - 34^\circ \text{ (\(\angle\text{ sum of } \triangle))} \\ &= 56^\circ\end{aligned}$$

9.

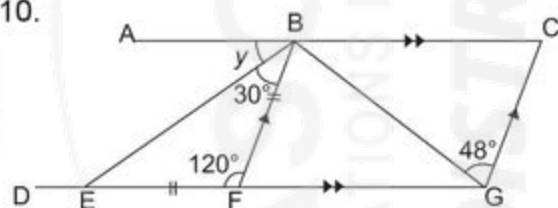


$$\angle BAD = 73^\circ \text{ (opp. } \angle\text{s of a rhombus)}$$

$$\begin{aligned}\angle ABD &= (180^\circ - 73^\circ) \div 2 \text{ (isos. } \triangle) \\ &= 107^\circ \div 2 \\ &= 53.5^\circ\end{aligned}$$

$$\begin{aligned}\angle y &= 180^\circ - 53.5^\circ - 73^\circ - 20^\circ \text{ (\(\angle\text{ sum of } \triangle))} \\ &= 33.5^\circ\end{aligned}$$

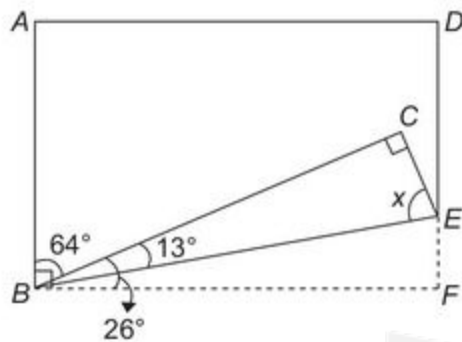
10.



$$\begin{aligned}\angle EBF &= (180^\circ - 120^\circ) \div 2 \text{ (isos. } \triangle) \\ &= 60^\circ \div 2 \\ &= 30^\circ\end{aligned}$$

$$\begin{aligned}\angle y &= 180^\circ - 120^\circ - 30^\circ \text{ (\(\angle\text{s between } // \text{ lines})} \\ &= 30^\circ\end{aligned}$$

11.



$$\angle ABF = 90^\circ \text{ (}\angle\text{s of a rectangle)}$$

$$\begin{aligned}\angle CBF &= 90^\circ - 64^\circ \\ &= 26^\circ\end{aligned}$$

$$\begin{aligned}\angle CBE &= 26^\circ \div 2 \\ &= 13^\circ\end{aligned}$$

$$\angle BCE = 90^\circ \text{ (}\angle\text{s of a rectangle)}$$

$$\begin{aligned}\angle x &= 180^\circ - 90^\circ - 13^\circ \text{ (}\angle\text{ sum of } \triangle) \\ &= 77^\circ\end{aligned}$$

Unit 8 Solid Figures and Nets

Drills

Exercise 1

1.

Figure					
Property	Cylinder	Cube	Rectangular Cuboid	Pyramid (Square-based)	Pyramid (Triangle-based)
Number of flat surface(s)	2	6	6	5	4
Number of curved surface(s)	1	0	0	0	0
Number of faces	3	6	6	5	4
Number of square face(s)	0	6	0	1	0
Number of rectangular face(s)	0	0	6	0	0
Number of triangular face(s)	0	0	0	4	4

2.

Cylinder 	Cube
Cuboid 	Square-based pyramid
Triangular prism 	

Perform


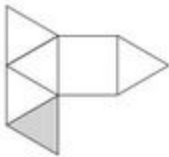
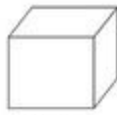
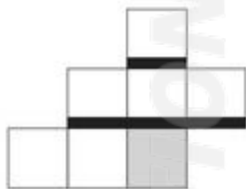

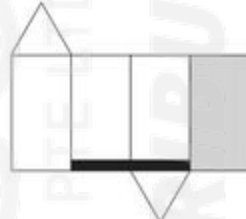
Exercise 1

Length of one edge	Number of unit cubes with 3 painted faces	Number of unit cubes with 2 painted faces	Number of unit cubes with 1 painted face	Number of unit cubes with no painted faces
3	8	12	6	1
5	8	36	54	27
7	8	60	150	125

Exercise 2

- Cuboid
 - Pyramid (square-based)
 - Cube
 - Triangular prism
- ✓
 - ✗
 - ✓
 - ✓
- C
- D
- A
- A
- A and C
- B, C and E
- D
- C

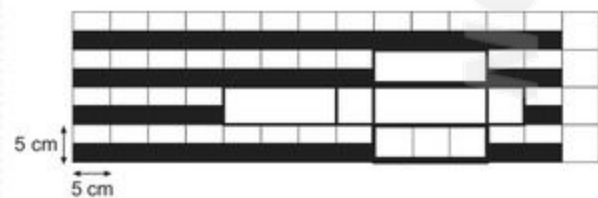
Exercise 3

Solid	Net
 Pyramid	
 Cube	
 Prism	

Achieve

Exercise 1

- A = 1 and B = 5.
- D
- Volume of cuboid
 $= 6 \times 3 \times 2$
 $= 36 \text{ cm}^3$
- (a)



$$\begin{aligned}
 & \text{(b) Total area of the faces} \\
 & = 4 \times (15 \times 5) + 2 \times (5 \times 5) \\
 & = 300 + 50 \\
 & = 350 \text{ cm}^2
 \end{aligned}$$

5. E

$$\begin{aligned}
 & \text{6. (a) Total surface area of solid} \\
 & = (4 \times 4) + 4 \times \left(\frac{1}{2} \times 4 \times 10\right) \\
 & = 16 + (4 \times 20) \\
 & = 16 + 80 \\
 & = 96 \text{ cm}^2
 \end{aligned}$$

$$\begin{aligned}
 & \text{(b) } \frac{1}{10} \times 96 \text{ cm}^2 = 9.6 \text{ cm}^2 \\
 & 96 \text{ cm}^2 + 9.6 \text{ cm}^2 = 105.6 \text{ cm}^2
 \end{aligned}$$

105.6 cm² of cardboard is required to make the solid.

Unit 9 Pie Charts

Drills

Exercise 1

$$\begin{aligned}
 & \text{1. (a) Fraction he spends on rent} \\
 & = \frac{1}{2} - \frac{1}{6} - \frac{1}{6} \\
 & = \frac{3}{6} - \frac{1}{6} - \frac{1}{6} \\
 & = \frac{1}{6}
 \end{aligned}$$

Amount he spends on rent

$$\begin{aligned}
 & = \frac{1}{6} \times \$1800 \\
 & = \mathbf{\$300}
 \end{aligned}$$

$$\begin{aligned}
 & \text{(b) Amount he saves} \\
 & = \frac{25}{100} \times \$1800 \\
 & = \mathbf{\$450}
 \end{aligned}$$

$$\begin{aligned}
 & \text{(c) Amount he spends on car instalment} \\
 & = \frac{1}{4} \times \$1800 \\
 & = \$450
 \end{aligned}$$

$$\$450 - \$300 = \$150$$

He spends **\\$150** more on car instalment than rent.

$$\begin{aligned}
 & \text{(d) } \frac{1}{6} + \frac{1}{6} = \frac{2}{6} \\
 & \quad \quad \quad = \frac{1}{3}
 \end{aligned}$$

Amount he spends on food and clothing

$$\begin{aligned}
 & = \frac{1}{3} \times \$1800 \\
 & = \mathbf{\$600}
 \end{aligned}$$

(e) $100\% - 25\% = 75\%$
 Monthly expenditure
 $= \frac{75}{100} \times \1800
 $= \$1350$

2. (a) $100\% - 75\% = 25\%$

$$25\% = \frac{25}{100} = \frac{1}{4}$$

Fraction of Malay pupils

$$\begin{aligned} &= \frac{1}{4} - \frac{1}{12} - \frac{1}{12} \\ &= \frac{3}{12} - \frac{1}{12} - \frac{1}{12} \\ &= \frac{1}{12} \end{aligned}$$

$$\frac{1}{12} \rightarrow 75 \text{ pupils}$$

There are **75** Indian pupils.

(b) $75\% = \frac{75}{100} = \frac{3}{4} = \frac{9}{12}$

$$\frac{1}{12} \rightarrow 75 \text{ pupils}$$

$$\frac{9}{12} \rightarrow 9 \times 75 = 675 \text{ pupils}$$

There are **675** Chinese pupils.

(c) $675 - 75 = 600$

There are **600** more Chinese than Malay pupils.

(d) $\frac{1}{12} \rightarrow 75 \text{ pupils}$

$$\frac{12}{12} \rightarrow 12 \times 75 = 900 \text{ pupils}$$

There are **900** pupils altogether.

(e) $900 - 675 = 225$

There are **225** non-Chinese pupils.

3. (a) Fraction of game cards

$$= \frac{1}{2} - \frac{1}{4}$$

$$= \frac{1}{4}$$

$$= \frac{2}{8}$$

$$\frac{2}{8} \rightarrow 720 \text{ items}$$

$$\frac{1}{8} \rightarrow 720 \div 2 = 360 \text{ items}$$

Raymond collected **360** erasers.

(b) $\frac{1}{8} \rightarrow 360 \text{ items}$

$$\frac{8}{8} \rightarrow 8 \times 360 = 2880 \text{ items}$$

The total number of items Raymond collected was **2880**.

(c) He had the same number of **game cards** and **stickers**.

(d) Number of stamps

$$= \frac{37.5}{100} \times 2880$$

$$= \mathbf{1080}$$

(e) $1080 - 720 = 360$

He collected **360** more stamps than stickers.

Perform

Exercise 1

1. (a) (4)

$$25\% - 12.5\% = 12.5\%$$

$$12.5\% \rightarrow 90 \text{ children}$$

$$1\% \rightarrow \frac{90}{12.5} = 7.2 \text{ children}$$

$$37.5\% \rightarrow 37.5 \times 7.2 = 270 \text{ children}$$

270 children prefer apples.

(b) (1)
90 children prefer mangoes.

(c) (2)
The same number of children prefer oranges as apples.

$$270 - 90 = 180$$

180 more children prefer oranges to grapes.

(d) (3)
Required fraction

$$\begin{aligned} &= \frac{37.5}{100} \\ &= \frac{75}{200} \\ &= \frac{3}{8} \end{aligned}$$

(e) (1)
Grapes : Oranges
90 : 270
= 1 : 3

2. (a) (1)

$$\begin{aligned} &1 - \frac{1}{8} - \frac{1}{4} \\ &= 1 - \frac{1}{8} - \frac{2}{8} \\ &= \frac{5}{8} \end{aligned}$$

$$\frac{5}{8} \rightarrow \$2000$$

$$\frac{1}{8} \rightarrow \$2000 \div 5 = \$400$$

Aunt Jessie spent \$400 on the doll house.

(b) (2)

$$\frac{1}{4} = \frac{2}{8}$$

$$\frac{1}{8} \rightarrow \$400$$

$$\frac{2}{8} \rightarrow 2 \times \$400 = \$800$$

Aunt Jessie spent \$800 on the wallet.

(c) (3)
 $\$2000 - \$800 = \$1200$

She spent \$1200 more on the computer than the wallet.

(d) (4)

$$\frac{1}{8} \rightarrow \$400$$

$$\frac{8}{8} \rightarrow 8 \times \$400 = \$3200$$

Aunt Jessie spent \$3200 altogether.

(e) (4)
Doll house : Total
\$400 : \$3200
= 4 : 32
= 1 : 8

3. (a) (1)

$$\begin{aligned} \frac{1}{2} - \frac{3}{8} &= \frac{4}{8} - \frac{3}{8} \\ &= \frac{1}{8} \end{aligned}$$

$$\frac{1}{4} = \frac{2}{8}$$

$$\frac{2}{8} \rightarrow 18 \text{ items}$$

$$\frac{1}{8} \rightarrow 18 \div 2 = 9$$

Baby Keith received 9 bibs.

$$\begin{aligned} \text{(b) (2)} \\ \frac{3}{8} - \frac{1}{4} \\ = \frac{3}{8} - \frac{2}{8} \\ = \frac{1}{8} \end{aligned}$$

Baby Keith received 9 more pieces of clothes than games.

$$\begin{aligned} \text{(c) (3)} \\ \text{Required percentage} \\ = \frac{3}{8} \times 100\% \\ = \underline{37.5\%} \end{aligned}$$

$$\begin{aligned} \text{(d) (1)} \\ \text{Required fraction} \\ = \frac{1}{8} \leftarrow \text{From part (a).} \end{aligned}$$

$$\begin{aligned} \text{(e) (2)} \\ \frac{1}{8} \longrightarrow 9 \text{ items} \\ \frac{3}{8} \longrightarrow 3 \times 9 = 27 \text{ items} \end{aligned}$$

Baby Keith received 27 pieces of clothing.

$$\begin{array}{l} \text{Milk bottles} : \text{Bibs} : \text{Clothing} \\ 18 : 9 : 27 \\ = \underline{2 : 1 : 3} \end{array}$$

Achieve

Exercise 1

$$1. \text{ (a) } \frac{1}{4} = 25\%$$

$$\begin{aligned} \text{Percentage of scouts} \\ = 100\% - 25\% - 25\% - 20\% \\ = 30\% \end{aligned}$$

30% of the pupils were scouts.

$$\begin{aligned} \text{(b) } 30\% \longrightarrow 180 \text{ pupils} \\ 1\% \longrightarrow 180 \div 30 = 6 \text{ pupils} \\ 25\% \longrightarrow 25 \times 6 = 150 \text{ pupils} \end{aligned}$$

150 pupils joined the Drama Club as their CCA.

$$\text{(c) } 20\% = \frac{20}{100} = \frac{1}{5}$$

$\frac{1}{5}$ of the pupils joined the Mathematics Club as their CCA.

$$\begin{aligned} \text{(d) } 25\% - 20\% = 5\% \\ 1\% \longrightarrow 6 \text{ pupils} \\ 5\% \longrightarrow 5 \times 6 = 30 \text{ pupils} \end{aligned}$$

The difference between the number of pupils who took up IT Club and Mathematics Club was 30.

$$\text{(e) } 100\% \longrightarrow 100 \times 6 = 600 \text{ pupils}$$

600 pupils took part in various CCA.

$$\begin{aligned} 30\% \longrightarrow 600 \text{ pupils} \\ 1\% \longrightarrow 600 \div 30 = 20 \text{ pupils} \\ 100\% \longrightarrow 100 \times 20 \\ = 2000 \text{ pupils} \end{aligned}$$

There were 2000 pupils in the school.

$$2. \text{ (a) } \frac{1}{8} \times 600 = 75$$

75 pupils eat noodles.

$$\text{(b) } \frac{1}{4} \times 600 = 150$$

150 pupils eat mee goreng.

$$\text{(c) } 10\% = \frac{10}{100} = \frac{1}{10}$$

$\frac{1}{10}$ of the pupils eat chicken rice.

$$(d) \quad \frac{1}{8} = \frac{1}{8} \times 100\% = 12.5\%$$

$$\frac{1}{4} = \frac{1}{4} \times 100\% = 25\%$$

Percentage of pupils who eat
curry puffs

$$= 100\% - 25\% - 20\% - 11\%$$

$$- 10\% - 12.5\%$$

$$= 21.5\%$$

$$21.5\% - 20\% = 1.5\%$$

$$\frac{1.5}{100} \times 600 = 9$$

The difference between the
number of pupils who choose
curry puffs and those who choose
porridge is 9.

$$(e) \quad \text{Number of plates of chicken rice}$$

$$= \frac{10}{100} \times 600$$

$$= 60$$

$$\text{Number of curry puffs}$$

$$= \frac{21.5}{100} \times 600$$

$$= 129$$

$$\text{Total amount spent}$$

$$= (60 \times \$1.50) + (129 \times \$0.80)$$

$$= \$90 + \$103.20$$

$$= \$193.20$$

\$193.20 is spent on these food
items.

$$3. (a) \quad \frac{1}{2} - \frac{1}{6} - \frac{1}{6}$$

$$= \frac{3}{6} - \frac{1}{6} - \frac{1}{6}$$

$$= \frac{1}{6}$$

$$\frac{1}{6} \longrightarrow \$390$$

He spends **\$390** on clothing.

$$(b) \quad \frac{1}{9} \times 100\% = 11.11\% \text{ (correct to 2 d.p.)}$$

He spends **11.11%** of his total
expenditure on food.

$$(c) \quad \frac{1}{2} - \frac{1}{9}$$

$$= \frac{9}{18} - \frac{2}{18}$$

$$= \frac{7}{18}$$

He spends $\frac{7}{18}$ of his income on
his car instalment.

$$(d) \quad \frac{1}{6} \longrightarrow \$390$$

$$\$390 \div 3 = \$130$$

Each of his children receives
\$130.

$$(e) \quad \frac{1}{6} \longrightarrow \$390$$

$$\frac{6}{6} \longrightarrow 6 \times \$390 = \$2340$$

His monthly expenditure is **\$2340**.

$$4. (a) \quad \frac{25}{100} \times 300 = 75$$

25% of the pupils chose **vanilla**
ice-cream.

(b) The most popular ice-cream
flavour was chocolate.

Percentage of pupils who chose
chocolate

$$= \frac{105}{300} \times 100\%$$

$$= 35\%$$

35% of the pupils chose the most
popular ice-cream flavour.

5. $55\% \rightarrow 32 + 12 = 44$ fruits
 $1\% \rightarrow \left(\frac{44}{55}\right)$ fruits
 $100\% \rightarrow 100 \times \frac{44}{55} = 80$ fruits

Lisa bought 80 fruits altogether.

$$\begin{aligned} \text{Number of pears} &= 80 - (21 + 32 + 12) \\ &= 80 - 65 \\ &= 15 \end{aligned}$$

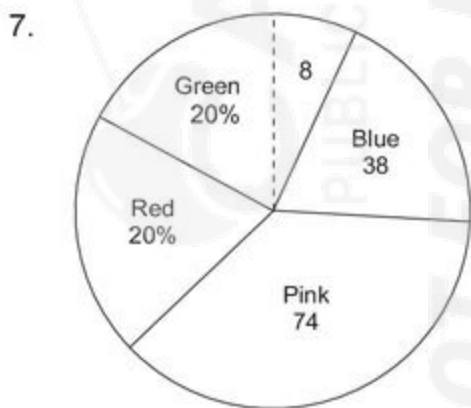
She bought 15 pears.

6. $\frac{1}{5} = 20\%$

$$\begin{aligned} \text{Percentage of blue beads} &= 100\% - 40\% - 25\% - 20\% \\ &= 15\% \end{aligned}$$

$$\begin{aligned} \text{Number of blue beads} &= \frac{15}{100} \times 80 \\ &= 12 \end{aligned}$$

There are 12 blue beads.



$$100\% - 20\% - 20\% = 60\%$$

$$\begin{aligned} 60\% &\rightarrow 8 + 38 + 74 = 120 \text{ scarves} \\ 1\% &\rightarrow 120 \div 60 = 2 \text{ scarves} \\ 100\% &\rightarrow 100 \times 2 = 200 \text{ scarves} \end{aligned}$$

She sold 200 scarves altogether that day.

Unit 10 Volume of Solids and Liquids

Drills

Exercise 1

1. 1764 cm ³	→	8 cm by 7 cm by 3 cm	(H)
2. 216 cm ³	→	9 cm by 5 cm by 4 cm	(E)
3. 1144 cm ³	→	6 cm by 6 cm by 6 cm	(C)
4. 168 cm ³	→	13 cm by 11 cm by 8 cm	(V)
5. 729 cm ³	→	18 cm by 14 cm by 7 cm	(I)
6. 3360 cm ³	→	20 cm by 12 cm by 14 cm	(A)
7. 180 cm ³	→	9 cm by 9 cm by 9 cm	(I)

A C H I E V E I
 3360 216 168 1764 180 1144 180 729

Exercise 2

No.	Length	Breadth	Base Area	Height	Volume
1.			65 cm ²	3 cm	195 cm ³
2.	12 cm	11 cm		4 cm	528 cm ³
3.	14 cm	9 cm		7 cm	882 cm ³
4.	8 cm	7 cm		5 cm	280 cm ³
5.			192 cm ²	6 cm	1152 cm ³
6.	21 cm	12 cm		15 cm	3780 cm ³
7.			184 cm ²	9 cm	1656 cm ³
8.			156 cm ²	8 cm	1248 cm ³
9.			102 cm ²	4 cm	408 cm ³
10.	17 cm	13 cm		8 cm	1768 cm ³

Perform

Exercise 1

1. (4)

$$11 \times 19 = 209 \text{ cm}^2$$

Breadth

$$\begin{aligned} &= 2926 \text{ cm}^3 \div 209 \text{ cm}^2 \\ &= \underline{14 \text{ cm}} \end{aligned}$$

2. (1)

Height

$$\begin{aligned} &= 224 \text{ cm}^3 \div 56 \text{ cm}^2 \\ &= \underline{4 \text{ cm}} \end{aligned}$$

3. (1)

$$25 \times 8 = 200 \text{ cm}^2$$

Height

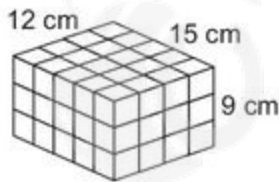
$$\begin{aligned} &= 3200 \text{ cm}^3 \div 200 \text{ cm}^2 \\ &= \underline{16 \text{ cm}} \end{aligned}$$

4. (2)

Length of side

$$\begin{aligned} &= \sqrt[3]{2197} \\ &= \underline{13 \text{ cm}} \end{aligned}$$

5. (3)



Number of cubes along its length

$$\begin{aligned} &= 15 \text{ cm} \div 3 \text{ cm} \\ &= 5 \end{aligned}$$

Number of cubes along its breadth

$$\begin{aligned} &= 12 \text{ cm} \div 3 \text{ cm} \\ &= 4 \end{aligned}$$

Number of cubes along its height

$$\begin{aligned} &= 9 \text{ cm} \div 3 \text{ cm} \\ &= 3 \end{aligned}$$

Number of cubes needed

$$\begin{aligned} &= 5 \times 4 \times 3 \\ &= \underline{60} \end{aligned}$$

6. (3)

Number of cubes along its length

$$\begin{aligned} &= 18 \text{ cm} \div 2 \text{ cm} \\ &= 9 \end{aligned}$$

Number of cubes along its breadth

$$\begin{aligned} &= 18 \text{ cm} \div 2 \text{ cm} \\ &= 9 \end{aligned}$$

Number of cubes along its height

$$\begin{aligned} &= 12 \text{ cm} \div 2 \text{ cm} \\ &= 6 \end{aligned}$$

Number of cubes needed

$$\begin{aligned} &= 9 \times 9 \times 6 \\ &= \underline{486} \end{aligned}$$

7. (2)

Breadth

$$\begin{aligned} &= \frac{1}{3} \times 18 \text{ cm} \\ &= 6 \text{ cm} \end{aligned}$$

Area of base

$$\begin{aligned} &= 18 \times 6 \\ &= 108 \text{ cm}^2 \end{aligned}$$

Height

$$\begin{aligned} &= 756 \text{ cm}^3 \div 108 \text{ cm}^2 \\ &= \underline{7 \text{ cm}} \end{aligned}$$

8. (1)

$$\frac{1}{3} \rightarrow 530 \text{ l}$$

$$1 = \frac{3}{3} \rightarrow 3 \times 530 \text{ l} = 1590 \text{ l}$$

$$\frac{1}{2} \rightarrow 1590 \text{ l} \div 2 = 795 \text{ l}$$

$$= \underline{795\,000 \text{ cm}^3}$$

Exercise 2

1. Breadth = $\frac{1}{4} \times 24$ cm
= 6 cm

Area of base
= 24×6
= 144 cm²

Height
= 1152 cm³ \div 144 cm²
= 8 cm

2. Area of base
= 13×9
= 117 cm²

Height
= 585 cm³ \div 117 cm²
= 5 cm

3. $12 \times 9 = 108$ cm²

Length
= 1620 cm³ \div 108 cm²
= 15 cm

4. Area of rectangle
= 10×5
= 50 cm²

Area of square
= 2×50
= 100 cm²

Length of square
= $\sqrt{100}$
= 10 cm

5. Area of each square tile
= 10×10
= 100 cm²

Height of 40 tiles
= 2000 cm³ \div 100 cm²
= 20 cm

Thickness of each tile
= 20 cm \div 40
= 0.5 cm

6. Length of square face
= 20 cm \div 4
= 5 cm

Area of square face
= 5×5
= 25 cm²

Length of cuboid
= 525 cm³ \div 25 cm²
= 21 cm

$\therefore p = 21$

7. Length of cube
= $\sqrt[3]{512}$
= 8 cm

Perimeter of shaded face
= 4×8 cm
= 32 cm

8. Area of base
= 540 cm³ \div 15 cm
= 36 cm²

Length of square base
= $\sqrt{36}$
= 6 cm

9. Area of base
= 15×10
= 150 cm²

Height of water level
= 1800 cm³ \div 150 cm²
= 12 cm

10. Volume of water
= $\frac{3}{5} \times (40 \times 30 \times 25)$
= $\frac{3}{5} \times 30\,000$
= 18 000 cm³

$$11. 9 l = 9000 \text{ cm}^3$$

$$\begin{aligned} \text{Base area} \\ &= 30 \times 15 \\ &= 450 \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} \text{Height of water level} \\ &= 9000 \text{ cm}^3 \div 450 \text{ cm}^2 \\ &= 20 \text{ cm} \end{aligned}$$

Exercise 3

$$1. 1 - \frac{1}{3} = \frac{2}{3}$$

$$\frac{2}{3} \longrightarrow 1536 \text{ cm}^3$$

$$\frac{1}{3} \longrightarrow 1536 \text{ cm}^3 \div 2 = 768 \text{ cm}^3$$

$$\frac{3}{3} \longrightarrow 3 \times 768 \text{ cm}^3 = 2304 \text{ cm}^3$$

$$\begin{aligned} \text{Height of tank} \\ &= 2304 \text{ cm}^3 \div 256 \text{ cm}^2 \\ &= 9 \text{ cm} \end{aligned}$$

$$\begin{aligned} 2. \text{ Volume of each 4-cm cube} \\ &= 4 \times 4 \times 4 \\ &= 64 \text{ cm}^3 \end{aligned}$$

$$\begin{aligned} \text{Volume of large cubic box} \\ &= 32 \times 64 \text{ cm}^3 \\ &= 2048 \text{ cm}^3 \end{aligned}$$

$$\begin{aligned} \text{Volume of each 2-cm cube} \\ &= 2 \times 2 \times 2 \\ &= 8 \text{ cm}^3 \end{aligned}$$

$$\begin{aligned} \text{Number of 2-cm cubes used} \\ &= 2048 \text{ cm}^3 \div 8 \text{ cm}^3 \\ &= 256 \end{aligned}$$

$$\begin{aligned} 3. \frac{1}{2} - \frac{1}{3} &= \frac{3}{6} - \frac{2}{6} \\ &= \frac{1}{6} \end{aligned}$$

$$\frac{1}{6} \longrightarrow 612 \text{ cm}^3$$

$$\frac{6}{6} \longrightarrow 6 \times 612 \text{ cm}^3 = 3672 \text{ cm}^3$$

$$\begin{aligned} \text{Height of tank} \\ &= 3672 \text{ cm}^3 \div 204 \text{ cm}^2 \\ &= 18 \text{ cm} \end{aligned}$$

$$\begin{aligned} 4. \text{ Volume of water in tank} \\ &= \frac{1}{2} \times (48 \times 15 \times 12) \\ &= \frac{1}{2} \times 8640 \\ &= 4320 \text{ cm}^3 \end{aligned}$$

$$\begin{aligned} \text{Volume of water in each smaller tank} \\ &= 4320 \text{ cm}^3 \div 3 \\ &= 1440 \text{ cm}^3 \end{aligned}$$

$$\begin{aligned} \text{Base area of smaller tank} \\ &= 24 \times 12 \\ &= 288 \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} \text{Height of water in smaller tank} \\ &= 1440 \text{ cm}^3 \div 288 \text{ cm}^2 \\ &= 5 \text{ cm} \end{aligned}$$

$$\begin{aligned} 5. \text{ Volume of water in tank at first} \\ &= 15 \times 6 \times 7 \\ &= 630 \text{ cm}^3 \end{aligned}$$

$$\frac{1}{3} \longrightarrow 630 \text{ cm}^3 - 30 \text{ cm}^3 = 600 \text{ cm}^3$$

$$\frac{3}{3} \longrightarrow 3 \times 600 \text{ cm}^3 = 1800 \text{ cm}^3$$

The capacity of the container is 1800 cm^3 .

6. Volume of water in Tank A

$$= \frac{1}{3} \times (60 \times 45 \times 60)$$

$$= \frac{1}{3} \times 162\,000$$

$$= 54\,000 \text{ cm}^3$$

Base area of Tank B

$$= 80 \times 50$$

$$= 4000 \text{ cm}^2$$

Height of water level in Tank B

$$= 54\,000 \text{ cm}^3 \div 4000 \text{ cm}^2$$

$$= 13.5 \text{ cm}$$

The height of the water level in Tank B is 13.5 cm.

7. Number of cubes in container now

$$= 12 + 4 + 2 + 2$$

$$= 20$$

Number of cubes that lie along the length = 8

Number of cubes that lie along the breadth = 4

Number of cubes that lie along the height = 4

Number of cubes that container can hold

$$= 8 \times 4 \times 4$$

$$= 128$$

$$128 - 20 = 108$$

108 more 1-cm cubes are needed to completely fill the container.

Achieve

Exercise 1

1. (a) $3 \text{ l} = 3000 \text{ cm}^3$

Volume of water in tank (15 cm high)

$$= 60 \times 40 \times 15$$

$$= 36\,000 \text{ cm}^3$$

$$3000 \text{ cm}^3 \longrightarrow 1 \text{ min}$$

$$1 \text{ cm}^3 \longrightarrow \frac{1}{3000} \text{ min}$$

$$36\,000 \text{ cm}^3 \longrightarrow 36\,000 \times \frac{1}{3000} \text{ min}$$
$$= 12 \text{ min}$$

It will take 12 minutes to fill the tank to a height of 15 cm.

(b) $12 \text{ min} + 20 \text{ min} = 32 \text{ min}$

$$1 \text{ min} \longrightarrow 3000 \text{ cm}^3$$

$$32 \text{ min} \longrightarrow 32 \times 3000 \text{ cm}^3$$
$$= 96\,000 \text{ cm}^3$$

Base area of tank

$$= 60 \times 40$$

$$= 2400 \text{ cm}^2$$

Height of tank

$$= 96\,000 \text{ cm}^3 \div 2400 \text{ cm}^2$$

$$= 40 \text{ cm}$$

The height of the tank is 40 cm.

2. $2 \text{ l} + 5 \text{ l} = 7 \text{ l}$

Both taps can fill the tank at 7 l/min.

$$1 \text{ min} \longrightarrow 7 \text{ l}$$

$$4 \text{ min} \longrightarrow 4 \times 7 \text{ l} = 28 \text{ l}$$

The capacity of the tank is 28 l.

$$\begin{aligned}
 5 \text{ l} &\longrightarrow 1 \text{ min} \\
 1 \text{ l} &\longrightarrow \frac{1}{5} \text{ min} \\
 28 \text{ l} &\longrightarrow 28 \times \frac{1}{5} \text{ min} = 5.6 \text{ min}
 \end{aligned}$$

Tap B will take **5.6 min** to fill up the empty tank on its own.

3. (a) 64 units – 1 unit = 63 units

$$\begin{aligned}
 63 \text{ units} &= 504 \text{ cm}^3 \\
 1 \text{ unit} &= 504 \text{ cm}^3 \div 63 \\
 &= 8 \text{ cm}^3
 \end{aligned}$$

The volume of the smaller cube is **8 cm³**.

- (b) 64 units = $64 \times 8 \text{ cm}^3$
= 512 cm³

The volume of the larger cube is 512 cm³.

$$\begin{aligned}
 \text{Length of each side of larger cube} \\
 &= \sqrt[3]{512} \\
 &= 8 \text{ cm}
 \end{aligned}$$

The length of each side of the larger cube is **8 cm**.

4. (a) Area of square base
= 20×20
= 400 cm²

$$\begin{aligned}
 \frac{3}{4} &\longrightarrow 9.6 \text{ l} \\
 \frac{1}{4} &\longrightarrow 9.6 \text{ l} \div 3 = 3.2 \text{ l} \\
 \frac{4}{4} &\longrightarrow 4 \times 3.2 \text{ l} = 12.8 \text{ l} \\
 &= 12\,800 \text{ cm}^3
 \end{aligned}$$

$$\begin{aligned}
 \text{Height of tank} \\
 &= 12\,800 \text{ cm}^3 \div 400 \text{ cm}^2 \\
 &= 32 \text{ cm}
 \end{aligned}$$

The height of the tank is **32 cm**.

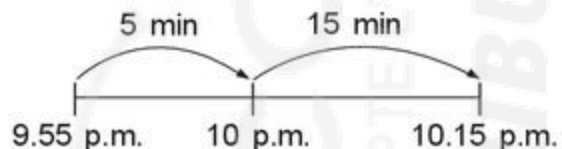
- (b) Volume of water when $\frac{3}{8}$ full
= $\frac{3}{8} \times 12\,800 \text{ cm}^3$
= 4800 cm³

$$\begin{aligned}
 8 \text{ l} &= 4800 \text{ cm}^3 \\
 &= 8000 \text{ cm}^3 - 4800 \text{ cm}^3 \\
 &= 3200 \text{ cm}^3
 \end{aligned}$$

$$160 \text{ cm}^3 \longrightarrow 1 \text{ min}$$

$$1 \text{ cm}^3 \longrightarrow \frac{1}{160} \text{ min}$$

$$\begin{aligned}
 3200 \text{ cm}^3 &\longrightarrow 3200 \times \frac{1}{160} \text{ min} \\
 &= 20 \text{ min}
 \end{aligned}$$



$$10.15 \text{ p.m.} = 22\,15$$

The tank will be $\frac{3}{8}$ full at **22 15**.

5. (a) Volume of water in tank at first

$$\begin{aligned}
 &= \frac{1}{2} \times (40 \times 30 \times 50) \\
 &= \frac{1}{2} \times 60\,000 \\
 &= 30\,000 \text{ cm}^3 \\
 1\frac{1}{4} \text{ h} &= 75 \text{ min}
 \end{aligned}$$

$$\begin{aligned}
 1 \text{ min} &\longrightarrow 120 \text{ cm}^3 \\
 75 \text{ min} &\longrightarrow 75 \times 120 \text{ cm}^3 \\
 &= 9000 \text{ cm}^3
 \end{aligned}$$

$$\begin{aligned}
 30\,000 \text{ cm}^3 &- 9000 \text{ cm}^3 \\
 &= 21\,000 \text{ cm}^3
 \end{aligned}$$

21 000 cm³ of water was left in the tank.

(b) Base area of tank
 $= 40 \times 30$
 $= 1200 \text{ cm}^2$

Height of new water level
 $= 21\,000 \text{ cm}^3 \div 1200 \text{ cm}^2$
 $= 17.5 \text{ cm}$

The height of the new water level is **17.5 cm**.

6. $1 - \frac{3}{5} = \frac{2}{5}$

Height of water level in Container B
 $= 10 \text{ cm} \div 2$
 $= 5 \text{ cm}$

Volume of water transferred to Container A

$$= \frac{2}{5} \times (25 \times 15 \times 5)$$

$$= \frac{2}{5} \times 1875$$

$$= 750 \text{ cm}^3$$

$$= 0.75 \text{ l}$$

$$2 \text{ l} - 0.75 \text{ l} = 1.25 \text{ l}$$

The original volume of water in Container A was **1.25 l**.

7. (a) Length of square base
 $= \sqrt{9}$
 $= 3 \text{ cm}$

$$\frac{2}{5} \text{ m} = \frac{2}{5} \times 100 \text{ cm}$$

$$= 40 \text{ cm}$$

$$40 \text{ cm} \div 2 \text{ cm} = 20 \text{ (Height)}$$

$$3 \text{ cm} \div 2 \text{ cm} = 1 \text{ R } 1 \text{ cm (Breadth)}$$

$$3 \text{ cm} \div 2 \text{ cm} = 1 \text{ R } 1 \text{ cm (Length)}$$

Number of cubes
 $= 1 \times 1 \times 20$
 $= 20$

The greatest number of 2-cm cubes that can be cut is **20**.

(b) Volume of wood at first
 $= 9 \text{ cm}^2 \times 40 \text{ cm}$
 $= 360 \text{ cm}^3$

Volume of each 2-cm cube
 $= 2 \times 2 \times 2$
 $= 8 \text{ cm}^3$

Volume of wood used
 $= 20 \times 8 \text{ cm}^3$
 $= 160 \text{ cm}^3$

$$360 \text{ cm}^3 - 160 \text{ cm}^3 = 200 \text{ cm}^3$$

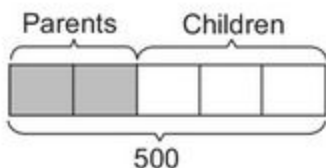
200 cm³ of the block of wood is left.

Challenging Problems

1. Number of people

$$= \frac{4}{10} \times 1250$$

$$= 500$$



$$5 \text{ units} = 500 \text{ people}$$

$$1 \text{ unit} = 500 \div 5$$

$$= 100 \text{ people}$$

$$2 \text{ units} = 2 \times 100$$

$$= 200 \text{ people (Parents)}$$

$$3 \text{ units} = 3 \times 100$$

$$= 300 \text{ people (Children)}$$

$$\text{Total amount collected}$$

$$= (200 \times \$6) + (300 \times \$3)$$

$$= \$1200 + \$900$$

$$= \$2100$$

The total amount of money collected during that concert was **\$2100**.

2. $\frac{\text{Length}}{8} : \frac{\text{Breadth}}{4}$

$$8 \text{ units} + 4 \text{ units} = 12 \text{ units}$$

$$12 \text{ units} = 24 \text{ m}$$

$$1 \text{ unit} = 24 \text{ m} \div 12$$

$$= 2 \text{ m}$$

$$8 \text{ units} = 8 \times 2 \text{ m}$$

$$= 16 \text{ m (Length)}$$

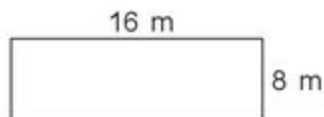
$$4 \text{ units} = 4 \times 2 \text{ m}$$

$$= 8 \text{ m (Breadth)}$$

$$\text{Area of rectangular garden}$$

$$= 16 \times 8$$

$$= 128 \text{ m}^2$$



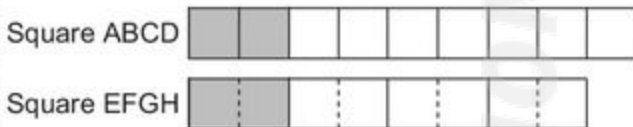
Area of flower bed

$$= \frac{25}{100} \times 128 \text{ m}^2$$

$$= 32 \text{ m}^2$$

The area of the flower bed is **32 m²**.

3. (a) $1 - \frac{3}{4} = \frac{1}{4}$
 $\frac{1}{4}$ of Square EFGH is shaded.



$$\frac{\text{Area X}}{7} : \frac{\text{Area Y}}{2} : \frac{\text{Area Z}}{6}$$

The required ratio is **7 : 2 : 6**.

- (b) Area of Square ABCD
 $= 12 \times 12$
 $= 144 \text{ cm}^2$

$$\text{Area of Y}$$

$$= \frac{2}{9} \times 144 \text{ cm}^2$$

$$= 32 \text{ cm}^2$$

$$\frac{1}{4} \rightarrow 32 \text{ cm}^2$$

$$\frac{3}{4} \rightarrow 3 \times 32 \text{ cm}^2 = 96 \text{ cm}^2$$

The area of the unshaded part of Square EFGH is **96 cm²**.

4. $\frac{\text{Raymond}}{7\frac{1}{2}} : \frac{\text{Mary}}{5} : \frac{\text{Paul}}{3} : \frac{\text{Jimmy}}{2}$

$$= 15 : 10 : 6 : 4$$

$$15 \text{ units} + 10 \text{ units} + 6 \text{ units} + 4 \text{ units}$$

$$= 35 \text{ units}$$

$$35 \text{ units} = 1400 \text{ stickers}$$

$$1 \text{ unit} = 1400 \div 35 \\ = 40 \text{ stickers}$$

$$35 \text{ units} - 10 \text{ units} = 25 \text{ units}$$

$$25 \text{ units} = 25 \times 40 \\ = 1000 \text{ stickers}$$

The boy's received **1000** stickers altogether.

5. Capacity of tank
 $= 50 \times 40 \times 8$
 $= 16\,000 \text{ cm}^3$

$$\frac{\text{Tank}}{24} : \frac{\text{Pail}}{1}$$

$$1 \text{ unit} = 500 \text{ cm}^3 \\ 24 \text{ units} = 24 \times 500 \text{ cm}^3 \\ = 12\,000 \text{ cm}^3$$

Amount of water required to fill the tank to its brim
 $= 16\,000 \text{ cm}^3 - 12\,000 \text{ cm}^3$
 $= 4000 \text{ cm}^3$

$$\text{Number of pails of water} \\ = 4000 \text{ cm}^3 \div 500 \text{ cm}^3 \\ = 8$$

8 pails full of water were needed to fill the tank to its brim.

6. (a) $\frac{\text{Men}}{3} : \frac{\text{Women}}{4}$

$$3 \text{ units} + 4 \text{ units} = 7 \text{ units}$$

$$7 \text{ units} = 350 \text{ seats} \\ 1 \text{ unit} = 350 \div 7 \\ = 50 \text{ seats}$$

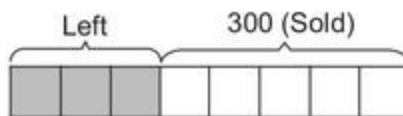
$$4 \text{ units} = 4 \times 50 \\ = 200 \text{ seats}$$

200 seats are solely reserved for women before the renovation.

(b) $\frac{120}{100} \times 350 = 420$

The number of seats reserved for adults after the renovation is **420**.

7.



$$5 \text{ units} = 300 \text{ pens} \\ 1 \text{ unit} = 300 \div 5 \\ = 60 \text{ pens} \\ 3 \text{ units} = 3 \times 60 \\ = 180 \text{ pens}$$

$$\text{Number of pens sold on Sunday} \\ = \frac{25}{100} \times 180 \\ = 45$$

$$\text{Number of pens sold on Monday} \\ = 180 - 45 \\ = 135$$

$$\text{Amount collected on Sunday} \\ = \$1200 - (300 \times \$2.50) - (135 \times \$3) \\ = \$1200 - \$750 - \$405 \\ = \$45$$

$$\$45 \div 45 = \$1$$

The sale price of each pen on Sunday was \$1.

8. (a) $25\% - 12\% = 13\%$
13% of the children prefer mangoes.

(b) $50\% - 12\% = 38\%$
 Fraction of children who prefer apples
 $= \frac{38}{100}$
 $= \frac{19}{50}$

$\frac{19}{50}$ of the children surveyed prefer apples.

- (c) $50\% - 13\% - 25\% = 12\%$
 12% of the children prefer strawberries.

$$25\% - 12\% = 13\%$$

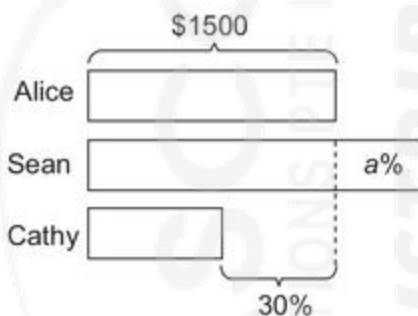
$$\frac{13}{100} \times 5000 = 650$$

650 more children prefer oranges to strawberries.

- (d) Mangoes : Apples
 13% : 38%
 = 13 : 38

The ratio of the number of children who prefer mangoes to apples is **13 : 38**.

9.



$$a\% \text{ of } \$1500 = \frac{a}{100} \times \$1500$$

$$= \$15a$$

$$\text{Amount Sean earned} = \$1500 + \$15a$$

$$\text{Amount Cathy earned} = \frac{70}{100} \times \$1500$$

$$= \$1050$$

$$\text{Total amount} = \$1500 + \$1500 + \$15a + \$1050$$

$$= \$4050 + \$15a$$

$$= \$(4050 + 15a)$$

The total amount of money earned by Alice, Cathy and Sean is **\\$(4050 + 15a)**.

10. (a) Area of triangle
 $= \frac{1}{2} \times 9 \times 12$
 $= 54 \text{ cm}^2$

$$\text{Area of small semicircle} = \frac{1}{2} \times 3.14 \times 3 \times 3$$

$$= 14.13 \text{ cm}^2$$

$$\text{Shaded area of triangle} = 54 - 14.13$$

$$= 39.87 \text{ cm}^2$$

The shaded area of the right-angled triangle is **39.87 cm²**.

- (b) Curved part of small semicircle
 $= \frac{1}{2} \times 3.14 \times 6$
 $= 9.42 \text{ cm}$

$$\text{Perimeter of shaded part} = 9.42 + (15 - 6) + 9 + 12$$

$$= 9.42 + 9 + 9 + 12$$

$$= 39.42 \text{ cm}$$

The perimeter of the shaded part of the figure is **39.42 cm**.

11. Angela : Jason
 $\times 7 \left(\begin{array}{l} 5 \\ 35 \end{array} : \begin{array}{l} 6 \\ 42 \end{array} \right) \times 7$

Jason:

$$\frac{2}{7} \times 42 \text{ units} = 12 \text{ units (given to Angela)}$$

$$\frac{5}{14} \times 42 \text{ units} = 15 \text{ units (spent on food)}$$

$$42 \text{ units} - 12 \text{ units} - 15 \text{ units} = 15 \text{ units}$$

$$15 \text{ units} = \$360$$

$$1 \text{ unit} = \$360 \div 15$$

$$= \$24$$

$$35 \text{ units} = 35 \times \$24$$

$$= \$840$$

$$\frac{123}{100} \times \$840 = \$1033.20$$

Ben had **\$1033.20**.

12. Perimeter of running track

$$\begin{aligned} &= \left(\frac{22}{7} \times 21\right) + 300 + 300 \\ &= 66 + 300 + 300 \\ &= 666 \text{ m} \end{aligned}$$

$$2 \times 666 \text{ m} = 1332 \text{ m}$$

$$180 \text{ m} \longrightarrow 1 \text{ min}$$

$$1 \text{ m} \longrightarrow \left(\frac{1}{180}\right) \text{ min}$$

$$1332 \text{ m} \longrightarrow 1332 \times \frac{1}{180} = 7.4 \text{ min}$$

She took 7.4 min to jog the whole distance.

13. Area of $\triangle PTS$

$$\begin{aligned} &= \frac{1}{2} \times 7 \times 7 \\ &= 24.5 \text{ cm}^2 \end{aligned}$$

Area of quadrant QSR

$$\begin{aligned} &= \frac{1}{4} \times \frac{22}{7} \times 7 \times 7 \\ &= 38.5 \text{ cm}^2 \end{aligned}$$

Area of semicircle

$$\begin{aligned} &= \frac{1}{2} \times \frac{22}{7} \times 3.5 \times 3.5 \\ &= 19.25 \text{ cm}^2 \end{aligned}$$

Total area of shaded parts

$$\begin{aligned} &= 24.5 + 38.5 + 19.25 \\ &= 82.25 \text{ cm}^2 \end{aligned}$$

The total area of the shaded parts is 82.25 cm^2 .

14. $\frac{\text{Tank A}}{5} : \frac{\text{Tank B}}{2}$

$$5 : 2$$

$$5 \text{ units} - 2 \text{ units} = 3 \text{ units}$$

$$3 \text{ units} = 4500 \text{ cm}^3$$

$$\begin{aligned} 1 \text{ unit} &= 4500 \text{ cm}^3 \div 3 \\ &= 1500 \text{ cm}^3 \end{aligned}$$

$$\begin{aligned} 5 \text{ units} &= 5 \times 1500 \text{ cm}^3 \\ &= 7500 \text{ cm}^3 \text{ (Tank A)} \end{aligned}$$

$$\begin{aligned} 2 \text{ units} &= 2 \times 1500 \text{ cm}^3 \\ &= 3000 \text{ cm}^3 \text{ (Tank B)} \end{aligned}$$

Base area of each tank

$$\begin{aligned} &= 50 \times 30 \\ &= 1500 \text{ cm}^2 \end{aligned}$$

Height of water level of Tank A

$$\begin{aligned} &= 7500 \text{ cm}^3 \div 1500 \text{ cm}^2 \\ &= 5 \text{ cm} \end{aligned}$$

Height of water level of Tank B

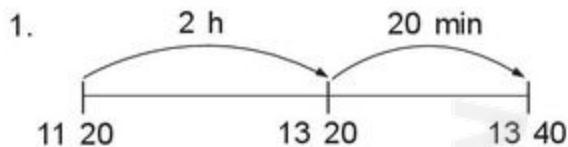
$$\begin{aligned} &= 3000 \text{ cm}^3 \div 1500 \text{ cm}^2 \\ &= 2 \text{ cm} \end{aligned}$$

$$5 \text{ cm} - 2 \text{ cm} = 3 \text{ cm}$$

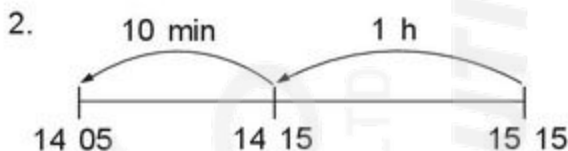
The difference in the heights of the water levels of Tank A and Tank B is 3 cm.

Revision of P4 and P5 Topics

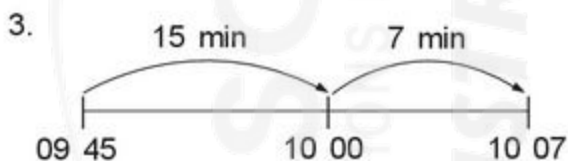
Exercise 1



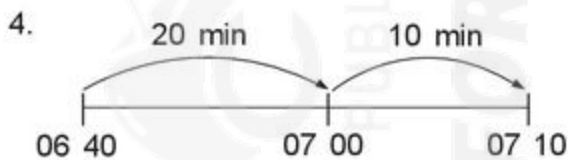
The movie was **2 h 20 min** long.



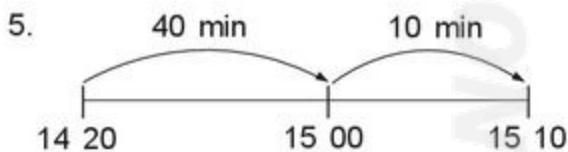
He started doing his homework at **14 05**.



He arrived at Little India station at **10 07**.



Joyce took **30 min** to travel to school.

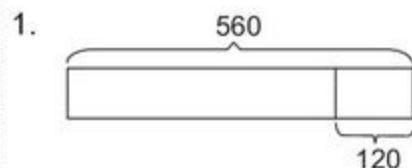


She finished baking at **15 10**.



Janet reached home at **15 25**.

Exercise 2



$$560 - 120 = 440$$

Thomas had **440** stamps in the end.

$$440 - 26 = 414$$

Sam had **414** stamps in the end.

$$414 - 120 = 294$$

Sam had **294** stamps at first.

2. $1 - \frac{3}{4} = \frac{1}{4}$

$$\frac{3}{5} \times \frac{3}{4} = \frac{9}{20}$$

$$\begin{aligned} \frac{1}{4} + \frac{9}{20} &= \frac{5}{20} + \frac{9}{20} \\ &= \frac{14}{20} \\ &= \frac{7}{10} \end{aligned}$$

$$\frac{7}{10} \rightarrow \$210$$

$$\frac{1}{10} \rightarrow \$210 \div 7 = \$30$$

$$\frac{10}{10} \rightarrow 10 \times \$30 = \$300$$

She had **\$300** at first.

3. Length of square

$$= \sqrt{64}$$

$$= 8 \text{ cm}$$

4. Cost of 5 T-shirts

$$= 5 \times \$5.20$$

$$= \$26$$

Cost of 7 bags

$$= \$26 + \$42$$

$$= \$68$$

$$\$68 - \$5.20 = \$62.80$$

The required difference is **\$62.80**.

5. Before:

<u>Jennifer</u>	:	<u>Gloria</u>	Total Units
7	:	5	$7 + 5 = 12$ units

After:

<u>Jennifer</u>	:	<u>Gloria</u>	Total Units
$\times 2 \left(\begin{array}{c} 1 \\ \downarrow \\ 2 \end{array} \right)$:	$\left(\begin{array}{c} 5 \\ \downarrow \\ 10 \end{array} \right) \times 2$	$2 + 10 = 12$ units
= 2	:	= 10	

$$7 \text{ units} - 2 \text{ units} = 5 \text{ units}$$

$$5 \text{ units} = 500 \text{ bracelets}$$

$$1 \text{ unit} = 500 \div 5$$

$$= 100 \text{ bracelets}$$

$$12 \text{ units} = 12 \times 100$$

$$= 1200 \text{ bracelets}$$

The total number of bracelets they made altogether was **1200**.

6. Before:

<u>Leslie</u>	:	<u>Rachel</u>	Total units
$\times 2 \left(\begin{array}{c} 5 \\ \downarrow \\ 10 \end{array} \right)$:	$\left(\begin{array}{c} 1 \\ \downarrow \\ 2 \end{array} \right) \times 2$	$10 + 2 = 12$ units
= 10	:	= 2	

After:

<u>Leslie</u>	:	<u>Rachel</u>	Total units
$\times 3 \left(\begin{array}{c} 3 \\ \downarrow \\ 9 \end{array} \right)$:	$\left(\begin{array}{c} 1 \\ \downarrow \\ 3 \end{array} \right) \times 3$	$9 + 3 = 12$ units
= 9	:	= 3	

$$10 \text{ units} - 9 \text{ units} = 1 \text{ unit}$$

$$1 \text{ unit} = 14 \text{ stickers}$$

$$2 \text{ units} = 2 \times 14$$

$$= 28 \text{ stickers}$$

Rachel had **28** stickers at first.

7. Area of big rectangle

$$= 25 \times 14$$

$$= 350 \text{ cm}^2$$

Area of small rectangle

$$= 21 \times 10$$

$$= 210 \text{ cm}^2$$

Area of shaded figure

$$= 350 - 210$$

$$= 140 \text{ cm}^2$$

8. 2 kg of lamb + 2 kg of beef \longrightarrow \$53.20

4 kg of lamb + 2 kg of beef \longrightarrow \$78.80

$$2 \text{ kg of lamb} \longrightarrow \$78.80 - \$53.20$$

$$= \$25.60$$

$$2 \text{ kg of beef} \longrightarrow \$53.20 - \$25.60$$

$$= \$27.60$$

$$1 \text{ kg of beef} = \$27.60 \div 2$$

$$= \$13.80$$

$$5 \text{ kg of beef} = 5 \times \$13.80$$

$$= \$69$$

The cost of 5 kg of beef is **\$69**.

9. Number of eggs left
 $= 989 - 53 - 768$
 $= 168$

Number of cartons
 $= 168 \div 12$
 $= 14$

He had **14** cartons of eggs.

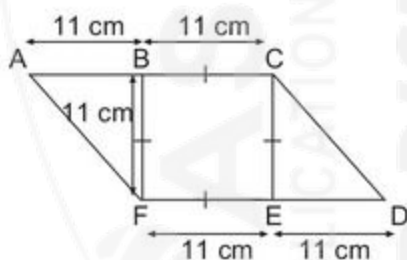
10.



13 units = 338 items
 1 unit = $338 \div 13$
 $= 26$ items
 3 units = 3×26 items
 $= 78$ items

There are **78** shirts in the store.

11.



Area of Square BCEF
 $= 11 \times 11$
 $= 121 \text{ cm}^2$

Area of figure
 $= 2 \times 121 \text{ cm}^2$
 $= 242 \text{ cm}^2$

12. $1 - \frac{3}{5} = \frac{2}{5}$

$\frac{2}{5} \times \$2400 = \960

$1 - \frac{1}{5} = \frac{4}{5}$

$\frac{4}{5} \times \$960 = \768

She saves **\$768** every month.

$12 \times \$768 = \9216

She will save **\$9216** in a year.

13. Total height of 5 children
 $= 5 \times 163 \text{ cm}$
 $= 815 \text{ cm}$

Jason's height
 $= 163 \text{ cm} + 24 \text{ cm}$
 $= 187 \text{ cm}$

Total height of 6 children
 $= 815 \text{ cm} + 187 \text{ cm}$
 $= 1002 \text{ cm}$

Average height of 6 children
 $= 1002 \text{ cm} \div 6$
 $= 167 \text{ cm}$

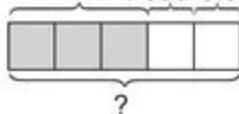
14. $185 \times \$2 = \370
 $185 \div 15 = 12 \text{ R } 5$
 $12 \times \$5 = \60

Amount he will get
 $= \$370 + \60
 $= \$430$

15. Area of floor
 $= 24 \times 20$
 $= 480 \text{ m}^2$

Cost of carpeting the floor
 $= 480 \times \$35$
 $= \$16\ 800$

16. Left Food Clothing (\$15)



$$\begin{aligned} 1 \text{ unit} &= \$15 \\ 5 \text{ units} &= 5 \times \$15 \\ &= \$75 \end{aligned}$$

He had **\$75** at first.

17. $\left. \begin{array}{l} 2 \text{ Pens } \boxed{} \boxed{} \\ 2 \text{ Pencils } \boxed{} \boxed{} \\ 1 \text{ Ruler } \boxed{} \boxed{90\text{¢}} \end{array} \right\} \3.70
- ?

$$\begin{aligned} 8 \text{ units} &= \$3.70 - \$0.90 \\ &= \$2.80 \\ 1 \text{ unit} &= \$2.80 \div 8 \\ &= \$0.35 \\ 2 \text{ units} &= 2 \times \$0.35 \\ &= \$0.70 \end{aligned}$$

$$\$0.70 + \$0.90 = \$1.60.$$

A ruler costs **\$1.60**.

18. $\left. \begin{array}{l} \text{Joe } \boxed{} \boxed{} \boxed{40} \\ \text{Susie } \boxed{} \boxed{} \\ \text{Ken } \boxed{} \end{array} \right\} 780$

$$\begin{aligned} 5 \text{ units} &= 780 - 40 \\ &= 740 \text{ stamps} \\ 1 \text{ unit} &= 740 \div 5 \\ &= 148 \text{ stamps} \\ 2 \text{ units} &= 2 \times 148 \\ &= 296 \text{ stamps} \end{aligned}$$

Susie had **296** stamps.

19. Perimeter of shaded part
= Perimeter of Rectangle ABCD
= $17 + 8 + 17 + 8$
= **50 cm**

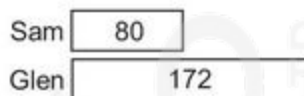
20. Greater number $\boxed{} \boxed{12}$
Smaller number $\boxed{}$ } 28
?

$$\begin{aligned} 2 \text{ units} &= 28 - 12 \\ &= 16 \\ 1 \text{ unit} &= 16 \div 2 \\ &= 8 \end{aligned}$$

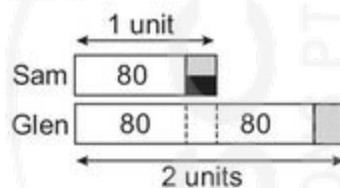
The other number is **8**.

Exercise 3

1. Before:



After:



$$172 - 80 - 80 = 12$$

Mother gave **12** stickers to each of them.

$$2 \times 12 = 24$$

Mother gave **24** stickers to both of them.

2. (a) Perimeter of Rectangle A
= $15 + 9.6 + 15 + 9.6$
= **49.2 cm**

$$\begin{aligned} \text{Perimeter of Square B} \\ &= 49.2 \text{ cm} \end{aligned}$$

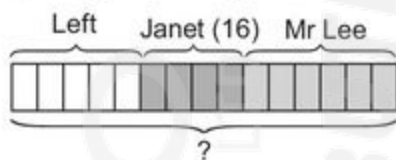
$$\begin{aligned} \text{Length of Square B} \\ &= 49.2 \text{ cm} \div 4 \\ &= \mathbf{12.3 \text{ cm}} \end{aligned}$$

(b) Area of Rectangle A
 $= 15 \times 9.6$
 $= 144 \text{ cm}^2$

Area of Square B
 $= 12.3 \times 12.3$
 $= 151.29 \text{ cm}^2$

Total area of both figures
 $= 144 + 151.29$
 $= 295.29 \text{ cm}^2$

3. (a) $\frac{2}{5} = \frac{6}{15}, \frac{1}{3} = \frac{5}{15}$



4 units = 16 pens
 1 unit = $16 \div 4$
 $= 4$ pens
 15 units = 15×4
 $= 60$ pens

Daniel had 60 pens at first.

(b) 5 units = 5×4
 $= 20$ pens
 He had 20 pens left.

$20 \div 4 = 5$

5 boxes were required to pack the remaining pens.

4. $1 - 0.15 = 0.85$

$0.85 \times 4 \text{ l} = 3.4 \text{ l}$
 $= 3400 \text{ ml}$

He had 3400 ml of orange juice left.

$3400 \text{ ml} \div 450 \text{ ml} = 7 \text{ R } 250 \text{ ml}$
 $450 \text{ ml} - 250 \text{ ml} = 200 \text{ ml}$

200 ml more orange juice is needed to fill the last bottle completely.

5. Before :

Dennis	84
Benjamin	132

After :

Dennis	
Benjamin	$\underbrace{\quad \quad \quad}_{132}$

3 units = 132 stamps
 1 unit = $132 \div 3$
 $= 44$ stamps

Dennis had 44 stamps in the end.

$84 - 44 = 40$
 Dennis gave away 40 stamps.

6. Before:

Men : Women
 $\times 3 \left(\begin{array}{l} 1 : 2 \\ \downarrow \quad \uparrow \\ 3 : 6 \end{array} \right) \times 3$
 $= 3 : 6$

After:

Men : Women
 $\times 2 \left(\begin{array}{l} 1 : 3 \\ \downarrow \quad \uparrow \\ 2 : 6 \end{array} \right) \times 2$
 $= 2 : 6$

3 units - 2 units = 1 unit

1 unit = 20 people
 6 units = 6×20
 $= 120$ people

There were 120 women in the concert hall at first.

7. Length of cloth used to sew a pair of shorts

$= \frac{3}{5} \times 2.5 \text{ m}$
 $= 1.5 \text{ m}$

$$\begin{aligned} \text{Length of cloth used to sew 6 shirts} \\ &= 6 \times 2.5 \text{ m} \\ &= 15 \text{ m} \end{aligned}$$

$$\begin{aligned} \text{Length of cloth used to sew the shorts} \\ &= 28.5 \text{ m} - 15 \text{ m} - 1.5 \text{ m} \\ &= 12 \text{ m} \end{aligned}$$

$$\begin{aligned} \text{Number of pairs of shorts} \\ &= 12 \text{ m} \div 1.5 \text{ m} \\ &= 8 \end{aligned}$$

She sewed 8 pairs of shorts.

8. Area of $\triangle ACF$

$$\begin{aligned} &= \frac{1}{2} \times 12 \times 5 \\ &= 30 \text{ cm}^2 \end{aligned}$$

Area of $\triangle ACF$: Area of Rectangle ABDE

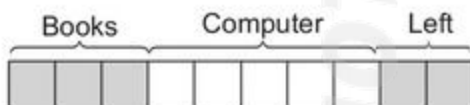
$$\begin{array}{ccc} 1 & : & 4 \\ 1 \text{ unit} & = & 30 \text{ cm}^2 \\ 4 \text{ units} & = & 4 \times 30 \text{ cm}^2 \\ & & = 120 \text{ cm}^2 \end{array}$$

The area of Rectangle ABDE is 120 cm^2 .

$$\begin{aligned} \text{Breadth of rectangle} \\ &= 120 \text{ cm}^2 \div 12 \\ &= 10 \text{ cm} \end{aligned}$$

$$\begin{aligned} \text{Perimeter of Rectangle ABDE} \\ &= 12 + 10 + 12 + 10 \\ &= 44 \text{ cm} \end{aligned}$$

9. (a) $0.3 = \frac{3}{10}$, $\frac{1}{5} = \frac{2}{10}$



$$\begin{aligned} 5 \text{ units} &= \$1400 \\ 1 \text{ unit} &= \$1400 \div 5 \\ &= \$280 \\ 8 \text{ units} &= 8 \times \$280 \\ &= \$2240 \end{aligned}$$

She spent **\$2240** altogether.

(b) $10 \text{ units} = 10 \times \280
 $= \$2800$

Her original sum of money was **\$2800**.

10. Mass of marshmallows
 $= 13 \times 5 \text{ kg}$
 $= 65 \text{ kg}$

$$\begin{aligned} \text{Total mass of candies and marshmallows} \\ &= 37.8 \text{ kg} + 65 \text{ kg} \\ &= 102.8 \text{ kg} \end{aligned}$$

$$\begin{aligned} \text{Mass of each packet} \\ &= 102.8 \text{ kg} \div 20 \\ &= 5.14 \text{ kg} \end{aligned}$$

The mass of each packet that he had repacked **5.14 kg**.

11. (a) Area of $\triangle F$

$$\begin{aligned} &= \frac{1}{2} \times 3 \times 10 \\ &= 15 \text{ cm}^2 \end{aligned}$$

Area of $\triangle F$: Shaded triangle

$$1 : 5$$

$$\begin{aligned} 1 \text{ unit} &= 15 \text{ cm}^2 \\ 5 \text{ units} &= 5 \times 15 \text{ cm}^2 \\ &= 75 \text{ cm}^2 \end{aligned}$$

The area of the shaded triangle is 75 cm^2 .

(b) Area of $\triangle F$: Area of $\triangle G$

$$1 : 4$$

$$\begin{aligned} 4 \text{ units} &= 4 \times 15 \text{ cm}^2 \\ &= 60 \text{ cm}^2 \end{aligned}$$

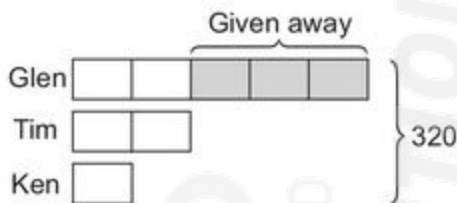
$$\begin{aligned} \text{Area of Rectangle ABCD} \\ &= 15 + 75 + 60 \\ &= 150 \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} \text{Length of Rectangle ABCD} &= 150 \text{ cm}^2 \div 10 \text{ cm} \\ &= 15 \text{ cm} \end{aligned}$$

$$\begin{aligned} \text{Perimeter of Rectangle ABCD} &= 15 + 10 + 15 + 10 \\ &= 50 \text{ cm} \end{aligned}$$

The perimeter of Rectangle ABCD is **50 cm**.

12.



$$\begin{aligned} 8 \text{ units} &= 320 \text{ game cards} \\ 1 \text{ unit} &= 320 \div 8 \\ &= 40 \text{ game cards} \\ 3 \text{ units} &= 3 \times 40 \\ &= 120 \text{ game cards} \end{aligned}$$

Glen gave away **120** game cards.

Trial Examination 1

PAPER 1

Booklet A:

1. (3)

When $a = 5$,

$$\begin{aligned} \frac{3a + 6}{7} &= \frac{3(5) + 6}{7} \\ &= \frac{15 + 6}{7} \\ &= \frac{21}{7} \\ &= \underline{3} \end{aligned}$$

2. (1)

It has 6 rectangular faces.

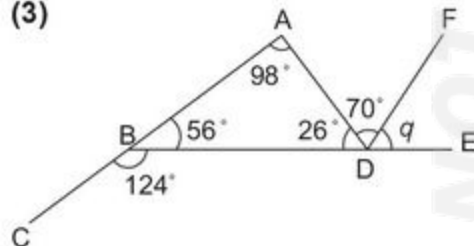
3. (3)

$$\begin{aligned} 48 \text{ min} &= \frac{48}{60} \text{ h} \\ &= \frac{4}{5} \text{ h} \end{aligned}$$

Average speed

$$\begin{aligned} &= 6.4 \text{ km} \div \frac{4}{5} \text{ h} \\ &= 6 \frac{2}{5} \text{ km} \div \frac{4}{5} \text{ h} \\ &= \frac{32}{5} \text{ km} \times \frac{5^1}{4^1} \text{ h} \\ &= \underline{8 \text{ km/h}} \end{aligned}$$

4. (3)



$$\begin{aligned} \angle ABD &= 180^\circ - 124^\circ \text{ (}\angle\text{s on a straight line)} \\ &= 56^\circ \end{aligned}$$

$$\begin{aligned} \angle ADB &= 180^\circ - 98^\circ - 56^\circ \text{ (}\angle\text{sum of } \triangle) \\ &= 26^\circ \end{aligned}$$

$$\angle q = 180^\circ - 70^\circ - 26^\circ \text{ (\(\angle\)'s on a straight line)}$$

$$= \underline{84^\circ}$$

5. (1)

$$\frac{9}{5} \rightarrow 45$$

$$\frac{1}{5} \rightarrow 45 \div 9 = \underline{5}$$

6. (2)

Number of adults

$$= \frac{3}{5} \times 60$$

$$= 36$$

$$100\% - 25\% = 75\%$$

Number of adults who do not wear glasses

$$= \frac{75}{100} \times 36$$

$$= \underline{27}$$

7. (1)

$$\text{Tom} : \text{Amy} : \text{Johnson}$$

$$1 : 3 : 8$$

$$1 \text{ unit} + 3 \text{ units} + 8 \text{ units} = 12 \text{ units}$$

$$12 \text{ units} = 204 \text{ stickers}$$

$$1 \text{ unit} = 204 \div 12$$

$$= 17 \text{ stickers}$$

Tom received 17 stickers.

8. (4)

$$15 \text{ cm} \div 3 \text{ cm} = 5 \text{ (Length)}$$

$$12 \text{ cm} \div 3 \text{ cm} = 4 \text{ (Breadth)}$$

$$7 \text{ cm} \div 3 \text{ cm} = 2 \text{ R } 1 \text{ cm (Height)}$$

Number of 3-cm cubes

$$= 5 \times 4 \times 2$$

$$= 40$$

9. (3)

Circumference of circle

$$= 4 \times 11 \text{ cm}$$

$$= 44 \text{ cm}$$

$$\frac{22}{7} \times \text{Diameter} = 44$$

$$\text{Diameter} = 44 \div \frac{22}{7}$$

$$= 44 \times \frac{7}{22}$$

$$= 14 \text{ cm}$$

$$\text{Radius} = 14 \text{ cm} \div 2$$

$$= 7 \text{ cm (BC)}$$

Area of square

$$= 7 \times 7$$

$$= 49 \text{ cm}^2$$

10. (3)

$$100\% - 55\% = 45\%$$

$$45\% \rightarrow \$36$$

$$1\% \rightarrow \$\left(\frac{36}{45}\right)$$

$$155\% \rightarrow 155 \times \$\left(\frac{36}{45}\right) = \underline{\$124}$$

11. (4)

Red : Yellow

$$\frac{1}{2} : \frac{1}{8}$$

$$= \frac{4}{8} : \frac{1}{8}$$

$$= \underline{4 : 1}$$

12. (1)

$$\frac{1}{4} - \frac{1}{8} = \frac{2}{8} - \frac{1}{8}$$

$$= \frac{1}{8}$$

$$\frac{1}{8} \times 40 = 5$$

5 more children prefer blue than green.

13. (2)

$$32 \text{ m} \div 4 \text{ m} = 8$$

$$8 \times 13 = 104$$

She can make 104 scarves.

14. (4)

Number of stamps in 1 album

$$= 15 \times 22$$

$$= 330$$

Number of stamps in 4 albums

$$= 4 \times 330$$

$$= \underline{1320}$$

15. (1)

Area of square

$$= 10 \times 10$$

$$= 100 \text{ cm}^2$$

Area of circle

$$= 3.14 \times 5 \times 5$$

$$= 78.5 \text{ cm}^2$$

Total area of shaded parts

$$= 100 - 78.5$$

$$= \underline{21.5 \text{ cm}^2}$$

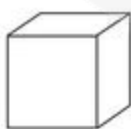
Booklet B:

16. $14r + 9 - 7 + 2r + 8 - 5r$

$$= 14r + 2r - 5r + 9 - 7 + 8$$

$$= 11r + 10$$

17.



18. $36\% \rightarrow 720$

$$1\% \rightarrow 720 \div 36 = 20$$

$$100\% \rightarrow 100 \times 20 = 2000$$

The number is 2000.

$$\frac{4}{5} \times 2000 = \mathbf{1600}$$

19. Square D : Square E

$$5 \quad : \quad 8$$

$$8 \text{ units} = 640 \text{ cm}^2$$

$$1 \text{ unit} = 640 \text{ cm}^2 \div 8$$

$$= 80 \text{ cm}^2$$

$$5 \text{ units} = 5 \times 80 \text{ cm}^2$$

$$= 400 \text{ cm}^2$$

The area of Square D is 400 cm^2 .

Length of Square D

$$= \sqrt{400}$$

$$= 20 \text{ cm}$$

Perimeter of Square D

$$= 4 \times 20 \text{ cm}$$

$$= \mathbf{80 \text{ cm}}$$

20. Cost 5 bags

$$= 5 \times \$78.90$$

$$= \$394.50$$

$$12 \div 3 = 4$$

Cost of 12 T-shirts

$$= 4 \times \$19$$

$$= \$76$$

Total cost

$$= \$394.50 + \$76$$

$$= \$470.50$$

Change

$$= \$500 - \$407.50$$

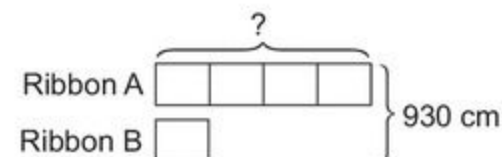
$$= \mathbf{\$29.50}$$

21. $4 \text{ m } 65 \text{ cm} = 465 \text{ cm}$

Total length of 2 ribbons

$$= 2 \times 465 \text{ cm}$$

$$= 930 \text{ cm}$$



$$\begin{aligned}
 5 \text{ units} &= 930 \text{ cm} \\
 1 \text{ unit} &= 930 \div 5 \\
 &= 186 \text{ cm} \\
 4 \text{ units} &= 4 \times 186 \text{ cm} \\
 &= 744 \text{ cm}
 \end{aligned}$$

The length of Ribbon A is **744 cm**.

22. Length of cube

$$\begin{aligned}
 &= \sqrt[3]{144} \\
 &= 12 \text{ cm}
 \end{aligned}$$

$$\begin{aligned}
 \text{Volume of cube} \\
 &= 12 \times 12 \times 12 \\
 &= \mathbf{1728 \text{ cm}^3}
 \end{aligned}$$

23. Curved part of semicircle

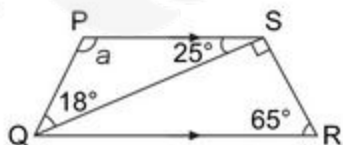
$$\begin{aligned}
 &= \frac{1}{2} \times \frac{22}{7} \times 14 \\
 &= 22 \text{ cm}
 \end{aligned}$$

$$\begin{aligned}
 \text{Perimeter of semicircle} \\
 &= 22 + 14 \\
 &= \mathbf{36 \text{ cm}}
 \end{aligned}$$

$$\begin{aligned}
 24. \quad 6\% &\longrightarrow \$15 \\
 1\% &\longrightarrow \$\left(\frac{15}{6}\right) \\
 100\% &\longrightarrow 100 \times \$\left(\frac{15}{6}\right) = \$250 \\
 12 \times \$250 &= \$3000
 \end{aligned}$$

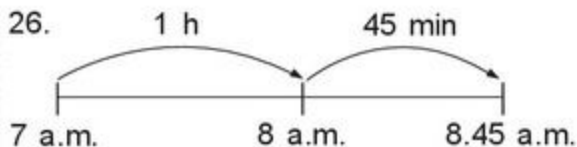
His allowance in a year is **\$3000**.

25.



$$\begin{aligned}
 \angle PSQ &= 180^\circ - 90^\circ - 65^\circ \text{ (\(\angle\)'s between // lines)} \\
 &= 25^\circ
 \end{aligned}$$

$$\begin{aligned}
 \angle a &= 180^\circ - 18^\circ - 25^\circ \text{ (\(\angle\)' sum of \(\Delta\))} \\
 &= \mathbf{137^\circ}
 \end{aligned}$$



$$\begin{aligned}
 1 \text{ h } 45 \text{ min} &= 1 \frac{45}{60} \text{ h} \\
 &= 1 \frac{3}{4} \text{ h}
 \end{aligned}$$

Average speed

$$\begin{aligned}
 &= 140 \text{ km} \div 1 \frac{3}{4} \text{ h} \\
 &= 140 \text{ km} \div \frac{7}{4} \text{ h} \\
 &= 140 \text{ km} \times \frac{4}{7} \text{ h} \\
 &= \mathbf{80 \text{ km/h}}
 \end{aligned}$$

27. Volume of water in tank

$$\begin{aligned}
 &= \frac{1}{5} \times 20 \times 18 \times 15 \\
 &= \frac{1}{5} \times 5400 \\
 &= 1080 \text{ cm}^3
 \end{aligned}$$

$$30 \text{ cm}^3 \longrightarrow 1 \text{ min}$$

$$1 \text{ cm}^3 \longrightarrow \frac{1}{30} \text{ min}$$

$$1080 \text{ cm}^3 \longrightarrow 1080 \times \frac{1}{30} = 36 \text{ min}$$

It will take **36 min** to empty the tank completely.

$$28. \quad 2 \times 50 \text{ cm}^2 = 100 \text{ cm}^2$$

Radius of circle

$$\begin{aligned}
 &= \sqrt{100} \\
 &= 10 \text{ cm}
 \end{aligned}$$

Area of shaded part

$$\begin{aligned}
 &= \frac{3}{4} \times 3.14 \times 10 \times 10 \\
 &= \mathbf{235.5 \text{ cm}^2}
 \end{aligned}$$

29. $100\% - 25\% = 75\%$

Selling price of computer

$$= \frac{75}{100} \times \$2800$$

$$= \$2100$$

30. $\frac{3}{13} \times 2\frac{1}{6}$ kg

$$= \frac{1\cancel{3}}{1\cancel{13}} \times \frac{13^1}{6_2}$$

$$= \frac{1}{2}$$
 kg (Given to Jennifer)

Mass of longans she ate

$$= 2\frac{1}{6} - \frac{1}{2}$$

$$= 1\frac{7}{6} - \frac{3}{6}$$

$$= 1\frac{4}{6}$$

$$= 1\frac{2}{3}$$
 kg

PAPER 2

1. Area of rectangle

$$= 248 \text{ cm}^2 \div 2$$

$$= 124 \text{ cm}^2$$

Breadth of rectangle

$$= 124 \text{ cm}^2 \div 16 \text{ cm}$$

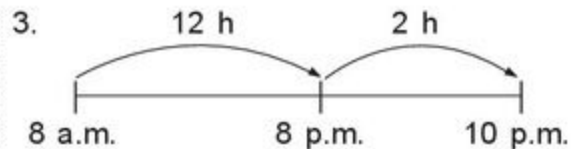
$$= 7.75 \text{ cm}$$

2. $1346 - 38 = 1308$

Total collection

$$= 1308 \times \$0.08$$

$$= \$104.64$$



$$12 \text{ h} + 2 \text{ h} = 14 \text{ h}$$

$$1 - \frac{9}{20} - \frac{3}{20} - \frac{3}{10} = \frac{1}{10}$$

$$\frac{1}{10} \div 2 = \frac{1}{10} \times \frac{1}{2}$$

$$= \frac{1}{20}$$

$$\frac{9}{20} + \frac{1}{20} = \frac{10}{20}$$

$$= \frac{1}{2}$$

$$\frac{1}{2} \times 14 \text{ h} = 7 \text{ h}$$

She spent 7 h doing her homework and playing computer games.

4. Curved part of small semicircle

$$= \frac{1}{2} \times 3.14 \times 3$$

$$= 4.71 \text{ cm}$$

Curved part of big semicircle

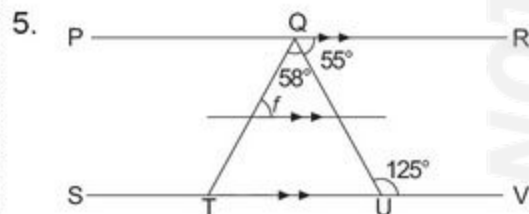
$$= \frac{1}{2} \times 3.14 \times 4$$

$$= 6.28 \text{ cm}$$

Length of wire

$$= 4.71 + 6.28 + 3 + 4$$

$$= 17.99 \text{ cm}$$



$$\angle RQU = 180^\circ - 125^\circ \text{ (}\angle\text{s between // lines)}$$

$$= 55^\circ$$

$$\angle f = 180^\circ - 55^\circ - 58^\circ \text{ (}\angle\text{s between // lines)}$$

$$= 67^\circ$$

6. (a) Sarah's share
 $= (150 - h) \div 3$
 $= \left(\frac{150 - h}{3}\right)$ necklaces
 Sarah's share was $\left(\frac{150 - h}{3}\right)$ necklaces.

(b) When $h = 36$,

$$\frac{150 - h}{3} = \frac{150 - 36}{3}$$

$$= \frac{114}{3}$$

$$= 38$$

Joan got **38** necklaces.

7. $2 \text{ dresses} + 3 \text{ bags} \rightarrow \367
 $\times 2 \left(\begin{array}{l} 1 \text{ dress} + 2 \text{ bags} \rightarrow \$212 \\ 2 \text{ dresses} + 4 \text{ bags} \rightarrow 2 \times \$212 = \$424 \end{array} \right)$

$$\begin{array}{l} 1 \text{ bag} \rightarrow \$424 - \$367 = \$57 \\ 1 \text{ dress} \rightarrow \$212 - (2 \times \$57) \\ \quad = \$212 - \$114 \\ \quad = \$98 \end{array}$$

$1 \text{ dress} + 1 \text{ bag} \rightarrow \$98 + \$57 = \155
 $6 \text{ dresses} + 6 \text{ bags} \rightarrow 6 \times \$155 = \$930$

The total cost of 6 such dresses and 6 such bags is **\$930**.

8. (a) Number of different triangles
 $= 1 + 2 + 3 + 4$
 $= 10$

She would get **10** different triangles.

(b) Number of different triangles
 $= 1 + 2 + 3 + 4 + 5 + 6 + 7$
 $+ 8 + 9 + 10 + 11$
 $= 66$

Alternative method:

$$\frac{11}{2} \times (1 + 11) = 66$$

She would get **66** different triangles.

9. $80\% = \frac{80}{100} = \frac{4}{5}$, $60\% = \frac{60}{100} = \frac{3}{5}$

Leslie : Jonathan : Jane
 $\frac{4 \times 3}{5 \times 3}$: $\frac{5 \times 3}{5 \times 3}$
 $= 12$: 15
 $\quad \quad \quad \frac{3 \times 5}{5 \times 5}$: $\frac{5 \times 5}{5 \times 5}$
 $\quad \quad \quad = 15$: 25

$= 12$: 15 : 25

$15 \text{ units} + 25 \text{ units} = 40 \text{ units}$



$4 \text{ parts} = 40 \text{ units}$

$1 \text{ part} = 40 \text{ units} \div 4 = 10 \text{ units}$

$3 \text{ parts} = 3 \times 10 \text{ units} = 30 \text{ units}$

After:

Leslie : Jonathan : Jane
 12 : 10 : 30

$15 \text{ units} - 10 \text{ units} = 5 \text{ units}$

$5 \text{ units} = 505 \text{ stamps}$

$1 \text{ unit} = 505 \div 5$

$= 101 \text{ stamps}$

$40 \text{ units} = 40 \times 101$

$= 4040 \text{ stamps}$

Jane and Jonathan had **4040** stamps at first.

10. Area of $\triangle ABC$

$= \frac{1}{2} \times 15 \times 15$

$= 112.5 \text{ cm}^2$

Area of quadrant

$= \frac{1}{4} \times \pi \times 7 \times 7$

$= 38.485 \text{ cm}^2$

$$\begin{aligned} &\text{Area of shaded part} \\ &= 112.5 - 38.485 \\ &= 74.02 \text{ cm}^2 \text{ (correct to 2 d.p.)} \end{aligned}$$

The area of the shaded part of the triangle is **74.02 cm²**.



Distance (1st part of journey)

$$\begin{aligned} &= 60 \text{ km/h} \times 6\frac{1}{2} \text{ h} \\ &= 390 \text{ km} \end{aligned}$$

$$\frac{1}{3} \rightarrow 390 \text{ km}$$

$$\frac{3}{3} \rightarrow 3 \times 390 \text{ km} = 1170 \text{ km}$$

The distance of the journey was **1170 km**.

(b) Average speed (Return journey)

$$\begin{aligned} &= 1170 \text{ km} \div 15 \text{ h} \\ &= 78 \text{ km/h} \end{aligned}$$

His average speed on his return journey was **78 km/h**.

12. Number of men

$$\begin{aligned} &= 1350 - 810 \\ &= 540 \end{aligned}$$

Number of men who wore glasses

$$\begin{aligned} &= \frac{8}{9} \times 540 \\ &= 480 \end{aligned}$$

Number of women who wore glasses

$$\begin{aligned} &= \frac{5}{6} \times 810 \\ &= 675 \end{aligned}$$

$$480 + 675 = 1155$$

1155 men and women wore glasses at the funfair altogether.

13. (a) $\frac{1}{2} - \frac{2}{5} = \frac{1}{10}$

$$\frac{1}{10} \rightarrow 8.5 \text{ l}$$

$$\begin{aligned} \frac{10}{10} &\rightarrow 10 \times 8.5 \text{ l} \\ &= 85 \text{ l} \\ &= 85\,000 \text{ cm}^3 \end{aligned}$$

Height of tank

$$\begin{aligned} &= 85\,000 \text{ cm}^3 \div 1250 \text{ cm}^2 \\ &= 68 \text{ cm} \end{aligned}$$

The height of the tank is **68 cm**.

(b) $\frac{2}{5} \times 85 \text{ l} = 34 \text{ l}$

The volume of water in the tank when it was $\frac{2}{5}$ filled was **34 l**.

14. $500 - 325 = 175$

$$\frac{60}{100} \times 175 = 105$$

$$325 \times \$2 = \$650$$

$$105 \times \$1.50 = \$157.50$$

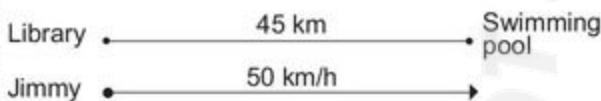
$$\$849.50 - \$650 - \$157.50 = \$42$$

$$500 - 105 - 325 = 70 \text{ balloons}$$

$$\$42 \div 70 = \$0.60$$

She sold each of the rest of the balloons for **\$0.60**.

15.



Time taken by Jimmy

$$= 45 \text{ km} \div 50 \text{ km/h}$$

$$= \frac{9}{10} \text{ h}$$

Time taken by Tony

$$\begin{aligned} &= \frac{9}{10} h - \frac{2}{5} h \leftarrow \frac{24}{60} h = \frac{2}{5} h \\ &= \frac{1}{2} h \end{aligned}$$

Tony's average speed

$$\begin{aligned} &= 45 \text{ km} \div \frac{1}{2} h \\ &= 90 \text{ km/h} \end{aligned}$$

Tony's average speed was **90 km/h**.

16. Area of larger semicircle

$$\begin{aligned} &= \frac{1}{2} \times 3.14 \times 14 \times 14 \\ &= 307.72 \text{ cm}^2 \end{aligned}$$

Area of smaller semicircle

$$\begin{aligned} &= 307.72 - 207.24 \\ &= 100.48 \text{ cm}^2 \end{aligned}$$

$$\frac{1}{2} \times 3.14 \times \text{Radius} \times \text{Radius} = 100.48$$

$$\begin{aligned} \text{Radius} \times \text{Radius} &= \frac{100.48 \times 2}{3.14} \\ &= 64 \\ &= 8 \times 8 \\ \text{Radius} &= 8 \text{ cm} \end{aligned}$$

Breadth of rectangle = 8 cm

Length of rectangle = $2 \times 8 \text{ cm}$
= 16 cm

Area of rectangle

$$\begin{aligned} &= 16 \times 8 \\ &= 128 \text{ cm}^2 \end{aligned}$$

Area of shaded part

$$\begin{aligned} &= 128 - 100.48 \\ &= 27.52 \text{ cm}^2 \end{aligned}$$

The area of the shaded part is **27.52 cm²**.

17. $1135 \times \$0.40 = \454

$$\$552 - \$454 = \$98$$

$$1135 \div 40 = 28 \text{ R } 15 \text{ (28 sets)}$$

$$\$98 \div 28 = \$3.50$$

The bonus she got for every 40 bags she sold was **\$3.50**.

Trial Examination 2

PAPER 1

Booklet A:

1. (4)

$$\begin{aligned}\text{Area of square} \\ &= 3 \times 3 \\ &= 9 \text{ cm}^2\end{aligned}$$

$$\begin{array}{r} \text{Area of square} : \text{Area of triangle} \\ 9 \quad \quad \quad : \quad 36 \\ \hline 1 \quad \quad \quad : \quad 4 \end{array}$$

2. (3)

$$\begin{aligned}\frac{24}{96} \times 100\% &= \frac{1}{4} \times 100\% \\ &= 25\%\end{aligned}$$

The number in the box is 25.

3. (1)

$$\begin{aligned}\text{Average speed} \\ &= 160 \text{ km} \div 2\frac{1}{2} \text{ h} \\ &= 160 \text{ km} \div \frac{5}{2} \text{ h} \\ &= 160 \text{ km} \times \frac{2}{5} \text{ h} \\ &= \underline{64 \text{ km/h}}\end{aligned}$$

4. (3)

$$\begin{aligned}\text{Area of 1 quarter circle} \\ &= \frac{1}{4} \times 3.14 \times 4 \times 4 \\ &= 12.56 \text{ cm}^2\end{aligned}$$

$$\begin{aligned}\text{Area of figure} \\ &= 5 \times 12.56 \text{ cm}^2 \\ &= \underline{62.8 \text{ cm}^2}\end{aligned}$$

5. (2)

$$\begin{aligned}\text{When } k = 12, \\ \frac{5k}{2} + 2k &= \frac{5(12)}{2} + 2(12) \\ &= 30 + 24 \\ &= 54\end{aligned}$$

6. (3)

$$\begin{array}{l} \text{Mangoes } \boxed{\quad} \boxed{60} \\ \text{Apples } \boxed{\quad} \end{array} \left. \vphantom{\begin{array}{l} \text{Mangoes} \\ \text{Apples} \end{array}} \right\} 480$$

$$\begin{aligned}2 \text{ units} &= 480 - 60 \\ &= 420 \text{ fruits} \\ 1 \text{ unit} &= 420 \div 2 \\ &= 210 \text{ fruits (Apples)}\end{aligned}$$

$$210 + 60 = 270 \text{ (Mangoes)}$$

$$\begin{array}{l} \text{Apples} : \text{Mangoes} \\ 210 : 270 \\ = 21 : 27 \\ = \underline{7 : 9} \end{array}$$

7. (1)

$$\begin{aligned}\text{Breadth} \\ &= \frac{2}{3} \times 90 \text{ cm} \\ &= 60 \text{ cm}\end{aligned}$$

$$\begin{aligned}\text{Base area} \\ &= 90 \times 60 \\ &= 5400 \text{ cm}^2\end{aligned}$$

$$\begin{aligned}\text{Height of box} \\ &= 70\,200 \text{ cm}^3 \div 5400 \text{ cm}^2 \\ &= \underline{13 \text{ cm}}\end{aligned}$$

8. (1)

$$\begin{aligned}\text{Diameter of smaller semicircle} \\ &= \frac{2}{3} \times 12 \\ &= 8 \text{ cm}\end{aligned}$$

$$\begin{aligned}\text{Area of smaller semicircle} \\ &= \frac{1}{2} \times 3.14 \times 4 \times 4 \\ &= \underline{25.12 \text{ cm}^2}\end{aligned}$$

9. (1)
It has 5 faces.

10. (2)
 $\angle k = 180^\circ - 85^\circ - 26^\circ$ (\angle s on a straight line)
 $= \underline{69^\circ}$

11. (3)

$$\frac{1}{2} - \frac{1}{6} - \frac{1}{6} = \frac{3}{6} - \frac{1}{6} - \frac{1}{6}$$

$$= \frac{1}{6}$$

$$\frac{1}{2} - \frac{1}{6} = \frac{3}{6} - \frac{1}{6}$$

$$= \frac{2}{6}$$

$$= \frac{1}{3}$$

$$\frac{1}{3} \times \$1830 = \$610$$

She spends \$610 more on her car instalment than clothing in a month.

12. (2)
Distance travelled
 $= 72 \text{ km/h} \times \frac{55}{60} \text{ h}$
 $= 72 \text{ km/h} \times \frac{11}{12} \text{ h}$
 $= 66 \text{ km}$

$$1 \text{ km} \longrightarrow 1.5 \text{ l}$$

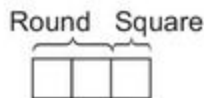
$$66 \text{ km} \longrightarrow 66 \times 1.5 \text{ l} = 99 \text{ l}$$

His car used up 99 l of petrol.

13. (3)
 $12 \times \$6 = \72
 $\frac{72}{1200} \times 100\% = 6\%$
 $6\% - 3\% = 3\%$

The annual rate of interest rose by 3%.

14. (3)



$$2 \text{ units} - 1 \text{ unit} = 1 \text{ unit}$$

$$1 \text{ unit} = 35 \text{ stickers (Square)}$$

$$3 \text{ units} = 3 \times 35$$

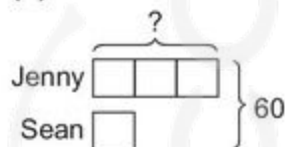
$$= 105 \text{ stickers (Total)}$$

$$35 + 2 = 37$$

$$105 + 2 = 107$$

$$\text{Required fraction} = \frac{37}{107}$$

15. (4)



$$4 \text{ units} = 60 \text{ phonecards}$$

$$1 \text{ unit} = 60 \div 4$$

$$= 15 \text{ phonecards}$$

$$3 \text{ units} = 3 \times 15$$

$$= 45 \text{ phonecards}$$

Jenny had 45 phonecards.

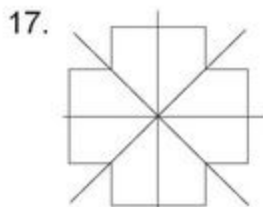
Booklet B:

16. Area of base
 $= 18 \times 15$
 $= 270 \text{ cm}^2$

$$\text{Height}$$

$$= 3240 \text{ cm}^3 \div 270 \text{ cm}^2$$

$$= 12 \text{ cm}$$



There are **4** lines of symmetry in the figure.

18. = $36 \div 3$
= 12 stamps

= $48 \div 2$
= 24 stamps

+ = $24 + 12$
= 36 stamps

19. $27 \div 3 = 9$
 $9 \times 4y = 36y$

The mass of 27 packets of sugar is **36y kg**.

20. $2 \text{ min} = 2 \times 60 = 120 \text{ s}$
 $1 \text{ s} \rightarrow 4\frac{1}{2} \text{ revolutions}$

$120 \text{ s} \rightarrow 120 \times 4\frac{1}{2}$
 $= 120 \times \frac{9}{2}$
 $= 540 \text{ revolutions}$

The fan will make **540** revolutions in 2 minutes.

21. Area of garden
 $= 40 \times 10$
 $= 400 \text{ m}^2$
 $1 - \frac{3}{8} = \frac{5}{8}$

Area of garden not planted with carrots
 $= \frac{5}{8} \times 400$
 $= 250 \text{ m}^2$

22. $100\% - 10\% = 90\%$

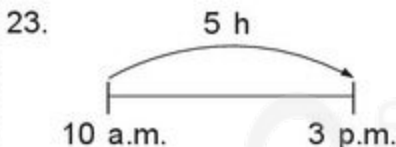
$90\% \rightarrow \$252$

$1\% \rightarrow \$\left(\frac{252}{90}\right)$

$100\% \rightarrow 100 \times \$\left(\frac{252}{90}\right) = \280

Price of fan after final discount

$= \frac{65}{100} \times \280
 $= \mathbf{\$182}$



Average speed
 $= 160 \text{ km} \div 5 \text{ h}$
 $= 32 \text{ km/h}$

24. (a) Smallest even number = 2796
(b) Number closest to 7000 = 6972

25. $\angle BCD = 62^\circ$ (opp. \angle s of a parallelogram)
 $\angle ACB = (180^\circ - 126^\circ) \div 2$ (isos. \triangle)
 $= 54^\circ \div 2$
 $= 27^\circ$

$\angle ACD = 62^\circ + 27^\circ$
 $= 89^\circ$

26. (a) $32 - 18 = 14$
He sold **14** more cameras in August than in June.

(b) May : September
 24 : 36
 $= 2$: 3

27. $\begin{array}{|c|c|} \hline 425 \text{ km} & 300 \text{ km} \\ \hline 3\frac{2}{5} \text{ h} & 1\frac{3}{5} \text{ h} \\ \hline \end{array}$

Total distance
 $= 425 + 300$
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Total time
 $= 3\frac{2}{5} \text{ h} + 1\frac{3}{5} \text{ h}$
 $= 5 \text{ h}$

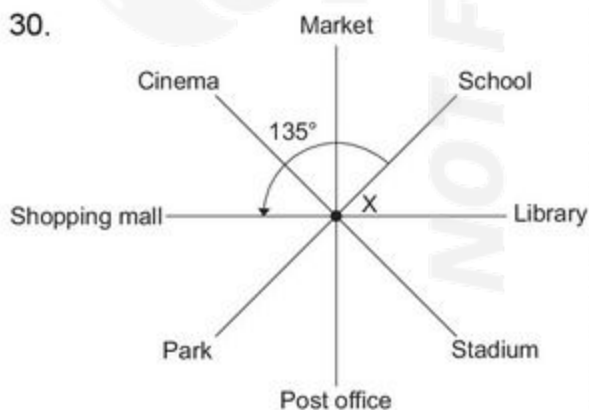
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 $= 12^\circ$

29. $100\% - 20\% = 80\%$
 $80\% \rightarrow \$50$
 $1\% \rightarrow \$\left(\frac{50}{80}\right)$
 $100\% \rightarrow 100 \times \$\left(\frac{50}{80}\right)$
 $= \$62.50$

Original price of 1 wallet
 $= \$62.50 \div 5$
 $= \$12.50$



He will be facing the shopping mall now.

PAPER 2

1. $\frac{1}{2} - \frac{1}{8} = \frac{4}{8} - \frac{1}{8}$
 $= \frac{3}{8}$

$\frac{1}{4} = \frac{2}{8}$

$\frac{2}{8} \rightarrow 712 \text{ items}$

$\frac{1}{8} \rightarrow 712 \div 2 = 356 \text{ items}$

$\frac{3}{8} \rightarrow 3 \times 356 = 1068 \text{ items}$

He sold **1068** more pens and rulers than pencils.

2. $6 \text{ m} = 600 \text{ cm}$
 $3 \text{ m} = 300 \text{ cm}$

$600 \text{ cm} \div 30 \text{ cm} = 20$
 $300 \text{ cm} \div 30 \text{ cm} = 10$

Number of tiles
 $= 20 \times 10$
 $= 200$

Cost of tiles
 $= 200 \times \$5.90$
 $= \$1180$

3. $7 \times 4 \times 3 = 84 \text{ m}^3$
 $84 \text{ m}^3 \div 3 \text{ m}^3 = 28 \text{ people}$

4. Sally

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 \$180
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 {
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$3 \text{ units} = \$900 - \180
 $= \$720$

$1 \text{ unit} = \$720 \div 3$
 $= \$240$

$\$240 + \$900 = \$1140$
 $2 \times \$1140 = \2280

Both of them had **\$2280** at first.

5. Radius = $18 \text{ cm} \div 3 = 6 \text{ cm}$

Area of circle
 $= 3.14 \times 6 \times 6$
 $= 113.04 \text{ cm}^2$

Area of each unshaded part
 $= 113.04 - 50.24$
 $= 62.8 \text{ cm}^2$

Total area of unshaded parts
 $= 2 \times 62.8 \text{ cm}^2$
 $= 125.6 \text{ cm}^2$

6. Length + Breadth = $70 \text{ cm} \div 2$
 $= 35 \text{ cm}$

$$4a + 4 + a + 3.4 = 35$$

$$5a + 7.4 = 35$$

$$5a = 35 - 7.4$$

$$= 27.6$$

$$a = 27.6 \div 5$$

$$= 5.52$$

Length = $4(5.52) + 4$
 $= 26.08 \text{ cm}$

Breadth = $5.52 + 3.4$
 $= 8.92 \text{ cm}$

Area of rectangle
 $= 26.08 \times 8.92$
 $= 232.6336 \text{ cm}^2$

The area of the rectangle is **232.6336 cm²**.

7. (a) $15 \text{ cm} \div 3 = 5 \text{ cm}$
 The length of one side of the square base is **5 cm**.

(b) Height
 $= (26 - 5 - 5) \div 2$
 $= 16 \div 2$
 $= 8 \text{ cm}$

Volume cuboid
 $= 5 \times 5 \times 8$
 $= 200 \text{ cm}^3$

The volume of the cuboid is **200 cm³**.

8. $\frac{\text{Green}}{3 \times 3} : \frac{\text{Red}}{3 \times 2} : \frac{\text{Blue}}{7 \times 2}$
 $3 \times 3 : 2 \times 3$

$9 : 6 : 14$

$9 \text{ units} + 6 \text{ units} + 14 \text{ units} = 29 \text{ units}$

$29 \text{ units} = 87 \text{ beads}$
 $1 \text{ unit} = 87 \div 29$
 $= 3 \text{ beads}$

$9 \text{ units} + 14 \text{ units} = 23 \text{ units}$

$23 \text{ units} = 23 \times 3$
 $= 69 \text{ beads}$

The total number of blue and green beads is **69**.

9. Area of square flower bed
 $= 5 \times 5$
 $= 25 \text{ m}^2$

Area of rectangular garden
 $= 4 \times 25 \text{ m}^2$
 $= 100 \text{ m}^2$

Breadth of rectangular garden
 $= 100 \text{ m}^2 \div 20 \text{ m}$
 $= 5 \text{ m}$

Perimeter of rectangular garden
 $= 20 + 5 + 20 + 5$
 $= 50 \text{ m}$

Cost of fencing
 $= 50 \times \$21.50$
 $= \$1075$

The cost of fencing the rectangular garden is **\$1075**.

10. Area of shaded part
 = Area of big semicircle
 = $\frac{1}{2} \times \pi \times 14 \times 14$
 = 307.88 cm^2 (correct to 2 d.p.)

The area of the shaded part is **307.88 cm²**.

11. (a) Area of Rectangle ABCD
 = 24×14
 = 336 cm^2

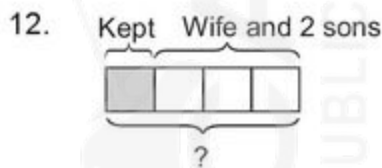
Area of 4 shaded squares
 = $4 \times (3 \times 3)$
 = 36 cm^2

$336 - 36 = 300 \text{ cm}^2$

The area of the cardboard left is **300 cm²**.

(b) Volume of box
 = $18 \times 8 \times 3$
 = 432 cm^3

The volume of the box is **432 cm³**.



Wife : Elder son : Younger son
 7 : 5 : 3

$5 \text{ units} - 3 \text{ units} = 2 \text{ units}$

$2 \text{ units} = \$765$

$1 \text{ unit} = \$765 \div 2$
 = $\$382.50$

$7 \text{ units} + 5 \text{ units} + 3 \text{ units} = 15 \text{ units}$

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Uncle Sam had **\\$7650** in savings.



Time taken by Uncle Lee
 = $120 \text{ km} \div 50 \text{ km/h}$
 = $2\frac{2}{5} \text{ h}$

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 = $120 \text{ km} \div 64 \text{ km/h}$
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Uncle Soh will reach the airport $\frac{21}{40} \text{ h}$ earlier.

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 = $\frac{15}{100} \times \$2400$
 = $\$360$

$\$2400 - \$360 - \$1290 = \750

Amount he spends on food
 = $\frac{40}{100} \times \$750$
 = $\$300$

$\$750 - \$300 = \$450$

He saves **\\$450** each month.

15. Total number of notebooks

$$\begin{aligned} &= 8 \times 20 \\ &= 160 \end{aligned}$$

$$\frac{60}{100} \times 160 = 96 \text{ books (Sold at \$1.20)}$$

$$96 \times \$1.20 = \$115.20$$

$$160 - 96 = 64$$

$$\frac{75}{100} \times 64 = 48 \text{ books}$$

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$$\frac{80}{100} \times \$1.20 = \$0.96$$

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He spent **\\$96.48** on buying the notebooks.

16. Area of rectangle

$$\begin{aligned} &= 16 \times 14 \\ &= 224 \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} \text{Area of big circle} \\ &= 3.14 \times 3.5 \times 3.5 \\ &= 38.465 \text{ cm}^2 \end{aligned}$$

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The area of the figure is **275.03 cm²**.

$$\begin{aligned} \text{Circumference of big circle} \\ &= 3.14 \times 7 \\ &= 21.98 \text{ cm} \end{aligned}$$

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Perimeter of figure

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17. Selling price of a game software

$$\begin{aligned} &= \$16 \div 2 \\ &= \$8 \end{aligned}$$

$$\begin{aligned} 6 \times \$8 &= \$48 \\ \$240 - \$48 &= \$192 \end{aligned}$$

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$$8 + 8 + 6 = 22$$

He bought **22** computer software.

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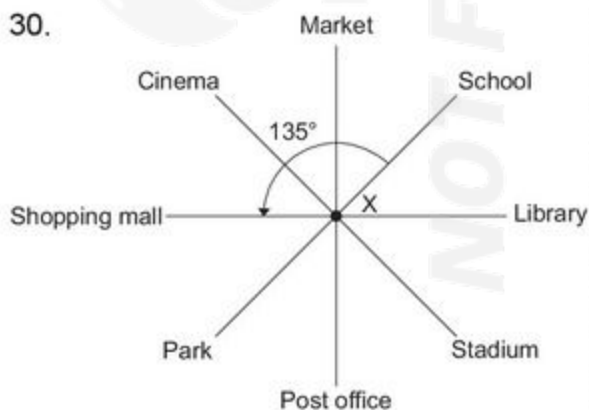
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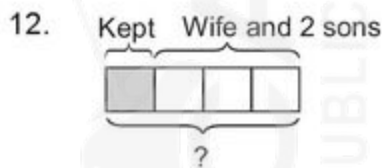
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He bought **22** computer software.